## GAUSS $15{ }^{\mathrm{TM}}$

## User Guide

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## 1 Introduction

### 1.1 Product Overview

The GAUSS Mathematical and Statistical System (GAUSS) ${ }^{\mathrm{TM}}$ is a complete analysis environment suitable for performing quick calculations, complex analysis of millions of data points, or anything in between. Whether you are new to computerized analysis or a seasoned programmer, the GAUSS family of products combine to offer you an easy to learn environment that is powerful and versatile enough for virtually any numerical task.

Since its introduction in 1984, GAUSS has been the standard for serious number crunching and complex modeling of large-scale data. Worldwide acceptance and use in government, industry, and the academic community is a firm testament to its power and versatility.

The GAUSS System can be described several ways: It is an exceptionally efficient number cruncher, a comprehensive programming language, and an interactive analysis environment. GAUSS may be the only numerical tool you will ever need.

### 1.2 Documentation Conventions

The following table describes how text formatting is used to identify GAUSS programming elements:

| Text Style | Use | Example |
| :---: | :---: | :---: |
| regular text | narrative | $" \ldots$ text formatting is |


| bold text | emphasis |
| :--- | :--- |
| italics | variables |
| monospace | code example |
| monospace | filename, path, etc. <br> monospace <br> bold |
| reference to a GAUSS <br> command or other <br> programming element <br> within a narrative <br> paragraph |  |
| Bold Text | reference to section of the <br> manual |

used ..."
"...not supported under UNIX."
"... If vnames is a string or has fewer elements than $x$ has columns, it will be ..."
if scalerr(cm); cm = inv(x); endif;
"...is located in the
examples subdirectory..." "...as explained under plotScatter..."
"...see Operator Precedence, Section 10.7 ..."

## 2 Getting Started

### 2.1 Installation Under Linux

1. Make a directory to install GAUSS in.

NOTE: If you choose to install GAUSS in a directory which does not have write permissions for normal user accounts such as /opt or /usr/local, then you must choose the Advanced Installation and Multi-User Installation options during installation.
2. cd to that directory.
3. Gunzip the.$g z$ file.
4. Untar the . tar file.
5. Run the executable script ginstall.

The script will give you the option of a default or advanced install. The default option will install everything under the current directory.

The advanced installation allows you to choose a single-user or multi-user installation and also allows you to place the shared libraries that GAUSS depends on in another location. If you choose a multi-user installation, the binaries and most of
the rest of the installation will reside in the current directory. Each time a new user (a user that has never started GAUSS on this machine ) starts GAUSS on this machine, GAUSS will create a local working directory for that user under the user's home directory. This local working directory will contain the files and folders that which may be customized by the user. This allows the admin to install GAUSS in a location without universal write privileges. No files will be placed under the home directory of any user who does not start GAUSS.
6. Put the installation directory in the executable path.
7. Install the license. To receive a license and license installation instructions, click here and include the hostid information of your machine. The hostid number of your machine is usually generated automatically during installation and stored in the main GAUSS directory in a file called myhostid.txt.

For last-minute information, see README.term.

### 2.2 Installation Under Windows

Following are the minimum recommended machine requirements and information on how to install GAUSS under Windows.

### 2.2.1 Machine Requirements

- Operating System and Memory (RAM) requirements: Aptech strongly recommends Windows 7 for greatest performance and reliability.
- Windows Vista 32-bit, 512 MB minimum, 2 GB recommended.
- Windows Vista 64 -bit, 1 GB minimum, 2 GB or more recommended.
- Windows 7 32-bit, 1 GB minimum, 2 GB or more recommended.
- Windows 7 64-bit, 2 GB minimum, 4 GB or more recommended.
- Windows 8 32-bit, 1 GB minimum, 2 GB or more recommended.
- Windows 8 64-bit, 2 GB minimum, 4 GB or more recommended.
- Minimum of 200 MB free hard disk space, more may be needed depending on the size of matrices and the complexity of the program.
- Minimum of 128 MB of RAM for video is required to run 3-D graphics. A dedicated graphics card is not required.
- Monthly defragmenting is recommended for traditional hard drives. Solid-state drives should not be defragmented.


### 2.2.2 Installation from Download

For information on downloading and download instructions, click here

### 2.2.3 Installation from CD

Insert the GAUSS compact disc into the CD-ROM drive, and setup should start automatically. If setup does not start automatically, browse to the CD-ROM drive, and double-click on the *.msi file to launch the installer.

You can use this procedure for the initial installation of GAUSS, and for additions or modifications to GAUSS components.

## Obtaining a license

To receive a license and license installation instructions, click here and include the hostid information of your machine. The hostid number of your machine is usually generated automatically during installation and stored in the main GAUSS directory in a file called myhostid.txt.

## 3 Introduction to the GAUSS Graphical User Interface

### 3.1 Page Organization Concept

GAUSS graphical user interface is organized into six separate "pages," each designed to facilitate the performance of one of the common tasks performed in GAUSS:

Command Page For executing interactive commands.
Source Page For editing program files.
Data Page For examining and editing GAUSS matrices and other data.

Debug Page For interactively debugging your programs.
Graphics Page For viewing and interacting with graphs.
Help Page For accessing the GAUSS help system.

Pages are separate, customizable, main windows with their own set of widgets. Each page is shown as a tab on the left-hand side of the main application, allowing you to instantly access a window custom-configured for the task you wish to perform.


Figure 3.1: GAUSS page tabs along the left side of the application

Pages may be undocked from the main application and redocked by toggling the Dock button on the right side of the status bar. Navigation between an undocked page and the main application may be accomplished with ALT+TAB and ALT+SHIFT+TAB. To navigate between pages, use CTRL+TAB to cycle forward and CTRL+SHIFT+TAB to cycle backward.

Each page has its own toolbars and menus, which perform desired functions and facilitate intuitive navigation through the GUI. For example, clicking the " New" toolbar button from any page in the GUI will bring the Source Page to the top of the window stack with a new file open and ready for editing.

### 3.2 Command Page

The Command Page is designed for entering interactive commands and viewing results.


Figure 3.2: Command Page

### 3.2.1 Command Page Menus

## File Menu

New

Open File

Open Project
Folder
Open Graph

Print Prints selected text.
Recent Files
Exit

## Edit Menu

Undo Restores your last unsaved change.
Redo Re-inserts changes removed with undo.
Cut Removes selected text and copies it to the clipboard.
Copy Copies selected text to the clipboard.
Paste Pastes the clipboard contents at the cursor position.

## Search

Advanced Search Opens the Source Browser.

## Tools Menu

| Preferences | Allows you to configure the GAUSS user <br> environment. |
| :--- | :--- |
| Install Application | Opens an installation wizard to install a GAUSS <br> application package. |
| Change Font | Allows you to specify a new font. Aptech <br> recommends using a monospaced font such as <br> Courier. |
| Clear Action List | Clears the recent files from the action list menus. |
| Change Working | Allows you to browse for a new working directory. |
| Directory | Deletes the contents of your recent working directory <br> Clear Working <br> history. |
| Recent Working <br> Directories | Contains a dropdown list of your most recent <br> working directories. |

## View Menu

The View menu lets you toggle on or off the windows on the current page.

## Help Menu

Goto Help Takes you to the Help Page.
About GAUSS Provides information regarding your version of GAUSS .

### 3.2.2 Command Page Toolbar



Figure 3.3: Command Page Toolbar

| New | Opens a new, untitled document in a programming <br> editor on the Source Page and brings you to the <br> Source Page. |
| :--- | :--- |
| Open | Opens an existing file for editing. <br> Open Folder |
| Adds a folder and its contents to the GAUSS project |  |
| window on the Source Page. |  |
| Cut | Removes selected text and places it on the clipboard. |
| Copy | Copies selected text to the clipboard. |
| Paste | Copies the clipboard contents to the cursor position. |
| Print | Prints selected text. |
| Run | Runs the file at the top of the Action List. |


| Debug | Debugs the file at the top of the Action List. |
| :--- | :--- |
| Edit | Opens the file at the top of the Action List. |
| Stop Program | Stops a running GAUSS program. |

### 3.2.3 Working Directory Toolbar



Figure 3.4: Working Directory Toolbar
The Working Directory Toolbar contains a dropdown list that shows your current working directory and a history of recent directories. The Change Working Directory button allows you to browse for and select a new working directory.

### 3.2.4 Command History Toolbar



Figure 3.5: Command History Toolbar

| Run | Executes the highlighted command from the <br> command history. |
| :--- | :--- |
| Paste | Pastes the highlighted command to the Program <br> Input/Output Window for further editing. |
| Search Previous | Searches the Command Output Window for previous <br> executions of a command and its output. |
| Search Next | Searches the Command Output Window for the next <br> execution of a command and its output. |

### 3.2.5 Action List Toolbar



Figure 3.6: Action List Toolbar

Run
Debug
Edit
Stop

Executes a file from the Action List.
Debugs a file from the Action List.
Edits a file from the Action List.
Stops a program that is currently running or being debugged.

The Action List is a dropdown list of the files you have most recently performed an action on. Clicking on the Run, Debug, or Edit button will perform the specified action on the file at the top of the Action List. Placing your mouse over the button produces a tooltip with the name of that file. To perform an action on a different file in the Action List, click on the downward-pointing triangle immediately to the right of the desired button.

All of the buttons share the same Action List. You may add a file to the Action List by running it from the command line. Or while editing a file, you can either select Current File from the dropdown menu next to the Run or Debug button or Add to List from the Edit dropdown menu.

### 3.2.6 Layout and Usage

The Command Page contains three main widgets: the Program Input/Output Window, the Command History Window, and the Error Output Window.


Figure 3.7: Command Page Widgets

### 3.2.7 Command History Window

The Command History Window contains a list of recently-executed commands organized by date or by GAUSS session. To re-run a command, double-click on it or select the command and then press the Enter key.

## Context Menu



Figure 3.8: Command History

Right-click in the Command History Window to bring up the context menu with the following options:
Copy
Copies the highlighted entry to the clipboard.
Delete Deletes the highlighted entry.
Clear Window Deletes all Command History entries.
Send to File Creates a new source file containing the highlighted commands.
Toggle View Mode Toggles between date mode and session mode.

### 3.2.8 Command Line History and Command Line Editing

When you run a command at the GAUSS prompt, it is added to your command line history. The last 1,000 commands executed at the GAUSS command line are stored. The following keystrokes are supported for movement and editing at the command line and for retrieving the command line history:

Left Arrow Moves cursor left one character.
Right Arrow Moves cursor right one character.
home Moves cursor to beginning of line.

END

CTRL+Left Arrow

CTRL+Right Arrow

Up Arrow

Down Arrow
Search down through command history.

NOTE: Use CTRL+PAGE-UP or CTRL+PAGE-DOWN to scroll through your program output in the program input/output window.

### 3.2.9 Error Output Window

The Error Output Window shows errors messages from program runs or interactive commands and may be viewed from any page by clicking the Error Output button on the right side of the status bar. However, it will automatically open when an error occurs and will close and empty its contents on the next program run or interactive command.

The line number shown next to the error message is a clickable link (indicated by blue text), which will take you to the file and line containing the error.

```
Error Output
(5) G0121 : Matrix not positive definite [cicular.e, ine 32]
```

Figure 3.9: Error Output Window

### 3.3 Source Page

The Source Page is designed for creating and editing programs and procedures.

### 3.3.1 Source Page Menus

Section 3.2 ) and the Debug Menu, the Source Page contains the following additional menu options.

## File Menu

| Close | Closes the selected file. |
| :--- | :--- |
| Close All | Closes all open files. |
| Save | Saves the active file. |
| Save As | Saves the active file with a different file or path <br> name. |

## Window Menu

Split File Buffer Horizontally splits the active file into two views.
Horizontally

$$
\text { Split File Buffer } \quad \text { Vertically splits the active file into two views. }
$$ Vertically

Remove Buffer $\quad$ Removes a buffer split in the active file.
Split

Split Tab Stack Tiles any open programming editors horizontally. Horizontally
Split Tab Stack Tiles any open programming editors vertically.
Vertically

Remove Tab Split Removes any editor window tiling.
Go Back Takes you to your last cursor position, which could be in a different file.

Go Forward
After using Go Back, takes you to the next cursor position, which could be in a different file.

Previous Open Cycles backwards through the list of open tabs.
Document
Next Open
Cycles forward through the list of open tabs.
Document

### 3.3.2 Layout and Usage

The Source Page contains seven separate widgets: the Programming Editor, the Error Output Window, the Program Input/Output Window, the Projects List, the Bookmarks List, the Library Tool, and the Source Browser.


Figure 3.10: Source Page

## Programming Editor

Individual programming editors are opened in the editor docking area. The editor docking area allows tabbing of multiple open files, with the option to tile editors with a horizontal or vertical split. Select Window->Split Horizontally or Window->Split Vertically to tile open editor windows.

```
autoregmt.e \ autoregmt.gr \ \ cralace \\ 
    ** AUTOREG.E
    ** example autoregression on data generated by AUTOREG.SIM
    */
    library tamt;
    #include tamt.adf
    struct automtControl are;
    atruct automtOut aro;
    arc = automtControlCreate;
    lagvars = 0;
    order = 3;|I
    struct DS d0;
    d0 = reahape (d0, 2, 1);
    d0[1].dname = "autoregmt";
    d0[1].vnames = "Y";
    d0[2].vnames = "X1" $। "X2";
    output file = autoregmt.out reset;
    aro = autoregmt (are,d0,lagvars,order) ;
    output off;
```

Figure 3.11: Programming Editor

## Programming editor features:

1. Syntax highlighting:The GAUSS programming editor will provide syntax highlighting for GAUSS, C/C++, Java, Fortran, R and many other languages.
2. Autocompletion:Autocompletion is available in the GAUSS programming editor for GAUSS functions and for structure members of any structure in an active GAUSS library.

3
4 eq
eqIn
eqSolve
eqSolvemt

- eqSolvemtControlCreate
- eqSolvemtOutCreate
- eqSolveset

Figure 3.12: Autocomplete

Using autocomplete: if the characters you enter match items in the autocomplete list, a dropdown box will appear containing those functions. To navigate the dropdown list, press the down arrow or continue typing until only one selection remains. Once the desired command is highlighted, press the ENTER key to insert the remainder of the word.

The editor will provide autocomplete for the members of any structures that are in a GAUSS library if: the library is loaded, the file contains a statement to load the library, or the structure definition is in the current file.
3. Function Call Tooltips:After a GAUSS command and an opening parenthesis has been entered, a tooltip will appear with the argument list for the function.


Figure 3.13: Tooltips
4. Function Browser:Dropdown list lists all procedures defined in your file and lists their arguments. Select a procedure from the list to navigate to its definition.


Figure 3.14: Function Browser
5. Code folding: At the start of code blocks (e.g., procedure definitions, do and for loops, and if statements), the left margin of the programming editor will contain $\mathrm{a}+$. Clicking the + will hide the block of code from view and place a horizontal line across the editor indicating folded code and changing the + to $\mathrm{a}-$. Clicking on the - will reveal the hidden code

```
160 Øproc (1) = matpm(xth);
161 local pm,ixth;
162 ixth = rows (xth);
163 pm = zeros(ns,ns);
164\square if ipm== 1; // for ns = |2
165 田 if izz == 1;
168■ else;
169 pm[1,1] = xth[1,1];
```

Figure 3.15: Code folding of 'if' block
6. Autoindenting: The GAUSS programming editor provides automatic code indenting and deindenting. Autoindenting not only simplifies the process of writing code but also encourages the creation of readable code.
7. Variable highlighting:Click on a variable name and all instances of that variable will be highlighted.

```
160 \squareproc (1) = matpm(xth);
161 local pm,ixth;
162 ixth = rows (则th);
163 pm = zeros(ns,ns);
164 }\square if ipm == 1; // for ns =2 this option has para
165■ if izz== 1;
166 pm[1,1] = xth[1,1]^2/(1 +xth[1,1]^2);
167 F
    pm[2,2] = xth[2,1]^2/(1 + xth[2,1]^2);
```

Figure 3.16: Variable highlighting
8. Find usages: Right click on a variable or procedure and select 'Find Usages' from the context menu to create an organized clickable list of all usages in your file.


Figure 3.17: Find usages
9. Bookmarks:Bookmarks allow quick navigation to often visited lines of code. To insert a bookmark, hold down the SHIFT key and left click in the left margin of the file on the line where you would like to set the bookmark.

If a file contains more than one bookmark, you may use F2 to navigate to the next bookmark in the file. To navigate between bookmarks in multiple files, use the bookmark window. The bookmark window contains a list of all of your bookmarks.

Double-click on a listed bookmark and GAUSS will bring you to the file and line of your bookmark regardless of whether the file is already open for editing or not.
10. Source code formatting: The GAUSS editor will correctly format a source file with incorrect formatting. This is available from the context menu or with the hotProgramming Editor Hot Keys
CTRL+A Select All.
CTRL+CCopy.Debug current file.
CTRL+F Find and replace.
CTRL+G Go to line.
CTRL+I Formats the current file.
CTRL+LDelete line.
CTRL+NOpen new file.Open existing file.CTRL+PCTRL+ /CTRL+RCTRL+SCTRL+TCTRL+V

Print file.
Used for block commenting.
Run current file.
Save current file.
Switches current line with the line above.
Paste.
Closes the current file.

CTRL+Z

CTRL+Y

CTRL+~

CTRL+F1

F1

SHIFT+F1

ALT+Left-Arrow

ALT+Right-Arrow

Undo.
Redo.
Cycles through open editor windows.
Go to definition of function under cursor.
Go to Help Page for function under cursor.
Open inline help for function under cursor.
Go to previous cursor position, which may be in a previous file

After ALT+Left-Arrow, go to next cursor position.

### 3.3.3 Find and Replace

From the Edit Menu, selecting Find and Replace or pressing CTRL+F will bring up the find and replace widget at the bottom of your open programming editor. If a word is highlighted when you access find and replace, it will automatically be present in the find box when the find and replace widget is opened. Press the ENTER key or $>$ to search forward. Press the $<$ button to search backwards. To close the find and replace widget, press ESC or click the button on the left.


Figure 3.18: Find and Replace

The Replace Box has three buttons: > means replace the highlighted expression and search forwards, < means replace the highlighted expression and search backwards and replace means replace the highlighted text and do not change the cursor position.

## Regular Expressions

Find and Replace in GAUSS supports regular expression searching. Regular expression searching gives users tremendous power allowing quick and precise search and replace throughout an entire file. For example, let us start with a file containing the following commands:

```
r = 100;
c = 50;
x = rndn (r, c);
y = rndu (r,c);
z = x.*rndn (r, C);
```

Regular expressions allow you to perform very specific find and replace commands. Suppose that we want to find all usages of $r n d u$ and rndn and replace them with rndKMu.


Figure 3.19: Find and Replace Regular Expression

To open Find and Replace, we enter CTRL+F in out open text editor. In the Find and Replace widget, select the check box next to Regex to enable regular expression searching. One of the most simple regular expression options is to add a '.'.' The '.' means any character. So, if we search for "rnd." that will find any string that contains rnd
followed by any character, such as rnda, rndb, rndc, rndn, rndu, etc. Now enter "rndKMu" in the replace box and click Replace All. Now all instances of rndu and rndn should be replaced with rndKMu.

### 3.3.4 Changing Editor Properties

Programming editor preferences can be accessed by selecting: Tools->Preferences from the menu bar. From the Preferences window, select Source from the tree on the left. Here you can customize the programming editor's behavior.


The editor preferences has three main sections:

## General Settings

The general settings are located on the top left.

## Colors

This section is located along the bottom half of the preferences dialog window. Click one of the color buttons to change an element in the color scheme used in the editor.

## Autocomplete Settings

On the top right of the Source Preferences, under the heading "Autocompletion Source" , are the controls for autocompletion settings. This allows you to choose the contents of your dropdown autocomplete suggestions. The options are:

Provides autocomplete suggestions for GAUSS intrinsic functions.

Current Document

All Provides autocomplete suggestions for both above.
None Provides autocomplete suggestions only when CTRL+SPACE are pressed.

### 3.3.5 Error Output Window

The Error Output Window can be accessed by toggling the Error Output button on the right side of the status bar. For details regarding the features and usage of the Error Output Window, see Section 3.2.9.

## Error Output

(9) G0121 : Matrix not positive definte [crcular.e, ine 32]

Figure 3.21: Error Output Window

### 3.3.6 The Source Browser: Advanced Search and Replace

The Source Browser is a powerful search and replace tool that makes it much easier to work with your code--especially when completing larger projects. You may open the Source Browser by selecting View->Source Browser from the Source Page or entering the hot-key SHIFT+CTRL+F.


Figure 3.22: Source Browser
The Source Browser is made up of two main sections. The control tabs are on the left and on the results display on the right.

You can enter your search query in the Search tab, which allows you to specify a particular file pattern, filename, or directory to search. The button with three dots [...] to the
right of the directory dropdown menu is a browse button that will open a dialog window allowing you to browse for the desired directory.


Figure 3.23: Search and Replace
The Advanced tab allows you to refine your search criteria. Checking the References check box will limit your search to only locations where a variable is referenced. Alternatively, checking the Assignments box would limit your search to only those places where the variable was assigned to. For example, if you were searching for the variable 'nobs', this is an assignment:

```
nobs = 300;
```

whereas this is a reference:
myVar = nobs - 1;

| Search Advanced | Replace |
| :---: | :---: |
| Match Case: <br> Whole Word: $\square$ <br> RegEx: $\square$ <br> Max File Size (MB): 500 <br> Search Subdirs: $\square$ <br> Ignore Binaries: $\square$ | Occurrences References Assignments |

Figure 3.24: Advanced Search and Replace

You may also select to limit your search to whole words, match case or use regular expressions. This tab also allows you to control whether your search extends to subdirectories and if you would like to exclude files larger than a certain size. It is recommended that you always select Ignore Binaries.

## Executing a search

Once you have a search string in the Find box and have your desired parameters set, press the 'search' button to execute your search. In the results display window, you will see a list of files that contain matches to your search. To the left of each file in the list you will see a check box which can be used to include or exclude the matches in a file from any Replace actions. To the right of the file name you will see a number in parentheses which indicates how many matches were found in the file.


Figure 3.25: Executing a search
Expand the node of a file to examine its list of matches, or right-click and select 'Expand All' from the context menu. Once you expand the node for a file, you will see the line number of the match followed by a colon and then the line of code with the match highlighted in yellow. Double-click on a line to edit that file.

## Executing a replace

After you have completed your search and unchecked any matches that you do not want replaced, click the Replace tab. Enter your replacement term and press the Replace button. GAUSS will warn you that any changes in unsaved files cannot be undone. If you are certain of your replacement, click OK.

If you are making a change across a large number of files, particularly if you are not using a version control system like Subversion or Git, it is a good idea to select the 'Backup Original' check box. With this selected, before GAUSS makes the replacements to your file it will save a copy of the original with a . bak extension. For example if your original file was myfile.gss, the backup file will be called myfile.gss.bak.

If you select the 'Overwrite Backup' checkbox, the next time that you make a change to this file, the file myfile.gss.bak will be overwritten. If you do NOT check the 'Overwrite Backup' check box, GAUSS will make incremented backup files: myfile.gss.bak(1), myfile.gss.bak(2), etc.

### 3.3.7 Project Organizer: Keeping track of files with the Project Window

The Project Window displays the contents of any folder you choose as well as its subfolders. To add a folder to the Project Window, either right-click in the Project Window and select "Add Folder" from the bottom of the context menu or click the "Open Folder" toolbar button.


Figure 3.26: Open Project Folder

By default, all files in the folder will be shown. If you would like the Project Window to display only certain file types, you can enable file filtering by right-clicking in the Project Window and selecting "Filter GAUSS Files."


Figure 3.27: Filter File List

With "Filter GAUSS Files" enabled, the Project Window will display only files that match the list of file extensions found under "Tools->Preferences->Source->Project View Filter: Files to Show". This is a comma-separated list of file extensions, which may be modified by the user.

## Interacting with files in "Project Window"

Double-click on a file name to open it or right click to bring up a context menu that will allow you to perform other actions, such as: "open", "run", "delete" and "rename".

## Searching for text through all files in a directory

Right-clicking on a directory in the Project Window and selecting "Find in folder" will open up the "Source Browser" an advanced find-and-replace window. The "Directory" field will be pre-populated with the directory you selected.


By default the "File Pattern" field will contain "*.*". This means GAUSS will search in all files in the specified directory that have any type of file extension. If you would like to include in your search files that do not have file extensions, change the "File Pattern" field to just "*". Finally, add the text you wish to search for to the "Find" field and click the "search" button.

Source Browser


Figure 3.29: "Find in Folder" opens the Source Browser

## Searching for a file by name

When working with large numbers of files over multiple directories, it can be difficult to search through a growing list of tabs. The GAUSS Project View Window allows you to almost instantly locate any file that is in one of the folders you have open or in your GAUSS SRC_PATH. To search for a file, click in the text edit box at the bottom of the Project Window, or use the $\mathrm{Ctrl}+\mathrm{K}$ shortcut. As you begin to enter the filename, an autocomplete list of matching files will appear. The up and down arrow keys will navigate the autocomplete list. Press ENTER to open the file.


Figure 3.30: Find File

### 3.4 Data Page

The Data Page provides a tree view of all of the active symbols in your GAUSS workspace organized by data type. Double-click one of your active symbols to open the data in a Symbol Editor. Symbol Editors provide a spreadsheet like view of your data.


Figure 3.31: Symbol Editor

### 3.4.1 Changing values

You may change the value of a single cell in a symbol editor by double-clicking in the cell and entering the new value. Note that hitting enter or clicking outside the cell will save your change. To revert an in-process change before it is saved, hit the escape key.


Figure 3.32: Change Cell Value

### 3.4.2 Changing formatting

Change the formatting of the numbers in a symbol editor by clicking the "Format" button and then, selecting a format type and then selecting the precision.


Figure 3.33: Change Number Format

The "Compact" format will choose either "Scientific" or "Decimal", whichever creates the most compact representation of the data.

If none of the cells are selected, the formatting will be applied to all cells. If you select a cell, column or row before you choose the format style, it will only be applied to the selected data. This allows you to apply different formatting to each of your variables if you desire.

### 3.4.3 Navigating multi-dimensional arrays

At the top-right of an array symbol editor you will find a listing of the all the dimensions in the array. All but the final two dimensions will be list widgets. Click them to select a particular dimension to view.


Figure 3.34: Select Dimension to View

On the left of the array dimensions is a button with a leftward facing chevron. Clicking this button will navigate towards the start of the array. The corresponding button on the right of the array dimensions will navigate towards the end of the array.

### 3.4.4 Viewing structure members

Double-click on a structure member in the Active Symbol Tree to open it in a symbol editor.

### 3.4.5 Creating a floating watch window

You may undock the symbol editors from the "Data Page" and place them anywhere on your screen by clicking the "Toggle dock" button which looks like an arrow to the left of the "Format" button. They will be updated every time that a program ends or a com-mand-line statement is executed, which can make this a good way to keep track of your data.

### 3.5 Debug Page

### 3.5.1 Menus and Toolbars



Figure 3.35: Debug Toolbar

| Go | Runs the program to the next breakpoint. |
| :--- | :--- |
| Toggle Breakpoint | Sets/Clears a breakpoint at the cursor. |
| Clear Breakpoints | Clears all breakpoints in a file. |
| Examine Variable | Opens a watch variable in a symbol editor. <br> Runs the next executable line of code in the <br> application and steps into procedures. |
| Step Into | Runs the next executable line of code, but does not <br> step into procedures. |
| Step Over | Runs the remainder of the current procedure and <br> stops at the next line in the calling procedure. |
| Step Out | Runs the program until it reaches the cursor position. |
| Run to Cursor | Terminates a debugging session. |

## Components and Usage

The Debug Page is composed of five main widgets:
Breakpoint List An interactive list of all breakpoints.
Call Stack Window
An interactive display of the chain of procedure calls.

Local Variable
Window
An interactive display of all variables that are in

Variable Dump
Window
Watch Window An interactive display of user specified variables.

The Debug Window indicates which line it is on by the >>> located in the left margin. This is also the location where breakpoints are added. To add a breakpoint, click in the left margin of the Debug Window on the line you wish to add the breakpoint. Clicking an active breakpoint will remove it.


Figure 3.36: Debug Window

## Starting and Stopping the Debugger

You can start debugging of a file you are in by pressing CTRL+D. Click the Debug button to debug the file in the top of the Action List. Placing your mouse over the Debug but-
ton will reveal a tooltip with the name of this file, or click the downward pointing triangle next to the debug button and select a file from the list.


Figure 3.37: Debug Button

When the debugger is started, it will highlight the first line of code to be run. Any breakpoints are shown in the left margin of the window. You can stop debugging at any time by clicking the Stop button on the debug toolbar.

### 3.5.2 Using Breakpoints

Breakpoints stop code execution where you have inserted them. Breakpoints are normally set prior to running the debugger, but can also be set or cleared during debugging by clicking the Set/Clear Breakpoint option on the Debug menu.

## Setting and Clearing Breakpoints

To set breakpoints in any part of the file not currently being executed, just click in the left margin of the line on which you would like the breakpoint. Alternatively, you can highlight a line then click Toggle Breakpoint.


Figure 3.38: Setting Breakpoints

To clear a breakpoint in the file, click on the breakpoint you would like to remove or click a line of code that has a breakpoint set and then click Set/Clear Breakpoint. You can clear all breakpoints from the active file by clicking Clear All Breakpoints.

### 3.5.3 Stepping Through a Program

GAUSS's debugger includes the ability to step into, step out of, and step over code during debugging.

Use Step Into to execute the line of code currently highlighted by the debugger.


Figure 3.39: Step In (F8)

Use Step Out to execute to the end of the current function without pause and return to the calling function.


Figure 3.40: Step Out (F10)

Use Step Over to execute the line of code currently highlighted by the debugger without entering the functions that are called.


Figure 3.41: Step Over (F9)

Use Stop to stop the debugger.


Figure 3.42: Stop

### 3.5.4 Viewing Variables

GAUSS allows you several ways to view the values of variables during debugging.

## Hover Tool-tip View

Once the debugger is started, hovering your mouse over a variable name will open tooltip with a preview of the values in the variable.


Figure 3.43: Hover Tool-tip

These tooltip views are only intended to give a quick view of the data, so they may not show all data held by the variable. If you need to view more data, you may either click on the variable name in the file and type CTRL+E, click the Examine Variable toolbar
button and enter the variable name, or double-click the variable in the Local/Watch Window to view the variable in a floating symbol editor.


Figure 3.44: Watch Window

## Setting a Watch Variable

The Watch Window list is directly below the the Local Variable list. It displays the same information about the variables in its list as does the Local Variable list. By default this list starts empty. You may add variables to the list by either right-clicking over the name of a variable in the Local Variable list and selecting "Add to watch" from the context menu, or by right-clicking directly in the Watch Window and selecting "Add new".

The debugger searches for a watch variable using the following order:

1. A local variable within a currently active procedure.
2. A global variable.

### 3.6 Help Page

The Help Page gives you access to the entire GAUSS help system in HTML format. The table of contents tree is on the left. Click the + symbol to expand a particular section of the contents and double-click on the title to view the page. As on the other pages, the Program Input/Output Window and the Error Window are available via toggle buttons on the status bar. It can be helpful to enter an interactive command and/or view error output while simultaneously viewing the relevant documentation.


Figure 3.45: Help Page

## Hot Keys

| F1 | Opens the Command Reference section for the <br> highlighted command. |
| :--- | :--- |
| CTRL+F1 | Opens a programming editor with the function <br> definition of a highlighted procedure. |
| SHIFT+F1 | Opens a floating Help Window for the highlighted <br> command. |

## 4 Hot Keys and Shortcuts

### 4.1 Action Hot Keys

| F2 | Navigates to the next bookmark in the Active File. |
| :--- | :--- |
| F3 | Find again. |
| F5 | Runs highlighted text. |
| F6 | Run file at top of Action List. |
| Debug file at top of Action List. Inside a debug |  |
| F7 | session, F6 will cause the debugger to run to the <br> next breakpoint, or the end of the file if no <br> breakpoints are encountered. |
| F8 | Edit file at top of Action List. |
| F9 | Step in (during a debug session). <br> F10 |
| Step over (during a debug session). |  |
| CTRL+D | Step out (during a debug session). |
| CTRL+R | Debug the Active File. |

### 4.2 Navigation Hot Keys

GAUSS automatically navigates between pages when you perform certain actions. For example, if you are editing a file in the Source Page and type CTRL+D to debug that file, GAUSS will automatically take you to the Debug Page.

However, there are also several hot keys that allow you to navigate quickly and easily between pages without performing any actions:

CTRL+1 Brings up the Command Page.
ctrli $2 \quad$ Brings up the Source Page.
CTRL+3 Brings up the Data Page.
CTRL $+4 \quad$ Brings up the Debug Page.
CTRL+5 Brings up the Help Page.

Mouse Scroll
Wheel

Brings up the next page. For example, CTRL+TAB from the Command Page will bring up the Source Page. CTRL+TAB from the Help Page will wrap and bring up the Command Page.

Cycles between any pages that are undocked as well as other open programs.

Windows only: Cycles between any pages that are undocked as well as other open programs.

When floating over any set of tabs, the mouse scroll wheel will cycle through the open tabs. This will work for programming editor tabs, symbol editor tabs, and the main page tabs on the left of the main application.

### 4.3 Focus Program Output on I/O

Under the Tools->Preferences->Command is a check box entitled Focus Program
Output on I/O. Selecting this option will open up a Program Output Window if any program output is printed or if any input is requested by the GAUSS commands key, keyw, or cons.

### 4.4 F1 Help

If your cursor is on the name of a GAUSS command in an editor, you can press F1 and it will take you to the Command Reference listing for that command. Inside the Help system, highlight command names by double-clicking on them to enable F1 help navigation.

## Shift+F1 Inline Help

Typing SHIFT+F1 when your cursor is on a GAUSS command will open an inline help window that floats above your editor window.


Figure 4.1: Inline help window opened with SHIFT+F1

### 4.5 CTRL+F1 Source Browsing

If your cursor is on the name of a procedure or global variable that resides in an active GAUSS Library (. lcg file), typing CTRL+F1 will open the source file in a Programming Editor.

To learn more about creating a User Library for your procedures, see Libraries, Chapter 19.

## 5 Using the GAUSS Debugger

The GAUSS debugger is a powerful tool to speed up and simplify your program development. Debugging takes place on the Debug Page, which is a full-featured dashboard providing you a wealth of information about the status of your variables and your program every step of the way.


Figure 5.1: The debug button automatically opens the Debug Page

### 5.1 Starting the Debugger

Figure 5.2: Debug Button

You may start a debug session by selecting the Action List Debug button, by entering CTRL+D from the file that you would like to debug, or by entering debug filename from the command line. GAUSS will bring the Debug Page to the front, and the debug session will begin with the first line of code highlighted, waiting to be run.


Figure 5.3: Debug Window
From here you can step through your program line-by-line, or run to a line of interest. To tell the debugger to run to a particular line, you must first set a breakpoint. Setting a breakpoint on a line in your program tells the debugger to pause when it gets to that line. You may set a breakpoint in any source file by simply clicking in the margin to the left of the line numbers. You will see a red dot appear in the margin, and a new entry will be added to the breakpoint window, which can be viewed on both the Source and Debug Pages. New breakpoints can be added before or during a debug session.

The Debug Page toolbar gives you the controls you need to navigate during debugging. Hover over any of the buttons to get a tooltip with a description of the button's function and its corresponding hot key.


Figure 5.4: Debug Toolbar

| Debug Run | Runs to the next breakpoint. |
| :--- | :--- |
| Debug Stop | Stops the debug session. <br> Toggle Breakpoint <br> Clear Breakpoints |
| Toggles a breakpoint on the current line. |  |
| Examine Variable | Removes all breakpoints from all files. <br> Opens a user-specified variable in a floating Symbol <br> Editor window. |
| Step in | Steps to the next line. If the next line is a procedure, it <br> will step inside this procedure. |
| Step over | Steps to the next line without stepping into other <br> procedures. |
| Step out | Runs through the end of the current procedure and <br> stops in the calling file. |
| Run to cursor | Runs to the location of your cursor as if it were a <br> breakpoint. |

### 5.2 Examining Variables

When the debugger is paused at a line in your program, you may view any of the variables in your GAUSS workspace. GAUSS offers several options for this. The first is through the Local Variable window. This window contains an alphabetical list of every variable that is currently in scope. It also lists the first value of each variable, its type (matrix, string, structure, etc.) and dimensions. The contents of this window are immediately updated each time you step to a new line of your program.

| Local/Watch Variables |  |  | $\times$ |
| :---: | :---: | :---: | :---: |
| Name ^ | Type | Value | * |
| Lgradproc[1x1] | Matrix | 0.000000 |  |
| Lmaxiters[1x1] | Matrix | 100000.000000 |  |
| Lprintiters[1x1] | Matrix | 0.000000 |  |
| Lrelgradtol[1x1] | ] Matrix | 0.000010 | = |
| Lrteps[1x1] | Matrix | 0.010000 |  |
| dx[1x1] | Matrix | 0.000000 |  |
| fnct[1x] | Matrix | 840.000000 |  |
| maxtry[1x1] | Matrix | 100.000000 |  |
| $n p[1 \times 1]$ | Matrix | 4.000000 |  |
| sp2[1×2] | Matrix | 0.000000 |  |
| $\mathrm{vv}[2 \mathrm{x} 2$ ] | Matrix | 1.000000 | - |
| Name | Type | Value |  |
| $\times 0[4 \times 1]$ | Matrix | 5.000000 |  |
| zz[2x1] | Matrix | 0.000000 |  |

Figure 5.5: Local Variable Window
Double-clicking on a variable in the Local Variable window opens that variable in a floating symbol editor. This symbol editor window looks much like a spreadsheet and will display the entire contents of the variable.

Located just below the Local Variable window is the Watch window. The Watch window looks and acts much the same as the Local Variable window, but it holds only variables that you specifically add to it. This allows you to place variables of interest in a smaller list that is easier to scan. You can add a variable to the Watch window by either right-clicking on a variable in the Locals list and selecting "Add to watchlist", by rightclicking in the Watch window and selecting "Add new", or by highlighting a variable in the file and then dragging and dropping it into the watch window.

| x - matrix (100x2)(auto)(sync) |  |  | $\times$ |
| :---: | :---: | :---: | :---: |
| Symbols Preferences |  |  |  |
| Dec Sci Hex Chr |  |  |  |
|  | 1 | 2 | - |
| 1 | -1.03359 | 1.50304 | E |
| 2 | -1.27639 | 0.149639 |  |
| 3 | $-0.974079$ | $-0.831634$ |  |
| 4 | -1.12487 | -1.12698 |  |
| 5 | $-0.761334$ | -2.2615 |  |
| 6 | -0.381396 | 1.70782 |  |
| 7 | $-1.31341$ | $-0.714726$ |  |
| 8 | $-0.474867$ | $-0.848527$ |  |
| 9 | -1.75034 | 0.163373 |  |
| 10 | 0.800256 | $-0.646054$ | - |

Figure 5.6: Symbol Editor Window
You may see a tooltip preview of any variable in your file by floating your cursor over the variable name. Placing your cursor on a variable and pressing CTRL-E will open that variable in a floating symbol editor.

### 5.3 The Call Stack Window

The Call Stack window is like a map into your program. The top entry in the Call Stack window is always your current location. It lists the name of the procedure you are in, the arguments that this procedure takes, the name of the file it is in, and the line number you are on. The next item in the list displays the same information for the location from which your current procedure was called. The item after that displays the location from which that procedure was called and so on.

```
Call Stack
    (1) = lpr(b) [circular.e: 47]
    (5) = _bfgs(fnct, x0, Lmaxiters, Lrelgradtol, Lgradproc, Lprintiters, Lrteps) [qnewton.src: 178]
    (4) = QNewton(fnct, x0) [qnewton.src: 98]
    (0) = main0 [circular.e: 30]
```

Figure 5.7: Call Stack Window
This list is interactive. Single-clicking on any of the items in the Call Stack window will bring you to that particular line and file. For example, if you would like to examine the line from which your current procedure was called, click on the second item in the call stack list. Not only will this open that line and file in your Debug window, but it will also update the Local Variable window to display all the variables that exist at that location, as well as their current values. To return to your current location, click the top line in the Call Stack window.

### 5.4 Ending Your Debug Session

If you would like to terminate a debug session before the debugger has run through the entire program, click the Debug Stop button, located at the top left of the Debug Page.


Figure 5.8: Debug stop button

## 6 GAUSS Graphics

### 6.1 Overview

The plotting functionality available in GAUSS is designed to provide intuitive methods for visualizing data using a variety of plot types. The main plot drawing functions are:

| plotArea | Creates a cumulative area plot. |
| :--- | :--- |
| plotBar | Creates a bar plot. |
| plotBox | Creates a box plot using the box graph percentile <br> method. |
| plotContour | Creates a contour plot. |
| plotHist | Calculates and creates a frequency histogram plot. |
| plotHistF | Creates a histogram plot from a vector of frequencies. |
| plotHistP | Calculates and creates a percentage frequency <br> histogram plot. |
| plotLogLog | Creates a 2-dimensional line plot with logarithmic <br> scaling of the both the x and y axes. |
| plotLogX | Creates a 2-dimensional line plot with logarithmic <br> scaling of the x-axis. |
| plotLogY | Creates a 2-dimensional line plot with logarithmic <br> scaling of the y-axis. |


| plotPolar | Creates a polar plot. |
| :--- | :--- |
| plotScatter | Creates a 2-dimensional scatter plot. |
| plotSurface | Creates a 3-dimensional surface plot. |
| plotTS | Creates a graph of time series data. |
| plotXY | Creates a 2-dimensional line plot. |

### 6.2 Basic Plotting

The simplest way to plot data in GAUSS is to use default values for the plot settings, such as line color, line size, legend text, etc. These settings may be changed by the user from the main menu bar: Tools-> Preferences-> Graphics. To create a plot using default plot settings, simply call one of the plotting functions with your data as inputs:

```
//Create a sequential column vector from
//-5 to 5 with 101 steps
x = seqa(-5, 0.1, 101);
//Set y to the normal probability density function
y = pdfn(x);
//Plot the data
plotXY(x, y);
```



Figure 6.1: One-Curve Plot

### 6.2.1 Plotting multiple curves

Each column of the input matrices is treated as a separate curve or line on the graph. Below is an example that uses the variables created from the example above and adds an additional line:

```
x = seqa(-5, 0.1, 101);
y1 = pdfn(x);
//Set y2 to the Cauchy probability density function
y2 = pdfCauchy(x, 1, 1);
```

```
//Plot the data using the ~ operator to horizontally
//concatenate y1 and y2
//Note that y1 and y2 will be plotted against the same
//x values
plotXY(x, y1~y2);
```



Figure 6.2: Two-Curve Plot

### 6.3 Plot Customization

GAUSS offers two ways to customize your graphs. The first is through the graphics preferences dialog window. The second method for plot customization is using a plotControl structure.

### 6.3.1 Using the Graphics Preferences Settings Window

## Main Graph Settings

The default settings for graphics can be opened by selecting Tools->Preferences from the main application menu bar. Then select Graphics from the list on the left of the preferences window.


Figure 6.3: The Graph Settings Tab

## Selecting a graph type

Each type of graph in GAUSS has its own settings. Click on the graph type list widget to expand the list of graph types. Click on one of the listed graph types to view its settings.
Command
Source
Data

Graphics
General
New graphs: (o) Reuse same


Figure 6.4: The Group Tab

Once you have selected a graph type, browse through the settings by clicking on a an individual graph component, such as the "Legend", "Axis Style" or "Axis Text". "Series 1 ", "Series 2", etc contain the preferences for the curves such as "line color", "line thickness", "symbol type", etc.


Figure 6.5: Scatter plot graph settings
After you have made your desired changes, Click the 'Apply' and 'OK' buttons. GAUSS will use these preferences for all future graphs that are made without passing in a plotControl structure. As we will see in the next section, these settings will also be the starting point when you create a plotControl structure. These settings may be changed at any time.

## Contour/Surface Plot Z-Level Color Settings



Surface/Contour Level Color Settings
If you select the 'Surface' graph type, you will see a 'Colors' option instead of 'Series 1 , Series $2 \ldots$...' as shown above. The "Colors" control allows you to add and subtract default z-level colors and to also change their order.

## Available Actions

| Add a new color | Click the add $(+)$ button |
| :--- | :--- |
| Edit a color | Double-click the color |
| Select a color | Single-click the color |
| Delete a color | Select a color and click the minus (-) button <br> Change color order |
| Click-and-drag color to desired position, or select a <br> color and click the up or down button |  |

### 6.4 PlotControl Structures

The GAUSSplotControl structure provides a powerful and flexible method for programmatic control of your graphs in GAUSS. This structure is a convenient package that stores all of the information about how you would like a specific graph to be displayed. These structures may be saved to disk and reloaded during a future session or passed on to colleagues. Using a plotControl structure requires just two easy steps:

1. Declare the structure.
2. Initialize the structure.

Once these steps are completed, you may change any of the plot settings in the structure. Once the plotControl structure is set how you would like, you can pass it in as the first argument to any of the GAUSS plot-creating functions. Below is an example that draws a graph using a plotControl structure set to default values:

```
//Declare the structure
struct plotControl myPlot;
//Initialize the structure
myplot = plotGetDefaults("xy");
//Create a column vector from -3 to 3 with a step size of 0.1
x = seqa (-3, 0.1, 60);
y = sin(x);
//Plot the data using the plotControl structure
plotXY(myPlot, x, y);
```

The available plotControl setting functions include:
plotGetDefaults
plotSetBar

Applies the user defined default settings for a specified graph type to a plotControl structure.

Sets the fill style and format of bars in a histogram or bar graph.
plotSetBkdColor
plotSetFill
plotSetGrid
plotSetLegend
plotSetLineColor
plotSetLineStyle
plotSetLineSymbol
plotSetLineThickness
plotSetNewWindow
plotSetTitle
plotSetWhichYAxis
plotSetXLabel
plotSetXRange
plotSetXTicCount

Sets background color of a graph.
Sets the fill style, opacity and color for area and bar plots as well as histograms.

Controls the settings for the background grid of a plot.

Adds a legend to a graph and optionally applies settings.

Sets line colors for a graph.
Sets line styles for a graph.
Sets line symbols displayed on the plotted points of a graph.

Sets line thickness for a graph.
Sets whether new graphs should be drawn in the same window or in a newly created window.

Controls the settings for the title for a graph.

Controls whether a particular curve uses the right or left Y-axis.

Controls the settings for the X -axis label on a graph.

Controls the minimum and maximum values of the X -axis.

Sets the number of major tics along the

| plotSetXTicInterval | X-axis. <br> Controls the interval between X-axis tic <br> labels and optionally at which X-value to <br> place the first tic label. |
| :--- | :--- |
| plotSetXTicLabel | Controls the formatting and angle of X- <br> axis tic labels for 2-D graphs. |
| plotSetYLabel | Controls the settings for the Y-axis label <br> on a graph. |
| plotSetYRange | Controls the minimum and maximum <br> values of the Y-axis. |
| plotSetYTicCount | Sets the number of major tics along the <br> Y-axis. |
| plotSetZLabel | Controls the settings for the Z-axis label <br> on a graph. |

Most of these functions begin with plotSet. This has two main advantages. First, you may quickly and easily survey the plotSet options by typing plotSet in a GAUSS editor and scrolling through the auto-complete list without needing to consult the documentation. Second, this convention makes your GAUSS code easy to read and understand.

## Example

```
//Declare plotControl structure
struct plotControl myPlot;
//Initialize the structure with the "bar" default values from
//the main application menu Tools->Preferences->Graphics
myPlot = plotGetDefaults("bar");
//Create data to plot
```

```
x = seqa(1, 1, 10);
y = abs(rndn( 10, 1 ));
//Change plot settings
//Turn off the grid
plotSetGrid(&myPlot, "off");
// Set x-axis label
plotSetXLabel(&myPlot, "Day of Project");
//Set the title, title font and font size
plotSetTitle(&myPlot, "Example Bar Plot", "arial", 18);
//Draw graph
plotBar(myPlot, x, y);
```



Figure 6.6: Example Bar Plot

Notice in the previous example that the first input to the plotSetTitle function is \&myPlot and not just the variable name, myPlot. This is because all of the plotControl setting functions take a structure pointer as the first input. The ampersand (\&) in front of the variable name makes the input argument a pointer to that structure.

Passing structure pointers as arguments is much faster and more efficient than passing an entire structure. The rule for remembering when to use a plotControl structure pointer instead of plotControl structure is simple. If the function you are calling sets a value in the structure, you need to use a structure pointer. In all other cases, use the structure.

Fortunately the function completion tooltip in the GAUSS editor will indicate which is required, in case you forget this simple rule. For more information on structures and structure pointers see Structures, Chapter 16.

### 6.5 Adding Data to Existing Plots

You may add additional data to 2-D plots. This functionality is accessed through the following:

| plotAddArea | Adds a cumulative area plot an existing 2-D <br> graph. |
| :--- | :--- |
| plotAddBar | Adds a set of bars to an existing 2-D graph. |
| plotAddBox | Adds a box plot to an existing 2-D graph. |
| plotAddHist | Adds a histogram to an existing 2-D graph. |
| plotAddHistF | Adds a frequency histogram to an existing 2- <br> D graph. |
| plotAddHistP | Adds a percentage histogram to an existing <br> 2-D graph. |
| plotAddPolar | Adds a polar plot to an existing polar graph. |

plotAddScatter
plotAddTS

## plotAddXY

Adds a scatter plot to an existing 2-D graph.
Adds a time series plot to an existing time series graph.

Adds an XY line to an existing 2-D graph.

Any 2-D plot type may be added to any other 2-D plot type, with the exception of contour plots, polar plots and time series plots. You may add a polar plot to a previous polar plot or a time series plot to a time series plot. Use the plotAdd functions only to add data to an existing graph. Do not attempt to use them to create a new graph.

## Example

```
//Create and plot multivariate random normal data
rndseed 19823434;
Cov = { 1 0.9, 0.9 1 };
mu = { 2, 2 };
y = rndMVn(300, mu, cov);
plotScatter(y[.,1], y[.,2]);
//Create line coordinates and add to scatter plot
x = {-0.3, 4.8};
y2 = { 0, 4.3 };
plotAddXY(x, y2);
```



Figure 6.7: Example Adding Data to a Plot

### 6.5.1 Styling and the plotAdd functions

## Plot-wide attributes

The plotAdd functions will not make any styling changes to the existing plot-wide attributes, such as the title, axes labels, grid, etc. It will, however, increase the scale of the view if needed to accommodate the new curve.

## Curve level attributes

If the plotAdd call does not use a plotControl structure, attributes for the added curves such as line or fill color, symbol style and the curve's legend text will be controlled by the preferences settings. The new curve will be treated as an additional series in sequence with any curves that already exist on the plot. For example if you draw a scatter plot with one column of data and then add another column of data with plotAddScatter and do not pass in a plotControl structure, the second set of scatter points will use the scatter settings from "Tools->Preferences->Graphics->Scatter->Series 2".

```
//Use scatter "Series 1" settings
plotScatter(x_1, x_2);
//Use scatter "Series 2" settings
plotAddScatter(x_3, x_4);
```

If you pass in a plotControl structure to the plotAdd call, GAUSS will apply the first series curve settings in the plotControl structure to the first series of data that is added. For example:

```
struct plotControl myPlot;
myPlot = plotGetDefaults ("scatter");
//Use the Series 1 line color settings
//set in 'myPlot' by 'plotGetDefaults'
plotScatter(myPlot, x_1, x_2);
plotSetLineColor (myPlot, "purple" $| "blue");
//Use the Series 1 line color settings
//in the plotControl structure, purple
//for x_3 vS x4, use blue for x_3 vS x_5
plotAddScatter(myPlot, x_3, x_4~x5);
```

The above code first creates a scatter plot of $x_{-} 1$ vs. $x_{-} 2$. It then changes the line color settings inside the plotControl structure to purple for the first set of scatter points and blue for the second set of scatter points. Finally, it adds the scatter series $x$ _ 3 vs. $x \_4$ which will be drawn in purple and $x \_3$ vs. $x \_5$ which will be drawn in blue.

### 6.6 Creating Subplots

GAUSS allows you to create two types of graphs within graphs. The first is called a subplot. In GAUSS a subplot divides the canvas up into tiles of equal size and shape.

This functionality is controlled with the plotLayout function. The plotLayout function splits the canvas up into a specified number of rows and columns and also specifies into which cell to draw the next graph.

```
//Divide the canvas into 2 rows and 3 columns
and
//set the next drawn graph to be placed into the
//last position (which is the sixth cell);
//plotLayouts use row major ordering
plotLayout(2, 3, 6);
```

| 1 | 2 | 3 |
| :--- | :--- | :--- |
| 4 | 5 | 6 |

Figure 6.8: plotLayouts use row major ordering
After calling plotLayout, all future graphs will be placed in the cell location specified by the plotLayout call until plotLayout is called again with new parameters or a call to plotClearLayout is made. A call to plotClearLayout will cause the next graph to be drawn to take up the entire canvas.

This next graph, after a call to plotClearLayout, will either draw over any existing graphs or be drawn in a new window depending on your graphics preferences. This setting can be controlled from the "New graphs" setting, located under Tools-> Prefer-ences-> Graphics. It may also be set with the plotSetNewWindow function.

## Example

```
//Divide the canvas into 2 rows and 2 columns
and
//place each successive graph in the next
//available cell
for i( 1, 4, 1);
    plotLayout(2, 2, i);
        //Plot a percentage histogram with 10*i bins
    of
        //random normal data
        plotHistP(rndn(1e5, 1 ), 10*i);
    endfor;
    //Clear the layout so future graphs are not
    drawn in
    //this layout
plotClearLayout();
```



Figure 6.9: Example Subplot

### 6.6.1 Creating Mixed Layouts

In GAUSS, plotLayouts may not overlap. For this functionality use the plotCustomLayout function. However, you may divide the canvas into sections of different size as long as they do not overlap.

## Example

```
//Divide the canvas into a 2x2 grid and fill in the first row
plotLayout(2, 2, 1);
plotHistP(rndn(1e5,1), 20);
plotLayout(2, 2, 2);
plotHistP(rndn(1e5, 1), 40);
//Divide the canvas into a 2x1 grid and fill in the
//bottom half, leaving the top section alone
plotLayout(2, 1, 2);
plotHistP(rndu(1e5, 1 ), 80);
```



Figure 6.10: Example Mixed Layout

### 6.6.2 Creating Custom Regions

Custom regions in GAUSS are graphs inside of graphs. They may be placed in any location on the canvas and may be any size. This functionality is controlled by the plotCustomLayout function. It takes the location and size parameters for the custom region as a percentage of the entire canvas. As with plotLayout, these settings will be applied to the next drawn graph.

```
//Draw a custom region that starts 25% of the
//distance from the left edge of the canvas, 10%
//from the bottom of the canvas with a width of 40%
//of the canvas and a height of 28% of the canvas
plotCustomLayout(0.25, 0.1, 0.4, 0.28);
```

Unlike with plotLayout, these custom regions will not delete any graphs below them and can thus be used to place a small graph over a portion of a larger graph.

## Example

```
//Draw a full size graph
rndseed 908734;
y = rndn(1e5, 1);
plotHistP(y, 30);
//Draw a custom region, close-up over the bottom left
// of the previously created graph
plotCustomLayout(0.1, 0.3, 0.2, 0.4);
//Set up plotControl struct with simple view
struct plotControl myPlot;
myPlot = plotGetDefaults("box");
plotSetLegend(&myPlot, "off");
plotSetGrid(&myPlot, "off");
plotSetXAxisShow(&myPlot, 0);
plotSetYAxisShow(&myPlot, 0);
//Create plot in custom region defined above
plotBox(myPlot, 0, y);
//Clear the layout, so future graphs will not be
//drawn in this custom region
plotClearLayout();
```



Figure 6.11: Example Custom Layout

### 6.7 Time Series Plots in GAUSS

GAUSS provides the following functions to simplify the process of creating time series graphics:
plotAddTS Adds a time series curve to a previously draw time series graph.
plotTS
plotSetXTicLabel
plotSetXTicInterval

Creates a graph of time series data.
Controls the formatting and angle of X -axis tic labels for 2-D time series graphs.

Controls the interval between X-axis tic labels and also allows the user to specify the first tic to be labeled for 2-D time series graphs.

To create a basic time series plot in GAUSS, you will use the plotTS function. In addition to the $y$ data to plot, this function requires the following inputs:

| dstart | Scalar, the starting date of the time series in DT <br> scalar format. |
| :--- | :--- |
| frequency | Scalar, the frequency of the data per year. Valid <br> options include: |

12 Monthly
12 Monthly
4 Quarterly
4 Quarterly
1 Yearly data
1 Yearly data

## Example

```
    //Data to plot
    y = rndu(24, 1);
    //Start the series in January of 1987
    dstart = 1987;
    //Specify the data as monthly
    freq = 12;
    //Plot the data
plotTS(dstart, freq, y);
```

The example program above will create a graph of monthly data from January of 1987 through December of 1988. It should look similar to the graph below:


Figure 6.12: Close-up of monthly data plot

## Understanding the dstart parameter

The dstart parameter is specified to be a scalar value in DT scalar format. In DT scalar format the leading four digits are the year and the next two digits, if present, represent the month. If the month information is not present, as in the example above, GAUSS will assume the first month of the year. This means that this:

```
2 0 0 8
```

and this:

```
200801
```

will both be treated as specifying January of 2008.
To specify a starting quarter in DT scalar format, set the final digits of your dstart to be the first month of the quarter. The following represent 2008 Q1, 2008 Q2, 2008 Q3 and 2008 Q4 respectively.

```
200801
```

200804

```
200807
200810
```


### 6.7.1 Quarterly Example

Using what we have just learned, we will create a quarterly graph that starts at 2007 Q4 and runs for 16 quarters.

```
//Create 16 random data points
y = rndu (16, 1);
//Start the series in 2007 Q4
dstart = 200710;
//Specify the data as quarterly
freq = 4;
//Plot the data
plotTS(dstart, freq, y);
```

This should produce a graph that looks similar to this:


Figure 6.13: Close-up of quarterly data plot

### 6.7.2 Controlling Tic Label Locations

The first tic label on the X -axis of the graph that we drew at the end of the last section is located on the first data point, 2007 Q4. Let us suppose that we would prefer the graph to have tic labels only on the first quarter of each year. We can accomplish this by using the function plotSetXTicInterval.
plotSetXTicInterval has the following parameters:
interval the number of data points between each X-tic that is labeled.

## firstLabeled

 the value of the first data point to be labeled.Since we are working with quarterly data and would like to place X -tic labels on each year, we will set the interval parameter equal to four and we will set the
firstLabeled to be the first full year in our series, 2008. This will change our program to look like this:

```
//Declare and initialize plotControl structure
struct plotControl myPlot;
myPlot = plotGetDefaults("xy");
//Create 16 example data points
y = exp(seqa (0, 0.2, 16)) + rndu(16, 1);
//Start the series in 2007 Q4 and specify
//quarterly data
dstart = 200710;
freq = 4;
//Start x-tic labels at 2008 and label every 4th
//data point
interval = 4;
firstLabeled = 2008;
plotSetXTicInterval(&myPlot, interval, firstLabeled);
//Plot the data
plotTS(myPlot, dstart, freq, y);
```

This code should create a graph with x-tic labels only on the first quarter of each year as you see below:


Figure 6.14: Quarterly data graph
We can see that the X-tics are in the correct location. However since we are only labeling each year, we may not want Q1 printed next to the year on each of the X-tic labels.

### 6.7.3 Tic Label Formatting

We can change the formatting of these labels and optionally the angle at which they are printed with the function plotSetXTicLabel. This function has the following arguments:
fmt
angle
string, specifying the format with which to format the X -tic labels.
scalar, the angle at which to print the labels

The fmt input can take many forms, see dttostr and strtodt for all options, but for this purpose we are only concerned with these three:

YYYY
QQ
MO
print the four digit year.
print the quarter as $\mathrm{Q} 1, \mathrm{Q} 2, \mathrm{Q} 3$ or Q 4 .
print the month as a two digit number.

These format specifiers can be placed in any order. You may place any characters in between them and they will be printed literally. For example if we start with 201204:

$$
f m t=" Y Y Y Y-Q Q "
$$

will tell GAUSS to print the date as:
2012-Q2
whereas:

```
fmt = "MO/YYYY";
```

tells GAUSS to print the date as:

```
04/2012
```

Since we want to print only the four digit year on our x-tic labels, we will set:

```
fmt = "YYYY";
```

Giving us the following program:

```
//Declare and initialize plotControl structure
struct plotControl myPlot;
myPlot = plotGetDefaults("xy");
//Create 16 example data points
y = exp (seqa (0, 0.2, 16)) + rndu (16, 1);
//Start the series in 2007 Q4 and specify
//quarterly data
```

```
dstart = 200710;
freq = 4;
//Start x-tic labels at 2008 and label every 4th
//data point
interval = 4;
firstLabeled = 2008;
plotSetXTicInterval(&myPlot, interval, firstLabeled);
//Label X-tics with only the 4 digit year
plotSetXTicLabel(&myPlot, "YYYY");
//Plot the data
plotTS(myPlot, dstart, freq, y);
```

This final program should yield a graph that looks similar to:


Figure 6.15: Quarterly data graph

### 6.8 Interacting with Plots in GAUSS

Once a graph has been created, GAUSS provides interactive zooming, panning, and the moving of legends and subplots as well as the ability to hide and restore individual curves on the graph. Plot rotation is also available for 3-dimensional plots.

### 6.8.1 Interacting with 2-D Plots

To interact with plots in GAUSS, first select the "Zoom/Pan Plot" button from the toolbar. With this button selected, you will be able to perform actions on the view of a particular plot. Zooming is controlled by the mouse scroll wheel. Scroll the mouse wheel forward to zoom in. Pan and scroll is accomplished by drag-and-drop with the mouse. Note that upon zooming or panning, the axes will be automatically updated to reflect the new view.


Figure 6.16: Zoom/Pan Plot Toolbar

## Hide/Restore Curves

Each legend item is also a button that hides and restores individual curves, bars, etc. Click on a legend item to hide the corresponding curve. Notice that the axes will automatically scale to the remaining curves. Click the legend item again to restore the curve to the graph.


Figure 6.17: The legend acts as a button to hide curves

## Relocating Graphic Items

To relocate subplots or legends first select the "Revise Layout" button. You may then drag and drop the item to its desired location. If you would like the legend to maintain its position relative to the graph when it is relocated, you can accomplish this by selecting the legend, right-clicking and selecting "regroup" from the context menu.


Figure 6.18: Drag and drop to relocate the legend
If you would like to change the z-order of an item in a layout, you may select it, rightclick to bring up the context menu and then choose, either "Send to Front" or "Send to Back." Individual plots and their respective legends will both be affected.


Figure 6.19: Bring textbox to top of z -order to cover arrow tail

### 6.8.2 3-D Plots



Figure 6.20: Surface plot

## Zoom

Zooming in and out on a 3-dimensional graph may be accomplished by use of the mouse scroll wheel.

## Rotate/Viewpoint Change

To rotate 3-dimensional plots and examine the graph from different viewpoints, rightclick and drag with the mouse (two-finger click and drag on Mac).

### 6.8.3 File Export

When exporting a graph interactively, the first step is to set the size of the entire graph image, called the Canvas.

## Customizing the Canvas

To access the Canvas settings, from the Graphics Page toolbar select "View->Graphics Settings". This will display the settings for whichever graphics object has focus. This could be the graph and its legend, an annotation object such as an arrow or textbox, or the Canvas. To give focus to the Canvas, click between the edge of your graph and the edge of the graphics tab.


Figure 6.21: Select Canvas

Once you have opened the Canvas settings, set "Fixed Size" to "true". This will prevent the Canvas, and your graph, from being resized if you manually resize your GAUSS window. With this box is checked, the Canvas size will be controlled only by the Canvas Settings window.

## Setting the size in terms of pixels

If you will be using the image in an electronic format, you will want to set the image size in terms of pixels. The "Units" Canvas setting controls whether the canvas will be
sized in terms of pixels or a unit of physical size. By default, "Units" will be set to "pixels".

Double-click the numbers in the "Width" and "Height" boxes to edit the numbers. If the "Fixed Ratio" option is set to "true", then when you change the "Width" or the "Height", the other dimension will be changed to keep the height-to-width ratio the same.

| Graph Settings |  | $5 \times$ |
| :---: | :---: | :---: |
| Field | Value |  |
| 4 Canvas Size |  |  |
| Fixed Size | true $\quad$ - |  |
| Units | pixels $\quad$ - |  |
| Width | 800 |  |
| Height | 455.00 |  |
| Fixed Ratio | true $\quad$ - |  |
| DPI | 96 |  |
| 4 Canvas General |  |  |
| Background | $\square$ |  |

Figure 6.22: Control canvas size

## Setting the size in terms of physical size (inches, millimeters)

If you are exporting an image for print, you may want to set the image size in terms of a physical size. To accomplish this, you will need to set the "Units" to either "millimeters" or "inches" and you will have to set "Width", "Height", and the "DPI" or dots per inch. This will allow GAUSS to create an image with enough pixels for your image to be printed at your desired size with the required dots per inch.

## Make any final adjustments

As you will see, when you change the Canvas dimensions in GAUSS, the graph image will be adjusted to reflect those changes. This gives you a live preview of what your exported image will look like. After you have changed the overall size of your Canvas, you may want to make some adjustments to the size of fonts or lines on your graph to make them proportional to the new size of the whole. Click on the graph to display the Graph Settings in the Graphics Editor window, then make any necessary adjustments.

## Exporting the file

Once you have the image as you would like it, select File->Export Graph from the main application menu and then select a filename, image type, and folder in which to save your file.

## Copy and paste graphs into other programs

To copy and paste a graph from GAUSS to another program such as PowerPoint ${ }^{\circledR}$ or Word®, right click on the graph inside of GAUSS and select "Copy to clipboard". Next, open the other program and "paste" the graph at an appropriate location into your file.

Note that when you copy an image to the clipboard, it becomes a raster image, which means that resizing may decrease the image quality. Therefore, it is recommended that you first appropriately size the image in GAUSS before copying the image to the clipboard.

### 6.8.4 Saving Graphs

Graphs may be saved and then reloaded later. To save a graph, select the graph you would like to save and then select File->Save Graph from the main menu. GAUSS graphs are saved in a file with JSON format and a . plot extension.


Figure 6.23: Save Graph menu
Graphs may also be saved programmatically with the plotSave function.

### 6.9 Adding Annotations Programmatically in GAUSS

In addition to adding annotations such as text boxes, arrows and lines interactively with the Graphics Editor, you may also add annotations in your GAUSS program. This functionality is provided through the following functions:

| plotAddArrow | Adds arrows or lines to the last created graph. |
| :--- | :--- |
| plotAddShape | Adds ellipses and rectangles to the last created <br> graph. |

## plotAddTextbox Adds a textbox to the last created graph.

## Basic rules

1. As you can see from the function prefix, plotAdd, these functions are meant to add to a graph that already exists. They will not create a new graph.
2. Added annotations will not expand the range of the $X$ and $Y$ axis so that they will fit inside the visible axes. This allows you to place annotations outside the axes or between different subplots.

### 6.9.1 Basic usage

Like the plotting functions, the graph annotation functions can be called without any styling options specified, or the user can pass in a control structure which will set the styling for the annotation. Here is a basic example of adding a text box:

```
//Create and plot some data
x = seqa (0, 0.01, 628);
y = cos(x) ~ sin (x);
plotXY(x, y);
//Text to place in the text box
text_string = "Sine is the derivative of cosine";
//Location of the top left corner of the text box
//will be the position (3,0.8) on the graph
x_start = 3;
y_start = 0.8;
//Add text box
plotAddTextbox(text_string, x_start, y_start);
```

The positioning of the annotation, set by $x$ start and $y_{\text {_ }}$ start above, are in terms of the points on the graph to which the annotation is added.

Here is another basic example of adding an arrow:

```
//Arrow start and end locations
x_start = 3;
y_start = 0.8;
x_end = 1.07;
y_end = 0.5;
//Specify the head size
//at the end of the arrow
//in terms of points
head_size 10;
//Add the arrow to the last created graph
plotAddArrow(x_start, y_start, x_end, y_end, head_size);
```


### 6.9.2 Creating multiple annotations with vector inputs

You may create multiple annotations with one function call by passing vector inputs to plotAddArrow, plotAddShape or plotAddTextbox. Here is an example adding three text boxes to a graph at once:

```
//Create x and y coordinates
x = { 67, 80, 46};
y={2.9,3.6,1.4};
//Create scatter plot
plotScatter(x, y) ;
//Create string array of text labels
countries = "France" $| "Germany" $| "Spain";
//Add labels to scatter points
plotAddTextbox(countries, x, y);
```


### 6.9.3 Customization with a plotAnnotation structure

After an annotation has been added to a graph, you can customize it with the Graphics Editor. If you would to set the style for your annotation inside of your GAUSS program, you can do this with a plotAnnotation structure. The steps for using a plotAnnotation structure are:

1. Declare an instance of a plotAnnotation structure
2. Fill in the plotAnnotation with default values
3. Set your desired options
4. Pass the structure in as the first argument to one of the annotation add functions

If you would like to create an instance of a plotAnnotation structure called myAnnotation and fill it in with default values, steps 1 and 2 above, you would do this:

```
//Declare 'myAnnotation' to be an instance
//of a 'plotAnnotation' structure
struct plotAnnotation myAnnotation;
//Fill 'myAnnotation' with default values
myAnnotation = annotationGetDefaults();
```

Now you are ready to apply your desired style preferences to 'myAnnotation' with the 'annotationSet' functions. Available functions include:
annotationSetBkd Sets the color and transparency level of the

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annotationSetFont<br>annotationSetLineColor<br>annotationSetLineStyle<br>annotationSetLineThickness

annotation's background
Sets the font style, font size and font color for a text box
Sets the line color for an arrow or the border of a shape
Sets the line style for an arrow or the border of a shape
Sets the line thickness for an arrow or the border of a shape

You do not need to memorize this list or consult it when you are writing a program. Simply start typing "annotationSet" into the GAUSS editor and the autocomplete will provide the full list of available functions.

### 6.9.4 Using the annotationSet functions

The 'annotationSet' functions work in the same manner as the 'plotSet' functions. The first argument will be a pointer to a 'plotAnnotation' structure (which simply means that there is an ampersand (\&) in front of the name). The remaining arguments to the function will be the settings to apply.

## Example: Styling an ellipse

Let's say that we would like to highlight a section of the center of our graph. We can do this by adding a semi-transparent circle to the center of the graph.

```
//Declare instance of 'plotAnnotation' structure
struct plotAnnotation myEllipse;
//Fill in 'myEllipse' with default values
```

```
myEllipse = annotationGetDefaults();
//Set the ellipse color to be violet
//and make it 30% opaque
annotationSetBkd(&myEllipse, "violet", 0.3);
//Add ellipse to the center of the graph
x_start = 2;
y_start = 5;
x_end = 3;
y_end = 8;
plotAddShape(myEllipse, "ellipse", x_start, y_start, x_end,
y_end) ;
```

To see examples of styling text boxes or arrows see the documentation for plotAddTextbox and plotAddArrow.

## 7 Graphics Editing

GAUSS allows you to interactively change most all attributes of a created graph. First create a graph. For demonstration purposes you may run the example program randomwalk.e to create a graph. Next open the Graph Settings window if it is not open already, by selecting View->Graph Settings from the menu bar.


Figure 7.1: Open the Graph Settings Window

### 7.1 Changing Appearance

Click on the graph or a graph annotation object to view its settings in the Graph Settings Window. When an item is selected its outer border will be highlighted with a red, dash line. Interacting with the Graph Settings is simple. Single-click on color squares to open a color settings dialog. Single-click on drop-down menus to view the available options. Double-click on font names to open your systems font dialog and also double-click on text inputs, such as the "X-Axis" label, to enter new text.


Figure 7.2: Color Palette

For example, click on the red color square next to "Line Color" under "Curve 1" to open the Color Palette dialog as shown above. Double-click the current text next to "Caption" under "Title" to enter text for the graph title as shown below.


Figure 7.3: Text Options

Double-click font names in the graph settings window to open a font dialog window.


Figure 7.4: Font Options

### 7.2 Adding Items

The Graphics Page toolbar has buttons for adding

- Lines and arrows
- Rectangles
- Ellipses
- Text boxes

To add an item, click the appropriate toolbar button and then click and drag to create the object in your graphic window.


Figure 7.5: Select the item to add


Figure 7.6: Click and drag to add the object

### 7.3 Adding Text to a Text Box

First add the textbox to the graph by selecting the textbox icon, which looks like a capital T, from the main GAUSS menubar. Then click and drag to size the textbox inside of your graph.


Figure 7.7: Color Palette

When you finish sizing the textbox, the Graphics Settings Window will open, displaying the graphical controls that allow you to customize the textbox. Towards the bottom of the graphics Settings Window will be the Content Input Pane. Its header will read "Content (Text/HTML). Enter the text that you would like to appear inside the textbox in the Content Input Pane and click the "Apply" button. You may enter text which can include snippets of HTML to create subscripting, superscripting, Greek letters or other special characters and formatting.

## Text

Font MS Shell Dig 28
Color Alignment Left Content (Text/HTML) This series represents

Figure 7.8: Entering content for a textbox

### 7.4 Which Object Will Be Edited?

If a graph or graphics object is actively selected, its border will be highlighted red. Changes made in the Graph Settings Window will apply to this selected object. If no object is actively selected, the Graph Settings Window will display the settings for the Canvas. The Canvas is the entire scene in which the graph or graphs are placed.
Changing the Canvas properties is used to make final changes to the sizing of a graph before exporting.


Figure 7.9: Highlighted Object

### 7.5 Moving and Resizing Objects

To move an object, including graphs, legends, textboxes and other annotations, hover your mouse over it. When your mouse pointer is a hand icon and the object you would like to move has a blue highlight around its edges, click and drag to move the object to its desired location.


Figure 7.10: Moving a graphic object
Hover over the corner of an object until your mouse pointer is two opposing arrows and the object has a blue edge highlight. Then click and drag to resize the object.


Figure 7.11: Resizing a graphic object

### 7.5.1 Note on Programmatic Annotations

Annotations that are added programmatically are tied to the coordinates to which they are placed. Items that are placed on the graph by two graph coordinate points such as arrow cannot be manually relocated. Items that are placed on the graph by only one coordinate point, such as textboxes, may be manually pivoted around the fixed point.

## 8 Using the Command Line Interface

TGAUSS is the command line version of GAUSS. The executable file, tgauss, is located in the GAUSS installation directory.

The format for using TGAUSS is:

| tgauss flag(s) program program. . |  |
| :--- | :--- |
| $-b$ | Execute file in batch mode and then exit. You can <br> execute multiple files by separating file names with <br> spaces. |
| -1 logfile | Set the name of the batch mode log file when using <br> the -b argument. The default is tmp/gauss.log\#\#\#, <br> where \#\#\# is the process ID. |
| $-e$ expression | Execute a GAUSS expression. This command is not <br> logged when GAUSS is in batch mode. |
| $-T$ | Suppress the sign-on banner (output only). |
| $-T$ | Turn the dataloop translator on. |

```
-t Turn the dataloop translator off.
```


### 8.1 Viewing Graphics

NOTE: Graphics using plot* functions are only available from the graphical user interface.

The deprecated Publication Quality Graphics graphics generated .tkf files for graphical output. The default output for these graphics is graphic.tkf. On Windows, you can use vwr. exe to view the graphics file; on Linux/Mac, you can use vwrmp. Two functions are available to convert.$t k f$ files to PostScript for printing and viewing with external viewers: the $t k f 2 p s$ function will convert.$t k f$ files to PostScript (.ps) files, and the tkf2eps function will convert . tkf files to encapsulated PostScript (.eps) files. For example, to convert the file graphic.tkf to a postscript file named graphic.ps use:

```
ret = tkf2ps("filename.tkf", "filename.ps")
```

If the function is successful it returns 0 .

### 8.2 Command Line History and Command Line Editing

When you run a command at the TGAUSS prompt, it is added to your command line history, which is stored in a file called .gauss_prompt_history in your \$(HOME) directory on Linux or in your \$(HOMEDRIVE) $\$($ HOMEPATH) directory on Windows. A separate history for commands entered in the command line debugger is stored in a file called .gauss_debug_prompt_history in the same directory. By default, the last 500 commands executed at the TGAUSS and debugger command lines are stored in these files. You can change this number by changing prompt_hist_num in your gauss.cfg file. The following keystrokes are supported for movement and editing at the command line and for retrieving the command line history:

### 8.2.1 Movement

| HOME or CTRL+A | Moves cursor to beginning of line |
| :--- | :--- |
| END or CTRL+E | Moves cursor to end of line |
| 8.2.2 Editing |  |
| DELETE or CTRL+D |  |
| BACKSPACE or <br> CTRL+H | Deletes character at cursor |
| CTRL+U | Deletes character left of cursor |
| CTRL+K | Cuts all characters left of cursor |
| CTRL+X | Cuts whole line characters right of cursor, including cursor |
| ESC (Win only) | Deletes whole line |
| CTRL+V | Pastes text from buffer to left of cursor |
| CTRL+T | Transposes character at cursor and character left of <br> cursor |

### 8.2.3 History Retrieval

| Up Arrow or <br> CTRL +P | Retrieves previous line in history |
| :--- | :--- |
| Down Arrow or <br> CTRL $+P$ | Retrieves next line in history |


| PAGE UP or CTRL+W | Retrieves previous line in history that matches text to left of cursor |
| :---: | :---: |
| PAGE DOWN or CTRL+S | Retrieves next line in history that matches text to left of cursor |
| ALT+H or OPTION+H (MAC only) | Prints prompt history to screen |
| ! ! | Runs last line in history |
| ! num | Runs the num line in history |
| !- num | Runs the line num before current line in history; |
|  | !-1 is equivalent to !! |
| ! text | Runs last line in history beginning with text |
| ALT+/ or ALT+? or <br> OPTION+/ (MAC only) | Prints help screen |

Note that some of these keystrokes are mapped differently on different computers. For example, on some computers, SHIFT+RIGHT ARROW behaves the same as RIGHT ARROW, while ALT+RIGHT ARROW moves the cursor right one word. Therefore, multiple keystroke mappings have been supported to maximize the availability of these commandson any given machine.

### 8.3 Interactive Commands

This section discusses interactive commands available in TGAUSS.

### 8.3.1 quit

The quit command will exit TGAUSS.
The format for quit is:

```
quit
```

You can also use the system command to exit TGAUSS from either the command line or a program (see system in the GAUSS LANGUAGE REFERENCE).

The format for system is:

```
system
```


### 8.3.2 ed

The ed command will open an input file in an external text editor (see ed in the GAUSS LANGUAGE REFERENCE).

The format for ed is:

```
ed filename
```


### 8.3.3 browse

The browse command allows you to search for specific symbols in a file and open the file in the default editor. You can use wildcards to extend search capabilities of the browse command.

The format for browse is:

## browse

symbol

### 8.3.4 config

The config command gives you access to the configuration menu allowing you to change the way GAUSS runs and compiles files.

The format for config is:

```
config
```


## Run Menu

| Translator | Toggles on/off the translation of a file using <br> dataloop. The translator is not necessary for <br> GAUSS program files not using dataloop. |
| :--- | :--- |

Translator line Toggles on/off execution time line number tracking number tracking of the original file before translation.

Line number tracking

Toggles on/off the execution time line number tracking. If the translator is on, the line numbers refer to the translated file.

## Compile Menu

| Autoload | Toggles on/off the autoloader. |
| :--- | :--- |
| Autodelete | Toggles on/off autodelete. |
| GAUSS Library | Toggles on/off the GAUSS library functions. |
| User Library | Toggles on/off the user library functions. |
| Declare Warnings | Toggles on/off the declare warning messages during <br> compiling. |


| Compiler Trace | Includes the following options: <br> Off <br> Turns off the compiler trace <br> function. |
| :--- | :--- |
| Line | Traces program file openings and <br> closings. |
| Symbol | Treates a report of procedures and the local and <br> global symbols they reference. |

### 8.4 Debugging

The debug command runs a program under the source level debugger.
The format for debug is:

```
debug filename
```


### 8.4.1 General Functions

?
Displays a list of available commands.
q/Esc
Exits the debugger and returns to the GAUSS command line.
+/-
Disables the last command repeat function.

### 8.4.2 Listing Functions

1 number Displays a specified number of lines of source code in the current file.
lc
Displays source code in the current file starting with the current line.

Displays source code in the named file starting with the specified line.

11 file Displays source code in the named file starting with the first line.

11 line Displays source code starting with the specified line. File does not change.

11 Displays the next page of source code.
$1 p$
Displays the previous page of source code.

### 8.4.3 Execution Functions

| $\mathbf{s}$ number | Executes the specified number of lines, stepping into <br> procedures. |
| :--- | :--- |
| $\mathbf{n}$ number | Executes the specified number of lines, stepping over <br> procedures. |
| $\mathbf{x}$ number | Executes code from the beginning of the program to <br> the specified line count, or until a breakpoint is hit. |
| $\mathbf{g}$ | Executes from the current line to the end of the <br> program, stopping at breakpoints. The optional <br> arguments specify other stopping points. The syntax |

for each optional argument is:

| filename <br> line <br> period | The debugger will stop every period times it reaches the specified line in the named file. |
| :---: | :---: |
| filename line | The debugger will stop when it reaches the specified line in the named file. |
| filename <br> ,, period | The debugger will stop every period times it reaches any line in the named file. |
| Iine period | The debugger will stop every period times it reaches the specified line in the current file. |
| filename | The debugger will stop at every line in the named file. |
| Iine | The debugger will stop when it reaches the specified line in the current file. |
| procedure period | The debugger will stop every period times it reaches the first line in a called procedure. |
| procedure | The debugger will stop every time it reaches the first line in a called procedure. |

j Executes code to a specified line, procedure, or period in the file without stopping at breakpoints. The optional arguments are the same as $\mathbf{g}$, listed above.
jx number
Executes code to the execution count specified (number) without stopping at breakpoints.

Executes the remainder of the current procedure (or to a breakpoint) and stops at the next line in the calling procedure.

### 8.4.4 View Commands

| $\mathbf{v}[$ vars $]]$ | Searches for (a local variable, then a global variable) <br> and displays the value of a specified variable. |
| :--- | :--- |
| $\mathbf{v} \mathbf{\$ [}[$ vars $]]$ | Searches for (a local variable, then a global variable) <br> and displays the specified character matrix. |

The display properties of matrices and string arrays can be set using the following commands.

| $\mathbf{r}$ | Specifies the number of rows to be shown. |
| :--- | :--- |
| c | Specifies the number of columns to be shown. |
| num, num | Specifies the indices of the upper left corner of the <br> block to be shown. |
| w | Specifies the width of the columns to be shown. <br> p |
| Specifies the precision shown. |  |

f Specifies the format of the numbers as decimal, scientific, or auto format.
$q$
Quits the matrix viewer.

### 8.4.5 Breakpoint Commands

lb Shows all the breakpoints currently defined.
b Sets a breakpoint in the code. The syntax for each optional argument is:

| filename line | The debugger will stop every |
| :--- | :--- |
| period |  |
|  | period times it reaches the specified |
| line in the named file. |  |

filename line The debugger will stop when it reaches the specified line in the named file.
filename ,, The debugger will stop every
period period times it reaches any line in the named file.
line period The debugger will stop every period times it reaches the specified line in the current file.
filename
line

The debugger will stop at every line in the named file.

The debugger will stop when it reaches the specified line in the current file.
procedure The debugger will stop every
period times it reaches the first line in a called procedure.

The debugger will stop every time it reaches the first line in a called procedure.
d Removes a previously specified breakpoint. The optional arguments are the same arguments as $b$, listed above.

### 8.5 Using the Source Browser in TGAUSS

To start the Source Browser in TGAUSS, type BROWSE followed by a symbol name. When the Source Browser is active, the prompt displays Browse : GAUSS searches through all active libraries for the file in which the symbol is defined. If found, the file containing the source code is opened in the default editor.

Wildcard (*) searches can also be used. When using wildcard searches, each symbol that the string matches will be displayed on-screen in a numbered list. To select a specific command to view in the default editor, select the number from the list.

The Source Browser will remain active until you type CTRL+C to return to the GAUSS prompt.

## 9 Language Fundamentals

GAUSS is a compiled language. GAUSS is also an interpreter. A compiled language, because GAUSS scans the entire program once and translates it into a binary code before it starts to execute the program. An interpreter, because the binary code is not the native code of the CPU. When GAUSS executes the binary pseudocode it must "interpret" each instruction for the computer.

How can GAUSS be so fast if it is an interpreter? Two reasons. First, GAUSS has a fast interpreter, and the binary compiled code is compact and efficient. Second, and most significantly, GAUSS is a matrix language. It is designed to tackle problems that can be solved in terms of matrix or vector equations. Much of the time lost in interpreting the pseudocode is made up in the matrix or vector operations.

This chapter will enable you to understand the distinction between "compile time" and "execution time," two very different stages in the life of a GAUSS program.

### 9.1 Expressions

An expression is a matrix, string, constant, function reference, procedure reference, or any combination of these joined by operators. An expression returns a result that can be assigned to a variable with the assignment operator ${ }^{\prime}=$ '.

### 9.2 Statements

A statement is a complete expression or command. Statements end with a semicolon.

$$
y=x * 3
$$

If an expression has no assignment operator ( $=$ ), it will be assumed to be an implicit print statement:

```
print x*3;
```

```
x*3;
```

Here is an example of a statement that is a command rather than an expression:

```
output on;
```

Commands cannot be used as a part of an expression.
There can be multiple statements on the same line as long as each statement is terminated with a semicolon.

### 9.2.1 Executable Statements

Executable statements are statements that can be "executed" over and over during the execution phase of a GAUSS program (execution time). As an executable statement is compiled, binary code is added to the program being compiled at the current location of the instruction pointer. This binary code will be executed whenever the interpreter passes through this section of the program. If this code is in a loop, it will be executed each iteration of the loop.

Here are some examples of executable statements:

```
y = 34.25;
```

```
print y;
```

```
x = 1 3 7 2 9 4 0 3;
```


### 9.2.2 Nonexecutable Statements

Nonexecutable statements are statements that have an effect only when the program is compiled (compile time). They generate no executable code at the current location of the instruction pointer.

Here are two examples:

```
declare matrix x = 1 2 3 4 ;
```

```
external matrix ybar;
```

Procedure definitions are nonexecutable. They do not generate executable code at the current location of the instruction pointer.

Here is an example:

```
zed = rndn(3,3);
proc sqrtinv(x);
    local y;
    y = sqrt(x);
    retp(y+inv(x));
endp;
zsi = sqrtinv(zed);
```

There are two executable statements in the example above: the first line and the last line. In the binary code that is generated, the last line will follow immediately after the
first line. The last line is the call to the procedure. This generates executable code. The procedure definition generates no code at the current location of the instruction pointer.

There is code generated in the procedure definition, but it is isolated from the rest of the program. It is executable only within the scope of the procedure and can be reached only by calling the procedure.

### 9.3 Programs

A program is any set of statements that are run together at one time. There are two sections within a program.

### 9.3.1 Main Section

The main section of the program is all of the code that is compiled together WITHOUT relying on the autoloader. This means code that is in the main file or is included in the compilation of the main file with an \#include statement. ALL executable code should be in the main section.

There must always be a main section even if it consists only of a call to the one and only procedure called in the program.

### 9.3.2 Secondary Sections

Secondary sections of the program are files that are neither run directly nor included in the main section with \#include statements.

The secondary sections of the program can be left to the autoloader to locate and compile when they are needed. Secondary sections must have only procedure definitions and other nonexecutable statements.
\#include statements are allowed in secondary sections as long as the file being included does not violate the above criteria.

Here is an example of a secondary section:

```
declare matrix tol = 1.0e-15;
proc feq(a,b);
    retp (abs (a-b) <= tol);
endp;
```


### 9.4 Compiler Directives

Compiler directives are commands that tell GAUSS how to process a program during compilation. Directives determine what the final compiled form of a program will be. They can affect part or all of the source code for a program. Directives are not executable statements and have no effect at run-time. They do not take a semicolon at the end of the line.

The \#include statement mentioned earlier is actually a compiler directive. It tells GAUSS to compile code from a separate file as though it were actually part of the file being compiled. This code is compiled in at the position of the \# include statement.

Here are the compiler directives available in GAUSS:

| \#define | Define a case-insensitive text-replacement or flag <br> variable. |
| :--- | :--- |
| \#definecs | Define a case-sensitive text-replacement or flag <br> variable. |
| \#undef | Undefine a text-replacement or flag variable. <br> \#ifdef |
| \#ifndef | \#define'd. <br> Compile code block if a variable has not been <br> \#define'd. |
| \#iflight | Compile code block if running GAUSS Light. |


| \#ifunix | Compile code block if running UNIX. |
| :--- | :--- |
| \#else | Else clause for \#if-\#else-\#endif code block. |
| \#endif | End of \#if-\#else-\#endif code block. |
| \#include | Include code from another file in program. |
| \#lineson | Compile program with line number and file name <br> records. |
| \#linesoff | Compile program without line number and file name <br> records. |
| \#srcline | Insert source file name record at this point (currently <br> used when doing data loop translation). |
|  | Insert source file line number record at this point <br> (currently used when doing data loop translation). |

The \#define statement can be used to define abstract constants. For example, you could define the default graphics page size as:

```
#define hpage 9.0
#define vpage 6.855
```

and then write your program using hpage and vpage. GAUSS will replace them with 9.0 and 6.855 when it compiles the program. This makes a program much more readable.

The \#ifdef-\#else-\#endif directives allow you to conditionally compile sections of a program, depending on whether a particular flag variable has been \#define'd. For example:

```
#ifdef log_10
    y = log(x);
#else
```

```
    y = ln}(x)
#endif
```

This allows the same program to calculate answers using different base logarithms, depending on whether or not the program has a \#define log_10 statement at the top.
\#undef allows you to undefine text-replacement or flag variables so they no longer affect a program, or so you can \#define them again with a different value for a different section of the program. If you use \#definecs to define a case-sensitive variable, you must use the right case when \#undef'ing it.

With \#lineson, \#linesoff, \#srcline, and \#srcfile you can include line number and file name records in your compiled code, so that run-time errors will be easier to track down. \#srcline and \#srcfile are currently used by GAUSS when doing data loop translation.

For more information on line number tracking, see Debugging, Section 8.4 and see Debugging Data Loops, Section 25.3. See also \#lineson in the GAUSS LANGUAGE REFERENCE.

The syntax for \#srcfile and \#srcline is different than for the other directives that take arguments. Typically, directives do not take arguments in parentheses; that is, they look like keywords:

```
#define red 4
```

\#srcfile and \#srcline, however, do take their arguments in parentheses (like procedures):

```
#srcline(12)
```

This allows you to place \#srcline statements in the middle of GAUSS commands, so that line numbers are reported precisely as you want them. For example:

```
#srcline(1) print "Here is a multi-line "
#srcline(2) "sentence--if it contains a run-time error, "
```

```
#srcline(3) "you will know exactly "
#srcline(4) "which part of the sentence has the problem.";
```

The argument supplied to \#srcfile does not need quotes:

```
#srcfile(/gauss/test.e)
```


### 9.5 Procedures

A procedure allows you to define a new function which you can then use as if it were an intrinsic function. It is called in the same way as an intrinsic function.

```
y = myproc (a,b,c);
```

Procedures are isolated from the rest of your program and cannot be entered except by calling them. Some or all of the variables inside a procedure can be local variables. local variables exist only when the procedure is actually executing and then disappear. Local variables cannot get mixed up with other variables of the same name in your main program or in other procedures.

For details on defining and calling procedures, see Procedures and Keywords, Chapter 11.

### 9.6 Data Types

There are four basic data types in GAUSS, matrices, N-dimensional arrays, strings and string arrays. It is not necessary to declare the type of a variable, but it is good programming practice to respect the types of variables whenever possible. The data type and size can change in the course of a program.

The declare statement, used for compile-time initialization, enforces type checking.
Short strings of up to 8 bytes can be entered into elements of matrices, to form character matrices (For details, see Command Summary, Section 28.1 ).

### 9.6.1 Constants

The following constant types are supported:

## Decimal

Decimal constants can be either integer or floating point values:

```
1.34e-10
1.34e123
-1.34e+10
-1.34d-10
    1.34d10
    1.34d+10
    123.456789345
```

Up to 18 consecutive digits before and after the decimal point(depending on the platform) are significant, but the final result will be rounded to double precision if necessary. The range is the same as for matrices (For details, see Matrices, Section 9.6.2

## String

String constants are enclosed in quotation marks:

```
"This is a string."
```


## Hexadecimal Integer

Hexadecimal integer constants are prefixed with $0 x$ :

```
0x0ab53def2
```


## Hexadecimal Floating Point

Hexadecimal floating point constants are prefixed with 0 v . This allows you to input a double precision value exactly as you want using 16 hexadecimal digits. The highest order byte is to the left:

```
Ovfff8000000000000
```


### 9.6.2 Matrices

Matrices are 2-dimensional arrays of double precision numbers. All matrices are implicitly complex, although if it consists only of zeros, the imaginary part may take up no space. Matrices are stored in row major order. A $2 \times 3$ real matrix will be stored in the following way from the lowest addressed element to the highest addressed element:

$$
[1,1] \quad[1,2] \quad[1,3] \quad[2,1] \quad[2,2] \quad[2,3]
$$

A $2 \times 3$ complex matrix will be stored in the following way from the lowest addressed element to the highest addressed element:

```
(real part)
[1,1] [1,2] [1,3] [2,1] [2,2] [2,3]
(imaginary part) [1,1] [1,2] [1,3] [2,1] [2,2] [2,3]
```

Conversion between complex and real matrices occurs automatically and is transparent to the user in most cases. Functions are provided to provide explicit control when necessary.

All elements of a GAUSS matrix are stored in double precision floating point format, and each takes up 8 bytes of memory. This is the IEEE 754 format:

| Bytes | Data Type | Significant Digits | Range |
| ---: | :---: | :---: | :---: |
| 8 | floating point | $15-16$ | $4.19 \times 10^{-307}$ |
|  |  |  | $<=\|X\|<=1.67 \times$ |
|  |  |  | $10^{+308}$ |

Matrices with only one element ( 1 x 1 matrices) are referred to as scalars, and matrices with only one row or column ( 1 xN or Nx 1 matrices) are referred to as vectors.

Any matrix or vector can be indexed with two indices. Vectors can be indexed with one index. Scalars can be indexed with one or two indices also, because scalars, vectors, and matrices are the same data type to GAUSS.

The majority of functions and operators in GAUSS take matrices as arguments. The following functions and operators are used for defining, saving, and loading matrices:

| [ ] | Indexing matrices. |
| :---: | :---: |
| $=$ | Assignment operator. |
| । | Vertical concatenation. |
| $\sim$ | Horizontal concatenation. |
| con | Numeric input from keyboard. |
| cons | Character input from keyboard. |
| declare | Compile-time matrix or string initialization. |
| let | Matrix definition statement. |
| load | Load matrix (same as loadm). |
| readr | Read from a GAUSS matrix or data set file. |
| save | Save matrices, procedures and strings to disk. |
| saved | Convert a matrix to a GAUSS data set. |
| stof | Convert string to matrix. |
| submat | Extract a submatrix. |
| writer | Write data to a GAUSS data set. |

Following are some examples of matrix definition statements.
An assignment statement followed by data enclosed in braces is an implicit let statement. Only constants are allowed in let statements; operators are illegal. When braces are used in let statements, commas are used to separate rows. The statement

```
let }x=123,456,789
```

or

$$
x=123,456,789 \text {; }
$$

will result in

$$
\mathrm{x}=\begin{array}{lll}
1 & 2 & 3 \\
4 & 5 & 6 \\
7 & 8 & 9
\end{array}
$$

The statement

```
let }x[3,3]=12345678 9
```

will result in

$$
x=\begin{array}{lll}
1 & 2 & 3 \\
4 & 5 & 6 \\
7 & 8 & 9
\end{array}
$$

The statement

$$
\text { let } x[3,3]=1 \text {; }
$$

will result in

$$
\mathrm{x}=\begin{array}{lll}
1 & 1 & 1 \\
1 & 1 & 1 \\
1 & 1 & 1
\end{array}
$$

The statement

$$
\text { let } x[3,3] \text {; }
$$

will result in

```
0 0 0
x = 0 0 0
    0 0
```

The statement

```
let x = 1 2 3 4 5 6 7 8 9;
```

will result in
1
2
3
4
5
6
7
8
9

Complex constants can be entered in a let statement. In the following example, the + or - is not a mathematical operator, but connects the two parts of a complex number. There should be no spaces between the + or - and the parts of the number. If a number has both real and imaginary parts, the trailing 'i' is not necessary. If a number has no real part, you can indicate that it is imaginary by appending the ' i '. The statement

```
let x[2,2] = 1+2i 3-4 5 6i;
```

will result in

$$
x=\begin{array}{cc}
1+2 i & 3-4 i \\
5 & 0+6 i
\end{array}
$$

Complex constants can also be used with the declare, con and stof statements.
An "empty matrix" is a matrix that contains no data. Empty matrices are created with the let statement and braces:

```
x = {};
```

Empty matrices are supported by several functions, including rows and cols and the concatenation $(\sim, \mid)$ operators.

```
x = {};
hsec0 = hsec;
do until hsec-hsec0 > 6000;
    x = x ~ data_in(hsec-hsec0);
endo;
```

You can test whether a matrix is empty by entering rows $(x), \operatorname{cols}(x)$ and scalerr (x). If the matrix is empty rows and cols will return a 0 , and scalerr will return 65535.

The $\sim$ is the horizontal concatenation operator and the $\mid$ is the vertical concatenation operator. The statement

$$
y=1 \sim 2 \mid 3 \sim 4 ;
$$

will be evaluated as

$$
y=(1 \sim 2) \mid(3 \sim 4) ;
$$

and will result in a $2 \times 2$ matrix because horizontal concatenation has precedence over vertical concatenation:

$$
y=\begin{array}{ll}
1 & 2 \\
3 & 4
\end{array}
$$

The statement

$$
y=1+1 \sim 2 * 2 \mid 3-2 \sim 6 / 2 ;
$$

will be evaluated as

$$
y=((1+1) \sim(2 * 2)) \quad \mid((3-2) \sim(6 / 2)) ;
$$

and will result in a $2 \times 2$ matrix because the arithmetic operators have precedence over concatenation:

$$
\begin{array}{rl}
y= & 4 \\
1 & 3
\end{array}
$$

For more information, see Operator Precedence, Section 10.7 .
The let command is used to initialize matrices with constant values:

$$
\text { let } \mathrm{x}[2,2]=123 \text {; }
$$

Unlike the concatenation operators, it cannot be used to define matrices in terms of expressions such as:

$$
y=x 1-x 2 \sim x 2 \mid x 3 * 3 \sim x 4 ;
$$

The statement

$$
y=x[1: 3,5: 8] ;
$$

will put the intersection of the first three rows and the fifth through eighth columns of $x$ into the matrix $y$.

The statement

$$
y=x\left[\begin{array}{llll}
1 & 3 & 1,5 & 5
\end{array}\right] ;
$$

will create a $3 x 3$ matrix $y$ with the intersection of the specified rows and columns pulled from $x$ (in the indicated order).

The following code

```
let r = 1 3 1;
let c = 5 5 9;
y = x[r,c];
```

will have the same effect as the previous example, but is more general.

The statement

$$
y[2,4]=3 ;
$$

will set the 2,4 element of the existing matrix $y$ to 3 . This statement is illegal if $y$ does not have at least 2 rows and 4 columns.

The statement

$$
x=\operatorname{con}(3,2) ;
$$

will cause the following prompt to be printed in the window:

```
- (1,1)
```

indicating that the user should enter the [1,1] element of the matrix. Entering a number and then pressing ENTER will cause a prompt for the next element of the matrix to appear. Pressing ? will display a help screen, and pressing $x$ will exit.

The statement

```
load x[] = b:mydata.asc
```

will load data contained in an ASCII file into an Nx1 vector $x$. (Use rows ( $x$ ) to find out how many numbers were loaded, and use reshape ( $x, N, K$ ) to reshape it to an NxK matrix).

The statement

```
load x;
```

will load the matrix x . fmt from disk (using the current load path) into the matrix x in memory.

The statement

```
open d1 = dat1;
x = readr (d1,100);
```

will read the first 100 rows of the GAUSS data set dat1. dat.

### 9.6.3 Sparse Matrices

Many GAUSS operators and commands support the sparse matrix data type. You may use any of the following commands to create a sparse matrix:

```
denseToSp Converts a dense matrix to a sparse matrix.
denseToSpRE Converts a dense matrix to a sparse matrix, using a
relative epsilon.
Creates a sparse matrix from a packed matrix of non-
zero values and row and column indices.
spCreate
spEye
spOnes
spZeros
Creates a sparse matrix from vectors of non-zero
values, row indices, and column indices.
Creates a sparse identity matrix.
Generates a sparse matrix containing only ones and zeros
Creates a sparse matrix containing no non-zero values.
```

See Sparse Matrices, Chapter 13 , for more information.

### 9.6.4 N-dimensional Arrays

Many GAUSS commands support arrays of N dimensions. The following commands may be used to create and manipulate an N -dimensional array:
aconcat
Concatenate conformable matrices and arrays in a user-specified dimension.
aeye
areshape
arrayalloc
arrayinit
mattoarray

Create an N -dimensional array in which the planes described by the two trailing dimensions of the array are equal to the identity.

Reshape a scalar, matrix, or array into an array of user-specified size.

Create an N -dimensional array with unspecified contents.

Create an N -dimensional array with a specified fill value.

Convert a matrix to a type array.

See N-Dimensional Arrays, Chapter 14 , for a more detailed explanation.

### 9.6.5 Strings

Strings can be used to store the names of files to be opened, messages to be printed, entire files, or whatever else you might need. Any byte value is legal in a string from 0 255. The buffer where a string is stored always contains a terminating byte of ASCII 0 . This allows passing strings as arguments to C functions through the Foreign Language Interface.

Here is a partial list of the functions for manipulating strings:

| \$+ Combine two strings into one long string. |  |
| :--- | :--- |
| chrs | Interpret following name as a variable, not a literal. |
| dttostr | Convert vector of ASCII codes to character string. |
|  | Convert a matrix containing dates in DT scalar <br> format to a string array. |


| ftocv | Character representation of numbers in NxK matrix. |
| :---: | :---: |
| ftos | Character representation of numbers in 1x1 matrix. |
| ftostrc | Convert a matrix to a string array using a C language format specification. |
| getf | Load ASCII or binary file into string. |
| indcv | Find index of element in character vector. |
| lower | Convert to lowercase. |
| stof | Convert string to floating point. |
| strindx | Find index of a string within a second string. |
| strlen | Length of a string. |
| strsect | Extract substring of string. |
| strsplit | Split an Nx1 string vector into an NxK string array of the individual tokens. |
| strsplitPad | Split a string vector into a string array of the individual tokens. Pads on the right with null strings. |
| strtodt | Convert a string array of dates to a matrix in DT scalar format. |
| strtof | Convert a string array to a numeric matrix. |
| strtofcplx | Convert a string array to a complex numeric matrix. |
| upper | Convert to uppercase. |

Convert from string to numeric vector of ASCII codes.

Strings can be created like this:

```
x = "example string";
```

or

```
x = cons; // keyboard input
```

or

```
x = getf("myfile",0); // read a file into a string
```

They can be printed like this:

```
print x;
```

A character matrix must have a ' $\$$ ' prefixed to it in a print statement:

```
print $x;
```

A string can be saved to disk with the save command in a file with a .fst extension and then loaded with the load command:

```
save x;
loads x;
```

or

```
loads x=x.fst;
```

The backslash is used as the escape character inside double quotes to enter special characters:

| $" \ b "$ | backspace (ASCII 8) |
| :---: | :---: |
| "\e" | escape (ASCII 27) |
| " $\$ ¢" & formfeed (ASCII 12)  \hline " $\backslash \mathrm{g} "$ | beep (ASCII 7) |
| "\1" | line feed (ASCII 10) |
| "\ヶ" | carriage return (ASCII 13) |
| "\t" | tab (ASCII 9) |
| " |  |
| " | a backslash |
| " \( |  |
| ) \#\#\#" | the ASCII character whose decimal value is "\#\#\#". |

When entering DOS pathnames in double quotes, two backslashes must be used to insert one backslash:

```
st = "c:\\gauss\\myprog.prg";
```

An important use of strings and character elements of matrices is with the substitution operator $(\wedge)$. In the command

```
create f1 = olsdat with x,4,2;
```

by default, GAUSS will interpret the olsdat as a literal; that is, the literal name of the GAUSS data file you want to create. It will also interpret the $x$ as the literal prefix string for the variable names: $x 1 \times 2 \times 3 \times 4$. If you want to get the data set name from a string variable, the substitution operator $\left(^{\wedge}\right)$ could be used as:

```
dataset="olsdat";
create f1=^dataset with x,4,2;
```

If you want to get the data set name from a string variable and the variable names from a character vector, use

```
dataset="olsdat";
let vnames=age pay sex;
create f1=^dataset with ^vnames,0,2;
```

The substitution operator $\left({ }^{\wedge}\right)$ works with load and save also:

```
lpath="/gauss/procs";
name="mydata";
load path=^lpath x=^name;
command="dir *.fmt";
```

The general syntax is:

```
^variable_name
```

Expressions are not allowed. The following commands are supported with the substitution operator ( ${ }^{\wedge}$ ):

```
create f1=^dataset with ^vnames,0,2;
create fl=^dataset using ^cmdfile;
open fl=^dataset;
output file=^outfile;
load x=^datafile;
load path=^lpath x,y,z,t,w;
loadexe buf=^exefile;
save ^name=x;
save path=^spath;
dos ^cmdstr;
run ^prog;
msym ^mstring;
```


### 9.6.6 String Arrays

String arrays are NxK matrices of strings. Here is a partial list of the functions for manipulating string arrays:

| \$1 | Vertical string array concatenation operator. |
| :---: | :---: |
| \$~ | Horizontal string array concatenation operator. |
| [ ] | Extract subarrays or individual strings from their corresponding array, or assign their values. |
| ' | Transpose operator. |
| . ' | Bookkeeping transpose operator. |
| declare | Initialize variables at compile time. |
| delete | Delete specified global symbols. |
| fgetsa | Read multiple lines of text from a file. |
| fgetsat | Reads multiple lines of text from a file, discarding newlines. |
| format | Define output format for matrices, string arrays, and strings. |
| fputs | Write strings to a file. |
| fputst | Write strings to a file, appending newlines. |
| let | Initialize matrices, strings, and string arrays. |
| loads | Load a string or string array file (.fst file). |
| lprint | Print expressions to the printer. |


| lshow | Print global symbol table to the printer. |
| :---: | :---: |
| print | Print expressions on window and/or auxiliary output. |
| reshape | Reshape a matrix or string array to new dimensions. |
| save | Save matrix, string array, string, procedure, function or keyword to disk and gives the disk file either a <br> .fmt, .fst or .fcg extension. |
| show | Display global symbol table. |
| sortcc | Quick-sort rows of matrix or string array based on character column. |
| type | Indicate whether variable passed as argument is matrix, string, or string array. |
| typecv | Indicate whether variables named in argument are strings, string arrays, matrices, procedures, functions or keywords. |
| varget | Access the global variable named by a string array. |
| varput | Assign the global variable named by a string array. |
| vec | Stack columns of a matrix or string array to form a column vector. |
| vecr | Stack rows of a matrix or string array to form a column vector. |

String arrays are created through the use of the string array concatenation operators. Below is a contrast of the horizontal string and horizontal string array concatenation operators. The statements:

```
x = "age";
y = "pay";
n = "sex";
s=x$+y$+n;
sa=x$~y$~n;
```

assign the values:

```
s = agepaysex
s = age pay sex
```


### 9.6.7 Character Matrices

Matrices can have either numeric or character elements. For convenience, a matrix containing character elements is referred to as a character matrix.

A character matrix is not a separate data type, but gives you the ability to store and manipulate data elements that are composed of ASCII characters as well as floating point numbers. For example, you may want to concatenate a column vector containing the names of the variables in an analysis onto a matrix containing the coefficients, standard errors, t -statistic, and p -value. You can then print out the entire matrix with a separate format for each column with one call to the function printfm.

The logic of the programs will dictate the type of data assigned to a matrix, and the increased flexibility allowed by being able to bundle both types of data together in a single matrix can be very powerful. You could, for instance, create a moment matrix from your data, concatenate a new row onto it containing the names of the variables and save it to disk with the save command.

Numeric matrices are double precision, which means that each element is stored in 8 bytes. A character matrix can thus have elements of up to 8 characters.

GAUSS does not automatically keep track of whether a matrix contains character or numeric information. The ASCII to GAUSS conversion program ATOG will record the types of variables in a data set when it creates it. The create command will, also. The function vartypef gets a vector of variable type information from a data set. This
vector of ones and zeros can be used by printfm when printing your data. Since GAUSS does not know whether a matrix has character or numeric information, it is up to you to specify which type of data it contains when printing the contents of the matrix. (For details, see print and printfm in the GAUSS LANGUAGE REFERENCE.)

Most functions that take a string argument will take an element of a character matrix also, interpreting it as a string of up to 8 characters.

### 9.6.8 Date and Time Formats

The DT scalar format is a double precision representation of the date and time with up to 14 digits. Each group of digits represents a different aspect of the date and time such as the year or month. Using characters, to represent each digit in a DT scalar number would look like this:

```
YYYYMODDHHSS
```

Starting from the left: the first four digits represent the year; the fifth and sixth digits, if present, represent the month; the seventh and eight digits, if present, represent the day; the ninth and tenth digits represent the hour; the eleventh and twelfth digits, if present, represent the minutes and finally, the thirteenth and fourteenth digits represent the seconds.

For example, in DT scalar format, the number:

```
20120723143207
```

represents $14: 32: 07$ or $2: 32: 07 \mathrm{PM}$ on July 23, 2012. It is important to remember that the leading digits will always be the year. This becomes relevant if the DT scalar number contains fewer than 14 digits to the right of the decimal point. For example, the number:

## 201302

would represent February 2013, rather than the time 20:13:02 (or 8:13:02 PM).

## DTV Vector Format

The DTV vector is a 1 x 8 vector. The format for the DTV vector is:
[1] Year
[2] Month, 1-12
[3] Day of month, 1-31
[4] Hour of day, 0-23
[5] Minute of hour, 0-59
[6]
Second of minute, 0-59
[7]
Day of week, $0-6$ where 0 is Sunday
[8]
Day since beginning of year, 0-365

## UTC Scalar Format

The UTC scalar format is the number of seconds since January 1, 1970, Greenwich Mean Time.

### 9.6.9 Special Data Types

The IEEE floating point format has many encodings that have special meaning. The print command will print them accurately so that you can tell if your calculation is producing meaningful results.

## NaN

There are many floating point encodings which do not correspond to a real number. These encodings are referred to as NaN's. NaN stands for Not A Number.

Certain numerical errors will cause the math coprocessor to create a NaN called an "indefinite." This will be printed as a -NaN when using the print command. These values are created by the following operations:

- $+\infty$ plus $-\infty$
- $+\infty$ minus $+\infty$
- $-\infty$ minus $-\infty$
- $0 * \infty$
- $\infty / \infty$
- $0 / 0$
- Operations where one or both operands is a NaN
- Trigonometric functions involving $\infty$


## INF

When the math coprocessor overflows, the result will be a properly signed infinity. Subsequent calculations will not deal well with an infinity; it usually signals an error in your program. The result of an operation involving an infinity is most often a NaN .

## DEN, UNN

When some math coprocessors underflow, they may do so gradually by shifting the significand of the number as necessary to keep the exponent in range. The result of this is a denormal (DEN). When denormals are used in calculations, they are usually handled automatically in an appropriate way. The result will either be an unnormal (UNN), which like the denormal represents a number very close to zero, or a normal, depending on how significant the effect of the denormal was in the calculation. In some cases the result will be a NaN .

Following are some procedures for dealing with these values. These procedures are not defined in the Run-Time Library. If you want to use them, you will need to define them yourself.

The procedure isindef will return 1 (true) if the matrix passed to it contains any NaN's that are the indefinite mentioned earlier. The GAUSS missing value code as well as GAUSS scalar error codes are NaN's, but this procedure tests only for indefinite:

```
proc isindef(x);
    retp(not x $/= __INDEFn);
endp;
```

Be sure to call gausset before calling isindef. gausset will initialize the value of the global $\qquad$ INDEFn to a platform-specific encoding.

The procedure normal will return a matrix with all denormals and unnormals set to zero.

```
proc normal(x);
    retp (x .* (abs (x) .> 4.19e-307));
endp;
```

```
proc isinf(x);
    local plus,minus;
    plus = __INFp;
    minus = __INFn;
    retp(not x /= plus or not x /= minus);
endp;
```

Be sure to call gausset before calling isinf. gausset will initialize the values of the globals __ INFn and __INFp to platform specific encodings.

### 9.7 Operator Precedence

The order in which an expression is evaluated is determined by the precedence of the operators involved and the order in which they are used. For example, the * and / operators have a higher precedence than the + and - operators. In expressions that contain
these operators, the operand pairs associated with the $*$ or / operator are evaluated first. Whether * or / is evaluated first depends on which comes first in the particular expression. For a listing of the precedence of all operators, see Operator Precedence, Section 10.7 .

The expression

```
-5+3/4+6*3
```

is evaluated as

$$
(-5)+(3 / 4)+(6 * 3)
$$

Within a term, operators of equal precedence are evaluated from left to right.
The term

```
2^3^7
```

is evaluated

$$
\left(2^{3}\right)^{7}
$$

In the expression

$$
f 1(x) * f 2(y)
$$

$f 1$ is evaluated before $f 2$. Here are some examples:

## Expression

$$
\begin{aligned}
& a+b^{*} c+d \\
& -2+4-6 * \operatorname{inv}(8) / 9
\end{aligned}
$$

## Evaluation

$$
\begin{aligned}
& (a+(b * c))+d \\
& ((-2)+4)-((6 * \operatorname{inv}(8)) / 9)
\end{aligned}
$$

| $3.14^{\wedge} 5^{*} 6 /(2+\operatorname{sqr} t(3) / 4)$ | $\left(\left(3.14^{5}\right) * 6\right) /(2+(\operatorname{sqrt}(3) / 4))$ |
| :--- | :--- |
| $-a+b^{*} c^{\wedge} 2$ | $(-a)+\left(b *\left(c^{2}\right)\right)$ |
| $a+b-c+d-e$ | $(((a+b)-c)+d)-e$ |
| $a^{\wedge} b^{\wedge} c^{*} d$ | $\left(\left(a^{b}\right)^{c}\right) * d$ |
| $a^{*} b / d^{*} c$ | $\left(\left(a a^{*} b\right) / d\right) * c$ |
| $a^{\wedge} b+c^{*} d$ | $\left(a^{b}\right)+(c * d)$ |
| $2^{\wedge} 4!$ | $2(4!)$ |
| $2 * 3!$ | $2 *(3!)$ |

### 9.8 Flow Control

A computer language needs facilities for decision making and looping to control the order in which computations are done. GAUSS has several kinds of flow control statements.

### 9.8.1 Looping

do loop
The do statement can be used in GAUSS to control looping.

```
do while
    scalar_expression; // loop if expression is true
.
.
statements
```

```
.
.
endo;
```

also

```
do until scalar_expression; // loop if expression is false
.
.
statements
.
endo;
```

The scalar_expression is any expression that returns a scalar result. The expression will be evaluated as TRUE if its real part is nonzero and FALSE if it is zero. There is no counter variable that is automatically incremented in a do loop. If one is used, it must be set to its initial value before the loop is entered and explicitly incremented or decremented inside the loop.

The following example illustrates nested do loops that use counter variables.

```
format /rdn 1,0;
space = " ";
comma = ",";
i = 1;
do while i <= 4;
    j = 1;
    do while j <= 3;
        print space i comma j;;
        j = j+1;
    endo;
    i = i+1;
    print;
endo;
```

This will print:

| 1,1 | 1,2 | 1,3 |
| :--- | :--- | :--- |
| 2,1 | 2,2 | 2,3 |
| 3,1 | 3,2 | 3,3 |
| 4,1 | 4,2 | 4,3 |

Use the relational and logical operators without the dot ' .' in the expression that controls a do loop. These operators always return a scalar result.
break and continue are used within do loops to control execution flow. When break is encountered, the program will jump to the statement following the endo. This terminates the loop. When continue is encountered, the program will jump up to the top of the loop and reevaluate the while or until expression. This allows you to reiterate the loop without executing any more of the statements inside the loop:

```
do until eof(fp); // continue jumps here
    x = packr (readr (fp,100));
    if scalmiss(x);
        continue; // iterate again
    endif;
    s = s + sumc(x);
    count = count + rows (x);
    if count >= 10000;
        break; // break out of loop
    endif;
endo;
mean = s / count; // break jumps here
```

```
for loop
```

The fastest looping construct in GAUSS is the for loop:

```
for counter ( start, stop, step );
.
•
    statements
.
```

```
.
endfor;
```

counter is the literal name of the counter variable. start, stop and step are scalar expressions. start is the initial value, stop is the final value and step is the increment.
break and continue are also supported by for loops. (For more information, see for in the GAUSS LANGUAGE REFERENCE.)

### 9.8.2 Conditional Branching

The if statement controls conditional branching:

```
    if scalar_expression;
        .
        statements
        .
    .
    elseif scalar_expression;
        .
        .
        statements
        •
    .
    else;
        .
        .
        statements
        .
        .
endif;
```

The scalar_expression is any expression that returns a scalar result. The expression will be evaluated as TRUE if its real part is nonzero and FALSE if it is zero.

GAUSS will test the expression after the if statement. If it is TRUE, then the first list of statements is executed. If it is FALSE, then GAUSS will move to the expression after the first elseif statement, if there is one, and test it. It will keep testing expressions and will execute the first list of statements that corresponds to a TRUE expression. If no expression is TRUE, then the list of statements following the else statement is executed. After the appropriate list of statements is executed, the program will go to the statement following the endif and continue on.

Use the relational and logical operators without the dot ' .' in the expression that controls an if orelseif statement. These operators always return a scalar result.
if statements can be nested.
One endif is required per if clause. If an else statement is used, there may be only one per if clause. There may be as many elseif's as are required. There need not be any elseif's or any else statement within an if clause.

### 9.8.3 Unconditional Branching

The goto and gosub statements control unconditional branching. The target of both a goto and a gosub is a label.

```
goto
```

A goto is an unconditional jump to a label with no return:

```
    label:
```

    goto label;
    Parameters can be passed with a goto. The number of parameters is limited by available stack space. This is helpful for common exit routines:

```
goto errout("Matrix singular");
    .
goto errout("File not found");
    .
errout:
pop errmsg;
errorlog errmsg;
end;
```

```
gosub
```

With a gosub, the address of the gosub statement is remembered and when a return statement is encountered, the program will resume executing at the statement following the gosub.

Parameters can be passed with a gosub in the same way as a goto. With a gosub it is also possible to return parameters with the return statement.

Subroutines are not isolated from the rest of your program and the variables referred to between the label and the return statement can be accessed from other places in your program.

Since a subroutine is only an address marked by a label, there can be subroutines inside of procedures. The variables used in these subroutines are the same variables that are known inside the procedure. They will not be unique to the subroutine, but they may be locals that are unique to the procedure that the subroutine is in. (For details, see gosub in the GAUSS LANGUAGE REFERENCE.)

### 9.9 Functions

Single line functions that return one item can be defined with the fn statement.

```
fn area(r) = pi * r * r;
```

These functions can be called in the same way as intrinsic functions. The above function could be used in the following program sequence.

```
diameter = 3;
radius = 3 / 2;
a = area(radius);
```


### 9.10 Rules of Syntax

This section lists the general rules of syntax for GAUSS programs.

### 9.10.1 Statements

A GAUSS program consists of a series of statements. A statement is a complete expression or command. Statements in GAUSS end with a semicolon with one exception: from the GAUSS command line, the final semicolon in an interactive program is implicit if it is not explicitly given:

```
(gauss) x=5; z=rndn (3,3); y=x+z
```

Column position is not significant. Blank lines are allowed. Inside a statement and outside of double quotes, the carriage return/line feed at the end of a physical line will be converted to a space character as the program is compiled.

A statement containing a quoted string can be continued across several lines with a backslash as follows.

```
s = "This is one really long string that would be \
    difficult to assign in just a single line.";
```


### 9.10.2 Case

GAUSS does not distinguish between uppercase and lowercase except inside double quotes.

### 9.10.3 Comments

```
// This comments out all text between the '//' and the end
// of the line
/* This kind of comment can be nested */
@ We consider this kind of comment to be obsolete, but it
is supported for backwards compatibility. We do, however,
recommend replacing them with one of the other types of
comments @
```


### 9.10.4 Extraneous Spaces

Extraneous spaces are significant in print and lprint statements where the space is a delimiter between expressions:

```
print x y z;
```

In print and lprint statements, spaces can be used in expressions that are in parentheses:

```
print (x * y) (x + y);
```


### 9.10.5 Symbol Names

The names of matrices, strings, procedures, and functions can be up to 32 characters long. The characters must be alphanumeric or an underscore. The first character must be alphabetic or an underscore.

### 9.10.6 Labels

A label is used as the target of a goto or a gosub. The rules for naming labels are the same as for matrices, strings, procedures, and functions. A label is followed immediately by a colon:

```
here:
```

The reference to a label does not use a colon:

```
goto here;
```


### 9.10.7 Assignment Statements

The assignment operator is the equal sign ' $=$ ':

$$
y=x+z
$$

Multiple assignments must be enclosed in braces ' $\}$ '. The statement:

```
mant,pow = base10(x);
```

is incorrect. It should be:

```
{ mant, pow } = base10(x);
```

The comparison operator (equal to) is two equal signs '==':

```
if x == y;
    print "x is equal to y";
endif;
```


### 9.10.8 Function Arguments

The arguments to functions are enclosed in parentheses ' ( ) ':

```
y = sqrt(x);
```


### 9.10.9 Indexing Matrices

Brackets ' [ ]' are used to index matrices:

```
x = { 1 2 3,
    375,
    3 7 4,
    8 5 5,
    6 1 8 };
y = x[3,3];
z = x[1 2:4,1 3];
```

Vectors can be indexed with either one or two indices:

```
v}=1\begin{array}{lllllllllll}{1}&{2}&{3}&{4}&{5}&{6}&{7}&{8}&{9}&{;}
k = v[3];
j = v[1,6:9];
```

$x[2,3]$ returns the element in the second row and the third column of $x$.
$\mathrm{x}\left[\begin{array}{llll}1 & 3 & 5,4 & 7\end{array}\right]$ returns the submatrix that is the intersection of rows 1,3 , and 5 and columns 4 and 7 .
$x[., 3]$ returns the third column of $x$.
$x[3: 5,$.$] returns the submatrix containing the third through the fifth rows of x$.
The indexing operator will take vector arguments for submatrix extraction or submatrix assignments:

```
y = x[rv,cv];
y[rv,cv] = x;
```

$r v$ and $C V$ can be any expressions returning vectors or matrices. The elements of $r v$ will be used as the row indices and the elements of $C V$ will be used as the column indices. If $r v$ is a scalar 0 , all rows will be used; if $C v$ is a scalar 0 , all columns will be used. If a vector is used in an index expression, it is illegal to use the space operator or the colon operator on the same side of the comma as the vector.

### 9.10.10 Arrays of Matrices and Strings

It is possible to index sets of matrices or strings using the varget function.
In this example, a set of matrix names is assigned to mvec. The name $y$ is indexed from mvec and passed to varget which will return the global matrix $y$. The returned matrix is inverted and assigned to $g$ :

```
mvec = { x y z a };
i = 2;
g = inv(varget(mvec[i]));
```

The following procedure can be used to index the matrices in mvec more directly:

```
proc
    imvec(i);
    retp(varget(mvec[i]));
endp;
```

Then imvec(i) will equal the matrix whose name is in the ith element of mvec.
In the example above, the procedure imvec() was written so that it always operates on the vector mvec. The following procedure makes it possible to pass in the vector of names being used:

```
proc
    get(array,i);
    retp(varget(array[i]));
endp;
```

Then get(mvec,3) will return the 3 rd matrix listed in mvec.

```
proc
    put(x,array,i);
    retp(varput(x,array[i]));
endp;
```

And put( $\mathrm{x}, \mathrm{mvec}, 3$ ) will assign x to the 3 rd matrix listed in mvec and return a 1 if successful or a 0 if it fails.

### 9.10.11 Arrays of Procedures

It is also possible to index procedures. The ampersand operator $(\varepsilon)$ is used to return a pointer to a procedure.

Assume that $\mathbf{f 1}, \mathbf{f 2}$, and $\mathbf{f} \mathbf{3}$ are procedures that take a single argument. The following code defines a procedure $f i$ that will return the value of the $i$ th procedure, evaluated at $x$.

```
nms = &f1 | &f2 | &f3;
proc fi(x,i);
    local f;
    f = nms[i];
    local f:proc;
    retp(f(x));
endp;
```

$\mathrm{fi}(\mathrm{x}, 2)$ will return $\mathrm{f} \mathbf{2 ( x )}$. The ampersand is used to return the pointers to the procedures. nms is a numeric vector that contains a set of pointers. The local statement is used twice. The first tells the compiler that $f$ is a local matrix. The $i$ th pointer, which is just a number, is assigned to $f$. Then the second local statement tells the compiler
to treat $f$ as a procedure from this point on; thus the subsequent statement $\mathbf{f}(\mathrm{x})$ is interpreted as a procedure call.

## 10 Operators

### 10.1 Element-by-Element Operators

Element-by-element operators share common rules of conformability. Some functions that have two arguments also operate according to the same rules.

Element-by-element operators handle those situations in which matrices are not conformable according to standard rules of matrix algebra. When a matrix is said to be ExE conformable, it refers to this element-by-element conformability. The following cases are supported:

| matrix | op | matrix |
| :---: | :---: | :---: |
| matrix | op | scalar |
| scalar | op | matrix |
| matrix | op | vector |
| vector | op | matrix |
| vector | op | vector |

In a typical expression involving an element-by-element operator

$$
z=x+y ;
$$

conformability is defined as follows:

- If $x$ and $y$ are the same size, the operations are carried out corresponding element by corresponding element:

```
132
x = 4 5 1
    374
    2 4 3
y = 3 1 4
    6 1 2
    376
z=765
    9 8 6
```

- If $x$ is a matrix and $y$ is a scalar, or vice versa, then the scalar is operated on with respect to every element in the matrix. For example, $x+2$ will add 2 to every element of $x$ :

```
    1 3 2
x = 4 5 1
    3 4
y = 2
    3 5 
z=673
    596
```

- If $x$ is an Nx1 column vector and $y$ is an NxK matrix, or vice versa, the vector is swept "across" the matrix:

| vector |  | matrix |  |  |  | result |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $\rightarrow$ | 2 | 4 | 3 |  | 3 | 5 | 4 |
| 4 | $\rightarrow$ | 3 | 1 | 4 | = | 7 | 5 | 8 |
| 3 | $\rightarrow$ | 6 | 1 | 2 |  | 9 | 4 | 5 |

- If $x$ is an $1 x K$ column vector and $y$ is an NxK matrix, or vice versa, then the vector is swept "down" the matrix:

```
vector 2 4 3
Matrix 7 2 4
        3 0 1
        5 3 2
        \downarrow \downarrow \downarrow
result 9 6 7
        5 4 4
        7 7 5
```

- When one argument is a row vector and the other is a column vector, the result of an element-by-element operation will be the "table" of the two:

| row vector |  | 2 | 4 | 3 | 1 |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  | $\downarrow$ | $\downarrow$ | $\downarrow$ | $\downarrow$ |
|  | 3 | $\rightarrow$ | 5 | 7 | 6 | 4 |
| column vector | $\rightarrow$ | 4 | 6 | 5 | 3 |  |
|  | 5 | $\rightarrow$ | 7 | 9 | 8 | 6 |

If $x$ and $y$ are such that none of these conditions apply, the matrices are not conformable to these operations and an error message will be generated.

### 10.2 Matrix Operators

The following operators work on matrices. Some assume numeric data and others will work on either character or numeric data.

### 10.2.1 Numeric Operators

For details on how matrix conformability is defined for element-by-element operators, see Element-by-Element Operators, Section 10.1 .

+ Addition:

$$
y=x+z ;
$$

Performs element-by-element addition.

- Subtraction or negation:

$$
\begin{aligned}
& y=x-z ; \\
& y=-k ;
\end{aligned}
$$

Performs element-by-element subtraction or the negation of all elements, depending on context. *Matrix multiplication or multiplication:

$$
y=x * z
$$

When $z$ has the same number of rows as $x$ has columns, this will perform matrix multiplication (inner product). If $x$ or $z$ are scalar, this performs standard element-by-element multiplication.
/Division or linear equation solution:

$$
\mathrm{x}=\mathrm{b} / \mathrm{A} ;
$$

If $A$ and $b$ are scalars, this performs standard division. If one of the operands is a matrix and the other is scalar, the result is a matrix the same size with the results of the divisions between the scalar and the corresponding elements of the matrix. Use . / for element-by-element division of matrices.

If $b$ and $A$ are conformable, this operator solves the linear matrix equation:

$$
A x=b
$$

Linear equation solution is performed in the following cases:

- If $A$ is a square matrix and has the same number of rows as $b$, this statement will solve the system of linear equations using an LU decomposition.
- If A is rectangular with the same number of rows as b , this statement will produce the least squares solutions by forming the normal equations and using the Cholesky decomposition to get the solution:

$$
x=\frac{A^{\prime} b}{A^{\prime} A}
$$

If trap 2 is set, missing values will be handled with pairwise deletion.
-Modulo division

```
y = x % z;
```

For integers, this returns the integer value that is the remainder of the integer division of $x$ by $z$. If $x$ or $z$ is noninteger, it will first be rounded to the nearest integer. This is an element-by-element operator.
!Factorial

```
y = x!;
```

Computes the factorial of every element in the matrix $x$. Nonintegers are rounded to the nearest integer before the factorial operator is applied. This will not work with complex matrices. If $x$ is complex, a fatal error will be generated.

## . * Element-by-element multiplication

$$
y=x \cdot * z ;
$$

If $x$ is a column vector, and $z$ is a row vector (or vice versa), the "outer product" or "table" of the two will be computed. (For comformability rules, see Element-by-Element Operators, Section 10.1 .)
. / Element-by-element division

$$
y=x . / z ;
$$

${ }^{\wedge}$ Element-by-element exponentiation

$$
y=x^{\wedge} z ;
$$

If $x$ is negative, $z$ must be an integer.
. ^ Same as ${ }^{\wedge}$
. * . Kronecker (tensor) product:

$$
y=x \cdot * \cdot z ;
$$

This results in a matrix in which every element in $x$ has been multiplied (scalar multiplication) by the matrix $z$. For example:

```
x = { 1 2,
    3 4 };
    z={4 5 6,
    7 8 9 };
y = x .*. z;
\(y=\)\begin{tabular}{rrrrrr}
4 & 5 & 6 & 8 & 10 & 12 \\
7 & 8 & 9 & 14 & 16 & 18 \\
12 & 15 & 18 & 16 & 20 & 24 \\
21 & 24 & 27 & 28 & 32 & 36
\end{tabular}
```

* $\sim$ Horizontal direct product:

$$
\begin{array}{ll}
x= & 2 \\
3 & 4
\end{array}
$$

```
y = 5 6
    7
z = x *~ y;
z=5 6 10 12
    2124 28 32
```

The input matrices $x$ and $y$ must have the same number of rows. The result will have $\operatorname{cols}(x) * \operatorname{cols}(y)$ columns.

### 10.2.2 Other Matrix Operators

' Transpose operator:

$$
y=x^{\prime} ;
$$

The columns of $y$ will contain the same values as the rows of $x$ and the rows of $y$ will contain the same values as the columns of $x$. For complex matrices this computes the complex conjugate transpose.

If an operand immediately follows the transpose operator, the ' will be interpreted as
$\prime *$. Thus $y=x^{\prime} x$ is equivalent to $y=x^{\prime} *_{x}$.
. ' Bookkeeping transpose operator:

$$
y=x . ' ;
$$

This is provided primarily as a matrix handling tool for complex matrices. For all matrices, the columns of $y$ will contain the same values as the rows of $x$ and the rows of $y$ will contain the same values as the columns of $x$. The complex conjugate transpose is NOT computed when you use . '.

If an operand immediately follows the bookkeeping transpose operator, the . ' will be interpreted as.$\quad{ }^{\prime *}$. Thus $y=x . ' x$ is equivalent to $y=x .{ }^{\prime *} x$.
| Vertical concatenation:

```
z = x | y;
x = 1 2 3
        4 6
y=7 8 9
z = x | y;
\(z=\)\begin{tabular}{lll}
1 & 2 & 3 \\
4 & 5 & 6 \\
7 & 8 & 9
\end{tabular}
```


### 10.3 Relational Operators

For details on how matrix conformability is defined for element-by-element operators, see Element-by-Element Operators, Section 10.1 .

Each of these operators has two equivalent representations. Either can be used (for example, < or $l t$ ), depending only upon preference. The alphabetic form should be surrounded by spaces.

A third form of these operators has a ' $\$$ ' and is used for comparisons between character data and for comparisons between strings or string arrays. The comparisons are done byte by byte starting with the lowest addressed byte of the elements being compared.

The equality comparison operators ( $<=,==,>=, /=,!=$ ) and their dot equivalents can be used to test for missing values and the NaN that is created by floating point exceptions. Less than and greater than comparisons are not meaningful with missings or NaN's, but equal and not equal are valid. These operators are sign-insensitive for missings, NaN 's, and zeros.

The string ' $\$$ ' versions of these operators can also be used to test missings, NaN's and zeros. Because they do a strict byte-to-byte comparison, they are sensitive to the sign
bit. Missings, NaN's, and zeros can all have the sign bit set to 0 or 1 , depending on how they were generated and have been used in a program.

If the relational operator is NOT preceded by a dot ' .', then the result is always a scalar 1 or 0 , based upon a comparison of all elements of $x$ and $y$. All comparisons must be true for the relational operator to return TRUE.

By this definition, then:

```
if x /= y;
```

is interpreted as: "if every element of $x$ is not equal to the corresponding element of $y$ ". To check if two matrices are not identical, use

```
if not x == y;
```

For complex matrices, the $==, /=, .==$ and.$/=$ operators compare both the real and imaginary parts of the matrices; all other relational operators compare only the real parts.

- Less than

$$
\begin{aligned}
& \mathrm{z}=\mathrm{x}<\mathrm{y} ; \\
& \mathrm{z}=\mathrm{x} l \mathrm{l} y ; \\
& \mathrm{z}=\mathrm{x} \$ \mathrm{y} ;
\end{aligned}
$$

- Less than or equal to

```
z = x <= y;
z = x le y;
z = x $<= y;
```

- Equal to

```
z = x == y;
z = x eq y;
z = x $== y;
```

- Not equal

$$
\begin{aligned}
& \mathrm{z}=\mathrm{x} /=\mathrm{y} ; \\
& \mathrm{z}=\mathrm{x} \text { ne } \mathrm{y} ; \\
& \mathrm{z}=\mathrm{x}!=\mathrm{y} ; \\
& \mathrm{z}=\mathrm{x} \$ /=\mathrm{y} ; \\
& \mathrm{z}=\mathrm{x} \$!=\mathrm{y} ;
\end{aligned}
$$

- Greater than or equal to

$$
\begin{aligned}
& z=x>=y ; \\
& z=x \text { ge } y ; \\
& z=x \$>=y ;
\end{aligned}
$$

- Greater than

$$
\begin{aligned}
& z=x>y ; \\
& z=x g t y ; \\
& z=x \$>y ;
\end{aligned}
$$

If the relational operator IS preceded by a dot '.', then the result will be a matrix of 1 's and 0 's, based upon an element-by-element comparison of $x$ and $y$.

- Element-by-element less than

$$
\begin{aligned}
& z=x .<y ; \\
& z=x \cdot l t y ; \\
& z=x . S<y ;
\end{aligned}
$$

- Element-by-element less than or equal to

$$
\begin{aligned}
& z=x \cdot<=y ; \\
& z=x \cdot l e y ; \\
& z=x . \$<=y ;
\end{aligned}
$$

- Element-by-element equal to

$$
\begin{aligned}
& z=x .==y ; \\
& z=x . e q y ; \\
& z=x . \$==y ;
\end{aligned}
$$

- Element-by-element not equal to

$$
\begin{aligned}
& \mathrm{z}=\mathrm{x} \cdot /=\mathrm{y} ; \\
& \mathrm{z}=\mathrm{x} \cdot \mathrm{ne} \mathrm{y} ; \\
& \mathrm{z}=\mathrm{x} .!=\mathrm{y} ; \\
& \mathrm{z}=\mathrm{x} . \$ /=\mathrm{y} ; \\
& \mathrm{z}=\mathrm{x} . \$!=\mathrm{y} ;
\end{aligned}
$$

- Element-by-element greater than or equal to

```
z = x .>= y;
z = x .ge y;
z = x .$>= y;
```

- Element-by-element greater than

```
z = x .> y;
z = x .gt y;
z = x .$> y;
```


### 10.4 Logical Operators

The logical operators perform logical or Boolean operations on numeric values. On input a nonzero value is considered TRUE and a zero value is considered FALSE. The logical operators return a 1 if TRUE and a 0 if FALSE. Decisions are based on the following truth tables:

| Complement |  |  |
| :---: | ---: | :---: |
| $\mathbf{x}$ | not $x$ |  |
| T | F |  |
| F | T |  |


| Conjunction |  |  |
| :---: | :---: | :---: |
| $\mathbf{x}$ | $y \quad x$ and $y$ |  |
| T | T | T |
| T | F | F |
| F | T | F |
| F | F | F |
| Disjunction |  |  |
| x |  | $x$ or $y$ |
| T | T | T |
| T | F | T |
| F | T | T |
| F | F | F |
| Exclusive Or |  |  |
|  |  | $x$ xor $y$ |
| T | T | F |
| T | F | T |
| F | T | T |
| F | F | F |
| Equivalence |  |  |
| $\mathbf{x}$ |  | $x$ eqv $y$ |
| T | T | T |
| T | F | F |
| F | T | F |
| F | F | T |

For complex matrices, the logical operators consider only the real part of the matrices. The following operators require scalar arguments. These are the ones to use in if and do statements:

- Complement

$$
\mathrm{z}=\operatorname{not} \mathrm{x}
$$

- Conjunction

$$
z=x \text { and } y ;
$$

- Disjunction

$$
z=x \text { or } y
$$

- Exclusive or

```
z = x xor y;
```

- Equivalence

$$
z=x \text { eqv } y ;
$$

If the logical operator is preceded by a dot '. ', the result will be a matrix of 1's and 0's based upon an element-by-element logical comparison of $x$ and $y$ :

- Element-by-element logical complement

```
z = .not x;
```

- Element-by-element conjunction

```
z = x .and y;
```

- Element-by-element disjunction

$$
z=x \text {.or } y
$$

- Element-by-element exclusive or

$$
z=x . x o r y ;
$$

- Element-by-element equivalence

$$
z=x \cdot e q v y ;
$$

### 10.5 Other Operators

## Assignment Operator

Assignments are done with one equal sign:

```
y = 3;
```


## Comma

Commas are used to delimit lists:

```
clear x,y,z;
```

to separate row indices from column indices within brackets:

$$
y=x[3,5]
$$

and to separate arguments of functions within parentheses:

```
y = momentd(x,d);
```


## Period

Dots are used in brackets to signify "all rows" or "all columns":

$$
y=x[., 5] ;
$$

## Space

Spaces are used inside of index brackets to separate indices:

$$
y=x\left[\begin{array}{llll}
1 & 3 & 5,3 & 5
\end{array}\right] ;
$$

No extraneous spaces are allowed immediately before or after the comma, or immediately after the left bracket or before the right bracket.

Spaces are also used in print and lprint statements to separate the separate expressions to be printed:

```
print x/2 2*sqrt(x);
```

No extraneous spaces are allowed within expressions in print or lprint statements unless the expression is enclosed in parentheses:

```
print (x / 2) (2 * sqrt(x));
```


## Colon

A colon is used within brackets to create a continuous range of indices:

$$
y=x[1: 5, .] ;
$$

## Ampersand

The ( $\varepsilon$ ) ampersand operator will return a pointer to a procedure (proc), function (fn), or structure (struct). It is used when passing procedures or functions to other functions, when indexing procedures, and when initializing structure pointers. (For more information, see Indexing Procedures, Section 11.5 or Structure Pointers, Section 16.2 .)

## String Concatenation

```
x = "dog";
y = "cat";
z = x $+ y;
print z;
dogcat
```

If the first argument is of type string, the result will be of type string. If the first argument is of type matrix, the result will be of type matrix. Here are some examples:

```
y = 0 $+ "caterpillar";
```

The result will be a 1 x 1 matrix containing 'caterpil'.

```
y = zeros (3,1) $+ "cat";
```

The result will be a $3 \times 1$ matrix, each element containing 'cat'.
If we use the $y$ created above in the following:

```
k = y $+ "fish";
```

The result will be a $3 \times 1$ matrix with each element containing 'catfish'.
If we then use $k$ created above:

```
t = "" $+ k[1,1];
```

The result will be a string containing 'catfish'.
If we used the same $k$ to create $z$ as follows:

```
```

z = "dog" \$+ k[1,1];

```
```

```
```

z = "dog" \$+ k[1,1];

```
```

The resulting $\quad z$ will be a string containing 'dogcatfish'.

## String Array Concatenation

\$| Vertical string array concatenation

```
x = "dog";
y = "fish";
k = x $| y;
print k;
    dog
    fish
```

\$~ Horizontal string array concatenation

```
x = "dog";
y = "fish";
k = x $~ y;
print k;
    dog fish
```


## String Variable Substitution

In a command like the following:

```
create f1 = olsdat with x,4,2;
```

by default GAUSS will interpret olsdat as the literal name of the GAUSS data file you want to create. It will also interpret $x$ as the literal prefix string for the variable names x1 x2 x3 x4.

To get the data set name from a string variable, the substitution operator $(\wedge)$ could be used as follows:

```
dataset = "olsdat";
create f1 = ^dataset with x,4,2;
```

To get the data set name from a string variable and the variable names from a character vector, use the following:

```
dataset = "olsdat";
vnames = { age, pay, sex };
create f1 = ^dataset with ^vvames,0,2;
```

The general syntax is:

```
^variable_name
```

Expressions are not allowed.
The following commands are currently supported with the substitution operator ( $\wedge$ ) in the current version.

```
create f1 = ^dataset with ^^vnames,0,2;
create f1 = ^dataset using ^cmdfile;
open f1 = ^dataset;
output file = ^outfile;
load x = ^datafile;
load path = ^lpath x,y,z,t,w;
loadexe buf = ^exefile;
save ^name = x;
save path = ^spath;
dos ^cmdstr;
run ^prog;
msym ^mstring;
```


### 10.6 Using Dot Operators with Constants

When you use those operators preceded by a '.' (dot operators) with a scalar integer constant, insert a space between the constant and any following dot operator. Otherwise, the dot will be interpreted as part of the scalar; that is, the decimal point. For example:

```
let }y=123
x = 2.<y;
```

will return $x$ as a scalar 0 , not a vector of 0 's and 1 's, because

$$
x=2 .<y
$$

is interpreted as

$$
x=2 .<y
$$

and not as

```
x = 2 .< y;
```

Be careful when using the dot relational operators (. $<, .<=, .==, . /=, .>, .>=$ ). The same problem can occur with other dot operators, also. For example:

```
let x = 1 1 1;
y = x./2./x;
```

will return $y$ as a scalar .5 rather than a vector of .5 's, because

$$
y=x . / 2 . / x ;
$$

is interpreted as

$$
y=(x . / 2 .) / x ;
$$

not

$$
y=(x . / 2) . / x ;
$$

The second division, then, is handled as a matrix division rather than an element-by-element division.

### 10.7 Operator Precedence

The order in which an expression is evaluated is determined by the precedence of the operators involved and the order in which they are used. For example, the * and / operators have a higher precedence than the + and - operators. In expressions that contain the above operators, the operand pairs associated with the * or / operator are evaluated first. Whether * or / is evaluated first depends on which comes first in the particular expression.

The expression

$$
-5+3 / 4+6 * 3
$$

is evaluated as

$$
(-5)+(3 / 4)+(6 * 3)
$$

Within a term, operators of equal precedence are evaluated from left to right. The precedence of all operators, from the highest to the lowest, is listed in the table below. PLEASE NOTE: The transpose operator is listed with a precedence of 90. This applies for the transpose operation only. It does NOT apply for the expression:

```
X'X
```

Which is shorthand for:

```
X'*X
```

For a compound statement such as:

$$
\mathrm{Z}=\left(\mathrm{X}^{\prime} \mathrm{X}\right) /\left(\mathrm{Y}^{\prime} \mathrm{X}\right) ;
$$

the parentheses are required.

|  | Operator | Precedence | Operator | Precedence | Operator | Precedence |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | . ' | 90 | . $\$>=$ | 65 | \$ $>=$ | 55 |
|  | $t$ | 90 | . $/=$ | 65 | /= | 55 |
|  | ! | 89 | . $<$ | 65 | $<$ | 55 |
|  | . ${ }^{\wedge}$ | 85 | . $<=$ | 65 | $<=$ | 55 |
|  | $\wedge$ | 85 | $==$ | 65 | = | 55 |
|  | (unary -) | 83 | . > | 65 | $>$ | 55 |
|  | * | 80 | . $>=$ | 65 | $>=$ | 55 |
|  | * | 80 | . eq | 65 | eq | 55 |
|  | . * | 80 | . 9 e | 65 | ge | 55 |
|  | . * | 80 | . $9 t$ | 65 | $g t$ | 55 |
|  | . $/$ | 80 | . Ie | 65 | le | 55 |
|  | / | 80 | . It | 65 | $1 t$ | 55 |


| 응 | 75 | . ne | 65 | ne | 55 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| \$+ | 70 | . not | 64 | not | 49 |
| + | 70 | . and | 63 | and | 48 |
| - | 70 | . or | 62 | Or | 47 |
| $\sim$ | 68 | . xor | 61 | xor | 46 |
| \| | 67 | . eqv | 60 | eqv | 45 |
| . $\$ 1=$ | 65 | \$/= | 55 | (space) | 35 |
| . $\$<$ | 65 | \$< | 55 | : | 35 |
| . $\$<=$ | 65 | \$<= | 55 | $=$ | 10 |
| . $\$==$ | 65 | S $=$ | 55 |  |  |
| . \$> | 65 | \$> | 55 |  |  |

## 11 Procedures and Keywords

Procedures are multiple-line, recursive functions that can have either local or global variables. Procedures allow a large computing task to be written as a collection of smaller tasks. These smaller tasks are easier to work with and keep the details of their operation from the other parts of the program that do not need to know them. This makes programs easier to understand and easier to maintain.

A procedure in GAUSS is basically a user-defined function that can be used as if it were an intrinsic part of the language. A procedure can be as small and simple or as large and complicated as necessary to perform a particular task. Procedures allow you to build on your previous work and on the work of others rather than starting over again and again to perform related tasks.

Any intrinsic command or function may be used in a procedure, as well as any userdefined function or other procedure. Procedures can refer to any global variable; that is, any variable in the global symbol table that can be shown with the show command. It is also possible to declare local variables within a procedure. These variables are known only inside the procedure they are defined in and cannot be accessed from other procedures or from the main level program code.

All labels and subroutines inside a procedure are local to that procedure and will not be confused with labels of the same name in other procedures.

### 11.1 Defining a Procedure

A procedure definition consists of five parts, four of which are denoted by explicit GAUSS commands:

## 1. Procedure declaration

2. Local variable declaration
3. Body of procedure
4. Return from procedure
5. End of procedure definition
proc statement
local statement
retp statement
endp statement

There is always one proc statement and one endp statement in a procedure definition. Any statements that come between these two statements are part of the procedure. Procedure definitions cannot be nested. local and retp statements are optional. There can be multiple local and retp statements in a procedure definition. Here is an example:

```
proc (3) = regress(x, y);
    local xxi,b,ymxb,sse,sd,t;
    xxi = invpd(x'x);
    b = xxi * (x'y);
    ymxb = y-xb;
    sse = ymxb'ymxb/(rows (x)-cols(x));
    sd = sqrt(diag(sse*xxi));
    t = b./sd;
    retp (b,sd,t);
endp;
```

This could be used as a function that takes two matrix arguments and returns three matrices as a result. For example: is:

```
{ b,sd,t } = regress(x,y);
```

Following is a discussion of the five parts of a procedure definition.

### 11.1.1 Procedure Declaration

The proc statement is the procedure declaration statement. The format is:

```
proc (rets) = name(arg1, arg2,...argn);
```

rets Optional constant, number of values returned by the procedure. Acceptable values here are 0-1023; the default is 1.
name Name of the procedure, up to 32 alphanumeric characters or an underscore, beginning with an alpha or an underscore.
arg\# Names that will be used inside the procedure for the arguments that are passed to the procedure when it is called. There can be 0-1023 arguments. These names will be known only in the procedure being defined. Other procedures can use the same names, but they will be separate entities.

### 11.1.2 Local Variable Declarations

The local statement is used to declare local variables. Local variables are variables known only to the procedure being defined. The names used in the argument list of the proc statement are always local. The format of the local statement is:

```
local x, y, f:proc, g:fn, z, h:keyword;
```

Local variables can be matrices or strings. If :proc, : fn, or : keyword follows the variable name in the local statement, the compiler will treat the symbol as if it were a procedure, function, or keyword respectively. This allows passing procedures, functions, and keywords to other procedures. (For more information, see Passing Procedures to Procedures, Section 11.4.)

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Variables that are global to the system (that is, variables listed in the global symbol table that can be shown with the show command) can be accessed by any procedure without any redundant declaration inside the procedure. If you want to create variables known only to the procedure being defined, the names of these local variables must be listed in a local statement. Once a variable name is encountered in a local statement, further references to that name inside the procedure will be to the local rather than to a global having the same name. (See clearg, varget, and varput in the GAUSS LANGUAGE REFERENCE for ways of accessing globals from within procedures that have locals with the same name.)

The local statement does not initialize (set to a value) the local variables. If they are not passed in as parameters, they must be assigned some value before they are accessed or the program will terminate with a Variable not initialized error message.

All local and global variables are dynamically allocated and sized automatically during execution. Local variables, including those that were passed as parameters, can change in size during the execution of the procedure.

Local variables exist only when the procedure is executing and then disappear. Local variables cannot be listed with the show command.

The maximum number of locals is limited by stack space and the size of workspace memory. The limiting factor applies to the total number of active local symbols at any one time during execution. If cat has 10 locals and it calls dog which has 20 locals, there are 30 active locals whenever cat is called.

There can be multiple local statements in a procedure. They will affect only the code in the procedure that follows. Therefore, for example, it is possible to refer to a global $x$ in a procedure and follow that with a local statement that declares a local x. All subsequent references to $x$ would be to the local $x$. (This is not good programming practice, but it demonstrates the principle that the local statement affects only the code that is physically below it in the procedure definition.) Another example is a symbol that is declared as a local and then declared as a local procedure or function later in the same procedure definition. This allows doing arithmetic on local function pointers before calling them. (For more information, see Indexing Procedures, Section 11.5 .)

### 11.1.3 Body of Procedure

The body of the procedure can have any GAUSS statements necessary to perform the task the procedure is being written for. Other user-defined functions and other procedures can be referenced as well as any global matrices and strings.

GAUSS procedures are recursive, so the procedure can call itself as long as there is logic in the procedure to prevent an infinite recursion. The process would otherwise terminate with either an Insufficient workspace memory message or a Procedure calls too deep message, depending on the space necessary to store the locals for each separate invocation of the procedure.

### 11.1.4 Returning from the Procedure

The return from the procedure is accomplished with the retp statement:

```
retp;
retp(expression1, expression2, arg1, arg2, argN,
    expressionN);
```

The retp statement can have multiple arguments. The number of items returned must coincide with the number of rets in the proc statement.

If the procedure was defined with no items returned, the retp statement is optional. The endp statement that ends the procedure will generate an implicit retp with no objects returned. If the procedure returns one or more objects, there must be an explicit retp statement.

There can be multiple retp statements in a procedure, and they can be anywhere inside the body of the procedure.

### 11.1.5 End of Procedure Definition

The endp statement marks the end of the procedure definition:

```
endp;
```

An implicit retp statement that returns nothing is always generated here so it is impossible to run off the end of a procedure without returning. If the procedure was defined to return one or more objects, executing this implicit return will result in a Wrong number of returns error message and the program will terminate.

### 11.2 Calling a Procedure

Procedures are called like this:

```
dog(i, j, k); // no returns
y = cat(i, j, k); // one return
{x, y, z } = bat(i, j, k); // multiple returns
call bat(i, j, k); // ignore any returns
```

Procedures are called in the same way that intrinsic functions are called. The procedure name is followed by a list of arguments in parentheses. The arguments must be separated by commas.

If there is to be no return value, use

```
proc (0) = dog(x, y ,z);
```

when defining the procedure and use

```
dog(ak, 4, 3);
```

or

```
call
dog(ak, 4, 3);
```

when calling it.

The arguments passed to procedures can be complicated expressions involving calls to other functions and procedures. This calling mechanism is completely general. For example,

```
y = dog(cat(3*x, bird(x, y))-2, 2, 1);
```

is legal.

### 11.3 Keywords

A keyword, like a procedure, is a subroutine that can be called interactively or from within a GAUSS program. A keyword differs from a procedure in that a keyword accepts exactly one string argument, and returns nothing. Keywords can perform many tasks not as easily accomplished with procedures.

### 11.3.1 Defining a Keyword

A keyword definition is much like a procedure definition. Keywords always are defined with 0 returns and 1 argument. The beginning of a keyword definition is the keyword statement:

```
keyword
name(strarg);
```

| name | Name of the keyword, up to 32 alphanumeric characters or an <br> underscore, beginning with an alpha or an underscore. |
| :--- | :--- |
| strarg | Name that will be used inside of the keyword for the <br> argument that is passed to the keyword when it is called. |
| There is always one argument. The name is known only in |  |
| the keyword being defined. Other keywords can use the same |  |
| name, but they will be separate entities. This will always be a |  |
| string. If the keyword is called with no characters following |  |

The rest of the keyword definition is the same as a procedure definition. (For more information, see Defining a Procedure, Section 11.1. Keywords always return nothing. Any retp statements, if used, should be empty. For example:

```
keyword
    add(s);
    local tok, sum;
    if s $== "";
        print "The argument is a null string";
        retp;
    endif;
    print "The argument is: '" s "'";
    sum = 0;
    do until s $== "";
        { tok, s } = token(s);
            sum = sum + stof(tok);
    endo;
    format /rd 1,2;
    print "The sum is: " sum;
endp;
```

The keyword defined above will print the string argument passed to it. The argument will be printed enclosed in single quotes.

### 11.3.2 Calling a Keyword

When a keyword is called, every character up to the end of the statement, excluding the leading spaces, is passed to the keyword as one string argument. For example, if you type

```
add 1 2 3 4 5;
```

the keyword will respond

```
The sum is: 15.00
```

Here is another example:

```
add;
```

the keyword will respond

```
The argument is a null string
```


### 11.4 Passing Procedures to Procedures

Procedures and functions can be passed to procedures in the following way:

```
proc max (x,y); // procedure to return maximum
    if x>y;
        retp(x);
    else;
        retp(y);
    endif;
endp;
proc min(x,y); // procedure to return minimum
    if x<y;
        retp(x);
    else;
        retp(y);
    endif;
endp;
fn lgsqrt(x) = ln(sqrt(x)); /* function to return
    log of square root */
proc myproc(&f1, &f2, x, y);
    local f1:proc, f2:fn, z;
    z = f1 (x, y);
    retp(f2(z));
endp;
```

The procedure myproc takes four arguments. The first is a procedure $\mathbf{f 1}$ that has two arguments. The second is a function $\mathbf{f} 2$ that has one argument. It also has two other arguments that must be matrices or scalars. In the local statement, $\mathbf{f 1}$ is declared to be a procedure and $\mathbf{f} \mathbf{2}$ is declared to be a function. They can be used inside the procedure in the usual way. $\mathbf{f 1}$ will be interpreted as a procedure inside myproc, and $\mathbf{f} \mathbf{2}$ will be interpreted as a function. The call to myproc is made as follows:

```
k = myproc(&max, &lgsqrt, 5, 7); // log of square root of 7
k = myproc(&min, &lgsqrt, 5, 7); // log of square root of 5
```

The ampersand $(\boldsymbol{\varepsilon})$ in front of the function or procedure name in the call to myproc causes a pointer to the function or procedure to be passed. No argument list should follow the name when it is preceded by the ampersand.

Inside myproc, the symbol that is declared as a procedure in the local statement is assumed to contain a pointer to a procedure. It can be called exactly like a procedure is called. It cannot be save'd but it can be passed on to another procedure. If it is to be passed on to another procedure, use the ampersand in the same way.

### 11.5 Indexing Procedures

 defined. A $1 \times 5$ vector procvec is defined by horizontally concatenating pointers to these procedures. A new procedure, $\boldsymbol{g}(x, i)$ is then defined to return the value of the $i$ th procedure evaluated at $x$ :

```
procVec = &f1 ~ &f2 ~ &f3 ~ &f4 ~ &f5;
proc g(x, i);
    local f;
    f = procVec[i];
    local f:proc;
    retp(f(x));
endp;
```

The local statement is used twice. The first time, $f$ is declared to be a local matrix. After $f$ has been set equal to the $i$ th pointer, $\mathbf{f}$ is declared to be a procedure and is called as a procedure in the retp statement.

### 11.6 Multiple Returns from Procedures

Procedures can return multiple items, up to 1023. The procedure is defined like this example of a complex inverse:

```
proc (2) = cminv(xr,xi); /* (2) specifies number of
    return values */
    local ixy, zr, zi;
    ixy = inv(xr)*xi;
    zr = inv(xr+xi*ixy); //real part of inverse
    zi = -ixy*zr; //imaginary part of inverse
    retp(zr, zi); //return: real part, imaginary part
endp;
```

It can then be called like this:

```
{ zr, zi } = cminv(xr, xi);
```

To make the assignment, the list of targets must be enclosed in braces.
Also, a procedure that returns more than one argument can be used as input to another procedure or function that takes more than one argument:

```
proc (2) = cminv(xr, xi);
    local ixy, zr, zi;
    ixy = inv(xr)*xi;
    zr = inv(xr+xi*ixy); //real part of inverse
    zi = -ixy*zr; //imaginary part of inverse
retp(zr, zi);
endp;
proc (2) = cmmult(xr, xi, yr, yi);
```

```
        local zr,zi;
        zr = xr*yr-xi*yi;
        zi = xr*yi+xi*yr;
        retp(zr, zi);
endp;
{ zr, zi } = cminv(cmmult(xr, xi, yr, yi));
```

The two returned matrices from cmmult() are passed directly to $\mathbf{c m i n v}()$ in the statement above. This is equivalent to the following statements:

```
{ tr, ti } = cmmult(xr, xi, yr, yi);
{ zr, zi } = cminv(tr, ti);
```

This is completely general so the following program is legal:

```
proc (2) = cmcplx(x);
    local r,c;
    r = rows(x);
    c = cols(x);
    retp(x, zeros(r,c));
endp;
proc (2) = cminv(xr,xi);
    local ixy, zr, zi;
    ixy = inv(xr)*xi;
    zr = inv(xr+xi*ixy); //real part of inverse
    zi = -ixy*zr; //imaginary part of inverse
retp(zr,zi);
endp;
proc (2) = cmmult(xr, xi, yr, yi);
    local zr, zi;
    zr = xr*yr-xi*yi;
    zi = xr*yi+xi*yr;
    retp(zr, zi);
endp;
```

```
{ xr, xi } = cmcplx(rndn (3,3));
{ yr, yi } = cmcplx(rndn (3,3));
{ zr, zi } = cmmult(cminv(xr, xi), cminv(yr, yi));
{ qr, qi } = cmmult(yr, yi, cminv(yr, yi));
{ wr, wi } = cmmult(yr, yi, cminv(cmmult(cminv(xr, xi), yr,
yi)));
```


### 11.7 Saving Compiled Procedures

When a file containing a procedure definition is run, the procedure is compiled and is then resident in memory. The procedure can be called as if it were an intrinsic function. If the new command is executed or you quit GAUSS and exit to the operating system, the compiled image of the procedure disappears and the file containing the procedure definition will have to be compiled again.

If a procedure contains no global references, that is, if it does not reference any global matrices or strings and it does not call any user-defined functions or procedures, it can be saved to disk in compiled form in a .fcg file with the save command, and loaded later with the loadp command whenever it is needed. This will usually be faster than recompiling. For example:

```
save path = c:\gauss\cp proc1,proc2,proc3;
loadp path = c:\gauss\cp proc1,proc2,proc3;
```

The name of the file will be the same as the name of the procedure, with a .fcg extension. (For details, see loadp and save in the GAUSS LANGUAGE REFERENCE.)

All compiled procedures should be saved in the same subdirectory, so there is no question where they are located when it is necessary to reload them. The loadp path can be set in your startup file to reflect this. Then, to load in procedures, use

```
loadp proc1,proc2,proc3;
```

Procedures that are saved in . fcg files will NOT be automatically loaded. It is necessary to explicitly load them with loadp. This feature should be used only when the time necessary for the autoloader to compile the source is too great. Also, unless these procedures have been compiled with \#lineson, debugging will be more complicated.

## 13 Random Number Generation in GAUSS

GAUSS provides a powerful suite of functionality for random number generation. The key features include:

1. Availability of several modern random number generators
2. Sampling of many distributions
3. Thread-safe random number generators
4. Parallel random number generation

### 13.1 Available Random Number Generators

1. KISS-Monster
2. MRG32k3a
3. MT19937: Mersenne-Twister 19937
4. MT2203: Mersenne-Twister 2203
5. Niederreiter
6. SFMT19937: Optimized Mersenne-Twister 19937
7. Sobol
8. WH: Wichmann-Hill

### 13.1.1 Choosing a Random Number Generator

## Quality

What is a high quality random number generator? Pierre L'Ecuyer stated that "The difference between the good and bad random number generators, in a nutshell, is that the bad ones fail very simple tests whereas the good ones fail only very complicated tests that are hard to figure out or impractical to run." The most prominent testsuites for testing random number generators (RNGs) are Marsaglia's DIEHARD, DIEHARDER (an extended version of DIEHARD maintained by Brown), and L'Ecuyer's TestU01. These are all good testsuites, with BigCrush from TestU01 being the most expansive and stringent. Below is a summary of the performance of each of the RNGs included in GAUSS on the BigCrush test.

| RNG | Number of <br> streams | Period <br> Length | Diehard | TestU01 <br> BigCrush |
| :--- | :---: | :--- | :--- | :---: |
| KISS-Monster | 1 | $10^{\wedge} 8859$ | PASS | PASS |
| MRG32k3a | 1 | $2^{\wedge} 191$ | PASS | PASS |
| MT19937 | 1 | $2^{\wedge} 19937$ | PASS* | 2 |
| MT2203 | 6024 | $2^{\wedge} 2203$ | PASS* | 4 |
| Wichmann-Hill | 273 | $2^{\wedge} 42.7$ | PASS* | 22 |

*The column under Test U01 indicates the number of test failures.
As we can see from the table above, all of the available RNGs (with the possible exception of Wichmann-Hill) provide very good to excellent performance. It is beyond the scope of this document to discuss the implications of particular test failures.

All of the RNGs in GAUSS are very fast. However, some are faster than others. Below is a chart of the relative speed of each random number generator in GAUSS.

1. SFMT19937
2. MT19937
3. MRG32K3A
4. Wichmann-Hill
5. Kiss-Monster

Beyond simply choosing the fastest available generators, two coding techniques can also cause your programs to run faster. The first is creating larger numbers of random deviates at a time. For example, creating one million random numbers in one call will be much faster than creating the same one million numbers through 100,000 calls that each create 10 numbers. Creating too many numbers at once can also slow down your program's performance if the resulting matrix takes up too much of your available RAM. The key point is to avoid creating large random matrices one or two numbers at a time. The second coding technique is incorporate multi-threading into your random number generation. This is covered in the next section of this chapter.

### 13.2 Thread-safe Random Number Generators

Each successive number in a pseudo-random sequence is computed based upon the generator's current state. The RNGs in GAUSS that take and return a state, such as rndKMu and rndGamma, are inherently thread-safe. These functions can be used independently in separate threads as long as the same state variable is not written to in more than one concurrent thread. Functions that do not take or return a state should not be used inside concurrent thread sets. For example, the following is not a legal program:

```
ThreadBegin;
    x = rndn (500, 1);
    y = myFunction(x);
ThreadEnd;
ThreadBegin;
    x2 = rndn (500, 1);
```

```
    y2 = myFunction(x2);
ThreadEnd;
ThreadJoin;
```

The problem with the above example is that implicit in each call to rndn is a write to the same global state. Note that rndn, rndGam and rndu all share the same global state. So replacing one of the above calls to rndn with a call to rndu would still result in an illegal program. To solve this problem, either move the call to rndn above the first ThreadBegin, like this:

```
x = rndn (500, 1);
x2 = \operatorname{rndn}(500, 1);
ThreadBegin;
    y = myFunction(x);
ThreadEnd;
ThreadBegin;
    y2 = myFunction(x2);
ThreadEnd;
ThreadJoin;
```

Or pass in and return the state vector:

```
seed1 = 723193;
seed2 = 94493;
ThreadBegin;
    { x1, state1 } = rndn(500, 1, seed1);
    y1 = myFunction(x1);
ThreadEnd;
ThreadBegin;
    { x2, state2 } = rndn (500,1,seed2);
    y2 = myFunction(x2);
ThreadEnd;
ThreadJoin;
```


### 13.3 Parallel Random Number Generation

### 13.3.1 Multiple Stream Generators

Some of the RNGs in GAUSS are a collection of more than one independent stream of random numbers. A stream is an independent series of numbers with a length that is the period length of the generator. Each of these sequences or streams has the same statistical properties. However, not all of the RNGs in GAUSS offer this ability. The MT2203 and the Wichman-Hill are examples of RNGs with multiple streams. The MT2203 is a set of 6024 different streams; the Wichmann-Hill contains 273 streams. You can initialize any of these streams with the rndCreateState function, like this:

```
// Initialize two Wichmann-Hill streams
seed = 192938;
whState3 = rndCreateState("wh-3", seed);
whState117 = rndCreateState("wh-117", seed);
// Initialize two MT2203 streams
seed = 192938;
mt2203State9 = rndCreateState("mt2203-3", seed);
mt2203State21 = rndCreateState("mt2203-21", seed);
```

Once created, these states can be passed into any of the new random number functions to create random numbers. To reiterate, from each of these newly created states you can create a full period length of random numbers.

### 13.3.2 Block-skipping

Creating random numbers from multiple streams provides multiple sets of independent random numbers with similar statistical properties that can be used in different threads. However, these separate streams do not form a contiguous set of random numbers. If you would like to process a contiguous stream of random numbers in multiple threads, you can use block-splitting. Block-splitting involves splitting a large chunk of random numbers into smaller contiguous blocks which can each be processed by different threads. This can be accomplished with the rndSkip function.

## Example

```
// Set seed and create new state vector
seed = 23423;
state1 = rndCreateState("mrg32k3a", seed);
// Advance state by 2
state2 = rndSkip(2, state1);
{ r, statel } = rndn (4, 1, statel);
// Same sequence as after skipping 2
{ r2, state2 } = rndn (2, 1, state2);
0.19971499
r=0.14053340
    -0.53132702
    0.48660530
r2 = -0.53132702
    0.48660530
```

For example if your program required four hundred million random numbers, you could split it into four blocks of one hundred million numbers each. This can be accomplished in GAUSS using the function rndStateSkip.

Each successive thread in the above program will process a different chunk of the sequence of random numbers.

```
// Set seed and create initial state vector
seed = 2342343;
state1 = rndCreateState("mrg32k3a", seed);
// Create 3 additional state vectors each starting le8
// numbers forward from the state just above it
state2 = rndStateSkip(1e8, state1);
state3 = rndStateSkip(1e8, state2);
state4 = rndStateSkip(1e8, state3);
// Use each state vector in a separate, concurrent thread
threadBegin;
```

```
    { x, statel } = rndGamma(1e8, 1, 2, 2, state1);
    y = myfunc(x);
threadEnd;
threadBegin;
    { x2, state2 } = rndGamma(1e8, 1, 2, 2, state2);
    y2 = myfunc(x2);
threadEnd;
threadBegin;
    { x, state3 } = rndGamma(1e8, 1, 2, 2, state3);
    y3 = myfunc(x3);
threadEnd;
threadBegin;
    { x, state4 } = rndGamma(1e8, 1, 2, 2, state4);
    y4 = myfunc(x);
threadEnd;
threadJoin;
```


## References

1. (MRG32k3a) L'Ecuyer, P. "Good Parameter Sets for Combined Multiple Recursive Random Number Generators." Operations Research, 47, 1, 159-164, 1999.
2. (TestU01) L'Ecuyer, P. and Simard, R. "TestU01: A C Library for Empirical Testing of Random Number Generators." ACM Trans. Math. Softw. 33, 4, Article 22 , 2007.
3. (Wichmann-Hill) MacLaren, N.M. "The Generation of Multiple Independent Sequences of Pseudorandom Numbers." Applied Statistics, 38, 351-359, 1989.

## 13 Sparse Matrices

The sparse matrix data type stores only the non-zero values of a 2-dimensional sparse matrix, which makes working with sparse matrices use less memory. Sparse matrix calculations may be faster or slower than those on an equivalent dense matrix, depending upon several factors.

Sparse matrix computations require extra complexity. This makes them slower than the same operation on an equivalent dense matrix. If the matrix is sufficiently sparse, the reduced element count can make up for this and provide better performance than dense operations. However, it is generally recommended to use dense matrices if your problem will fit into memory.

### 13.1 Defining Sparse Matrices

The sparse matrix data type is strongly typed in GAUSS, which means that a variable must be defined as a sparse matrix variable before it may be used as such. Once a variable has been defined as a sparse matrix, it may not be used as another data type. Similarly, once a variable has been used as a matrix, array, or other non-sparse data type, it may not be redefined as a sparse matrix.

To define a global sparse matrix, you may use either the declare or the let command:

```
declare sparse matrix sm1;
let sparse matrix sm1;
```

or the following implicit let statement:

```
sparse matrix sm1;
```

declare may be used to define multiple sparse matrices in a single statement:

```
declare sparse matrix sm1, sm2, sm3;
```

To define a local sparse matrix inside of a procedure, use an implicit let statement:

```
sparse matrix lsm1;
```

As neither let nor declare support the initialization of a sparse matrix at this time, you must initialize a sparse matrix with an assignment after defining it.

### 13.2 Creating and Using Sparse Matrices

Several new functions have been added to allow you to create and manipulate sparse matrices. These functions are:

| denseToSp | Converts a dense matrix to a sparse matrix. |
| :--- | :--- |
| denseToSpRe | Converts a dense matrix to a sparse matrix, using a <br> relative epsilon. |
| packedToSp | Creates a sparse matrix from a packed matrix of non- <br> zero values and row and column indices. |
| spBiconjGradSol | Solves the system of linear equations Ax=b using the <br> biconjugate gradient method. |
| spConjGradSol | Solves the system of linear equations Ax=b for <br> symmetric matrices using the conjugate gradient |

method.
spCreate
spDenseSubmat
spDiagRvMat
spEigv
spEye
spGetNZE
spLDL
spLU
spNumNZE
spOnes
spSubmat
spToDense
spTrTDense

Creates a sparse matrix from vectors of non-zero values, row indices, and column indices.

Returns a dense submatrix of sparse matrix.
Inserts submatrices along the diagonal of a sparse matrix.

Computes a specified number of eigenvalues and eigenvectors of a square, sparse matrix.

Creates a sparse identity matrix.
Returns the non-zero values in a sparse matrix, as well as their corresponding row and column indices.

Computes the LDL decomposition of a symmetric sparse matrix.

Computes the LU decomposition of a sparse matrix with partial pivoting.

Returns the number of non-zero elements in a sparse matrix.

Generates a sparse matrix containing only ones and zeros

Returns a sparse submatrix of sparse matrix.
Converts a sparse matrix to a dense matrix.
Multiplies a sparse matrix transposed by a dense matrix.
spTScalar
spZeros

Multiplies a sparse matrix by a scalar.
Creates a sparse matrix containing no non-zero values.

See Command Reference for detailed information on each command.

### 13.3 Sparse Support in Matrix Functions and Operators

Support for the sparse matrix data type has also been added to many matrix functions and operators. The following is a complete list of the matrix functions and operators that currently support the new sparse matrix type:

| . . . | /= | . $>=$ | minc |
| :---: | :---: | :---: | :---: |
| $\sim$ | $!=$ | $<$ | print |
| 1 | . $/=$ | . $<$ | rows |
| * | . $!=$ | . $<$ | scalerr |
| . * | == | <= | show |
| + | . $==$ | . $<=$ | type |
| - | > | abs |  |
| / | . $>$ | cols |  |
| . $/$ | >= | maxc |  |

Indexing is also supported for sparse matrices, using the same syntax as matrix indexing.

Note that printing a sparse matrix results in a table of the non-zero values contained in the sparse matrix, followed by their corresponding row and column indices, respectively.

### 13.3.1 Return Types for Dyadic Operators

The types of the returns for the dyadic operators were decided on a case-by-case basis, using the following general principles:

1. The return type for dyadic operations on two dense arguments is always dense.
2. The return type for dyadic operations on two sparse arguments is always sparse unless the result is likely to be significantly less sparse than the sparse arguments.
3. The return type for dyadic operations on a dense argument and a sparse argument (regardless of order) is dense unless the return is likely to be at least as sparse as the sparse argument.

These general principles have led to the following decisions regarding return types (note that only the cases that are displayed in these tables have been implemented at this point):

## Element-by-Element Numeric Operators

Element-by-Element Addition

| Result | $=$ | Left | Operator | Right |
| :---: | :--- | :--- | :---: | :---: |
| dense | $=$ | sparse | + | dense |
| dense | $=$ | dense | sparse | + |
| sparse | $=$ | dense | + | dense |
| dense |  |  | sparse |  |

Element-by-Element Subtraction
Result $=\quad$ Left Operator $\quad$ Right

| dense | $=$ | sparse | - | dense |
| :--- | :--- | :--- | :--- | :--- |
| dense | $=$ | dense | - | dense |
| sparse | $=$ | sparse | - | sparse |
| dense | $=$ | dense | - | sparse |

Element-by-Element Multiplication

| Result | $=$ | Left | Operator | Right |
| :--- | :--- | :---: | :---: | :---: |
| sparse | $=$ | sparse | .$^{*}$ | dense |
| dense | $=$ | dense | sparse | .$^{*}$ |
| sparse | $=$ | dense | .$^{*}$ | dense |
| sparse |  |  | sparse |  |
|  |  |  |  | sparse |

Element-by-Element Division

| Result | $=$ | Left | Operator | Right |
| :---: | :---: | :---: | :---: | :---: |
| sparse | $=$ | sparse | .$/$ | dense |
| dense | $=$ | dense | .$/$ | dense |
| dense | $=$ | sparse | .$/$ | sparse |
| dense | $=$ | dense | .$/$ | sparse |

## Other Numeric Operators

Matrix Multiplication

| Result | $=$ | Left | Operator | Right |
| :---: | :--- | :---: | :---: | :---: |
| dense | $=$ | sparse | $*$ | dense |
| dense | $=$ | dense | $*$ | dense |
| sparse | $=$ | sparse | $*$ | sparse |
|  |  | Linear Solve |  |  |
| Result | $=$ | Left | Operator | Right |


| dense | $=$ | dense | $/$ | dense |
| :--- | :--- | :--- | :--- | :--- |
| dense | $=$ | dense | $/$ | sparse |

Note that at this time, the dense $=$ dense / sparse case is defined only for real data.
When either of its arguments are sparse, the / operator uses a tolerance to determine the result, which may be read or set using the sysstate function, case 39. The default tolerance is $1 \mathrm{e}-14$.

## Relational Operators

Since the results of element-by-element 'dot' comparison operators depend largely on the kind of data inputted, there are both both dense-returning and sparse-returning versions of the dot comparison operators when one or both arguments is a sparse matrix. The regular dot comparison operators and their alphabetic counterparts always return dense matrices, and there is a new set of alphabetic dot comparison operators that all return sparse matrices:

Element-by-Element Dot Comparison Operators

| Operation | Dense-Returning | Sparse- <br> Returning |  |
| :--- | :--- | :--- | :--- |
| Equal to | .$==$ | . eq | .speq |

Since the element-by-element 'non-dot' comparison operators ( $=, /=,<,<=,>,>=$ ) and their alphabetic counterparts (eq, ne, lt, le, gt, ge) all return scalars, there are no sparsereturning versions of them.

## Other Matrix Operators

|  |  | Horizontal Concatenation |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Result | $=$ | Left | Operator | Right |
| dense | $=$ | dense | $\sim$ | dense |
| sparse |  | Sparse | $\sim$ | sparse |
| Result | $=$ | Left | Operator | Right |
| dense | $=$ | dense |  | dense |
| sparse |  |  |  |  |

## 14 N-Dimensional Arrays

In GAUSS, internally, matrices and arrays are separate data types. Matrices, which are 2-dimensional objects, are stored in memory in row major order. Therefore, a $3 \times 2$ matrix is stored as follows:

```
[1,1] [1,2] [2,1] [2,2] [3,1] [3,2]
```

The slowest moving dimension in memory is indexed on the left, and the fastest moving dimension is indexed on the right. This is true of N-dimensional arrays as well. A $4 \times 3 \times 2$ array is stored in the following way:

```
[1,1,1] [1,1,2] [1,2,1] [1,2,2] [1,3,1] [1,3,2]
[2,1,1] [2,1,2] [2,2,1] [2,2,2] [2,3,1] [2,3,2]
[3,1,1] [3,1,2] [3,2,1] [3,2,2] [3,3,1] [3,3,2]
[4,1,1] [4,1,2] [4,2,1] [4,2,2] [4,3,1] [4,3,2]
```

A complex N -dimensional array is stored in memory in the same way. Like complex matrices, complex arrays are stored with the entire real part first, followed by the entire imaginary part.

Every N-dimensional array has a corresponding Nx1 vector of orders that contains the sizes of each dimension of the array. This is stored with the array and can be accessed with getorders. The first element of the vector of orders corresponds to the slowest
moving dimension, and the last element corresponds to the fastest moving dimension (refer to the Glossary of Terms at the end of the chapter for clear definitions of these terms). The vector of orders for a $6 \times 5 \times 4 \times 3 \times 2$ array, which has 5 dimensions, is the following 5x1 vector:

```
    6
    5
    4
    3
    2
```

Two terms that are important in working with N -dimensional arrays are "dimension index" and "dimension number." A dimension index specifies a dimension based on indexing the vector of orders. It is a scalar, 1-to-N, where 1 corresponds to the dimension indicated by the first element of the vector of orders of the array (the slowest moving dimension) and N corresponds to the dimension indicated by the last element of the vector of orders (the fastest moving dimension).

A dimension number specifies dimensions by numbering them in the same order that one would add dimensions to an array. In other words, the dimensions of an N -dimensional array are numbered such that the fastest moving dimension has a dimension number of 1 , and the slowest moving dimension has a dimension number of N .

A $6 \times 5 \times 4 \times 3 \times 2$ array has 5 dimensions, so the first element of the vector of orders (in this case, 6) refers to the size of dimension number 5. Since the index of this element in the vector of orders is 1 , the dimension index of the corresponding dimension (dimension number 5) is also 1 .

You will find references to both dimension index and dimension number in the documentation for the functions that manipulate arrays.
There are a number of functions that have been designed to manipulate arrays. These functions allow you to manipulate a subarray within the array by passing in a locator vector to index any subarray that comprises a contiguous block of memory within the larger block. A vector of indices of an N -dimensional array is a [1-to-N]x1 vector of base 1 indices into the array, where the first element corresponds to the first element in a vector of orders. An Nx1 vector of indices locates the scalar whose position is indicated by the indices. For a $4 \times 3 \times 2$ array $x$, the $3 \times 1$ vector of indices:

```
3
2
1
```

indexes the [3,2,1] element of $x$. A $2 x 1$ vector of indices for this 3-dimensional example, references the 1-dimensional array whose starting location is given by the indices.

Because the elements of the vector of indices are always in the same order (the first element of the vector of indices corresponds to the slowest moving dimension of the array, the second element to the second slowest moving dimension, and so on), each unique vector of indices locates a unique subarray.

In general, an $[\mathrm{N}-\mathrm{K}] \mathrm{x} 1$ vector of indices locates a K -dimensional subarray that begins at the position indicated by the indices. The sizes of the dimensions of the K-dimensional subarray correspond to the last K elements of the vector of orders of the N -dimensional array. For a $6 \times 5 \times 4 \times 3 \times 2$ array $y$, the $2 \times 1$ vector of indices:

$$
\begin{aligned}
& 2 \\
& 5
\end{aligned}
$$

locates the $4 \times 3 \times 2$ subarray in $y$ that begins at $[2,5,1,1,1]$ and ends at $[2,5,4,3,2]$.

### 14.1 Bracketed Indexing

Brackets '[ ]' can be used to index N -dimensional arrays in virtually the same way that they are used to index matrices. Bracketed indexing is slower than the convenience array functions, such as getarray and setarray; however, it can be used to index non-contiguous elements. In order to index an N -dimensional array with brackets, there must be N indices located within the brackets, where the first index corresponds to the slowest moving dimension of the array and the last index corresponds to the fastest moving dimension.

For a $2 \times 3 \times 4$ array $x$, such that:
$[1,1,1]$ through $[1,3,4]=$
$\begin{array}{llll}1 & 2 & 3 & 4\end{array}$
$\begin{array}{llll}5 & 6 & 7 & 8\end{array}$
9101112
$[2,1,1]$ through $[2,3,4]=$
$\begin{array}{llll}13 & 14 & 15 & 16\end{array}$
$\begin{array}{llll}17 & 18 & 19 & 20\end{array}$
$2122 \quad 2324$
$x[1,2,3]$ returns a $1 x 1 x 1$ array containing the $[1,2,3]$ element of $x$.
7
$x[., 3,2]$ returns a $2 x 1 x 1$ array containing:
10
22
$x[2, \ldots, 1]$ returns a $1 \times 3 \times 2$ array containing
$13 \quad 16$

1720
2124
$x[., 2,1: 3]$ returns a $2 x 1 \times 3$ array containing

| 5 | 6 | 7 |
| ---: | ---: | ---: |
| 17 | 18 | 19 |

### 14.2 ExE Conformability

The following describes rules for ExE conformability of arrays for operators and functions with two or more arguments.

- Any N -dimensional array is conformable to a scalar.
- An array is conformable to a matrix only if the array has fewer than 3 dimensions, and the array and matrix follow the standard rules of ExE conformability.
- Two arrays are ExE conformable if they comply with one of the following requirements:
- The two arrays have the same number of dimensions, and each dimension has the same size.
- The two arrays have the same number of dimensions, and each of the N-2 slowest moving dimensions has the same size. In this case, the 2 fastest moving dimensions of the arrays must follow the ExE comformability rules that apply to matrices.
- Both of the arrays have fewer than 3 dimensions, and they follow the ExE conformability rules that apply to matrices.


### 14.3 Glossary of Terms

dimensions The number of dimensions of an object.
vector of orders Nx1 vector of the sizes of the dimensions of an object, where N is the number of dimensions, and the first element corresponds to the slowest moving dimension.
vector of indices
dimension number
[1-to-N]x1 vector of indices into an array, where the first element corresponds to the first element in a vector of orders.

Scalar [1-to-N], where 1 corresponds to the fastest moving dimension and N to the slowest moving dimension.

|  | dimension index | Scalar [1-to-N], where 1 corresponds to the first element of the vector of orders or vector of indices. |
| :---: | :---: | :---: |
|  | locator | [1-to-N]x1 vector of indices into an array used by array functions to locate a contiguous block of the array. |

## 15 Working with Arrays

### 15.1 Initializing Arrays

The use of N-dimensional arrays in GAUSS is an additional tool for reducing development time and increasing execution speed of programs. There are multiple ways of handling N -dimensional arrays and using them to solve problems, and these ways sometimes have implications for a trade-off between speed of execution and development time. We will try to make this clear in this chapter.

The term "arrays" specifically refers to N -dimensional arrays and must not be confused with matrices. Matrices and arrays are distinct types even if in fact they contain identical information. Functions for conversion from one to the other are described below.

There are five basic ways of creating an array depending on how the contents are specified:

| areshape | Create array from specified matrix . |
| :--- | :--- |
| aconcat | Create array from matrices and arrays. |
| aeye | Create array of identity matrices. |
| arrayinit | Allocate array filled with specified scalar value. |
| arrayalloc | Allocate array with no specified contents. |

### 15.1.1 areshape

areshape is a method for creating an array with specified contents. arrayinit creates an array filled with a selected scalar value: areshape will do the same, but with a matrix. For example, given a matrix, areshape will create an array containing multiple copies of that matrix:

```
x = reshape(seqa (1, 1, 4), 2, 2);
ord = 3 | 2 | 2;
a = areshape(x, ord);
print a;
    Plane [1,.,.]
    1.0000 2.0000
    3.0000 4.0000
    Plane [2,.,.]
    1.0000 2.0000
    3.0000 4.0000
    Plane [3,.,.]
    1.0000 2.0000
    3.0000 4.0000
```


## Reading Data from the Disk into an Array

areshape is a fast way to re-dimension a matrix or array already in memory. For example, suppose we have a GAUSS data set containing panel data and that it's small enough to be read in all at once:

```
panel = areshape(loadd("panel"),5|100|10);
mn = amean(panel,2); // 5x1x10 array of means of each panel
mm = moment(panel,0); // 5x10x10 array of moments of each
panel
/*
** VC is a 5x10x10 array of
** covariance matrices
```

```
*/
vc = mm / 100 - amult(atranspose(mn, 1|3|2), mn);
```

panel is a $5 \times 100 \times 10$ array, and in this context is 5 panels of 100 cases measured on 10 variables.

## Inserting Random Numbers into Arrays

A random array of any dimension or size can be quickly created using areshape. Thus, for a $10 \times 10 \times 5 \times 3$ array:

```
ord = { 10, 10, 5, 3 };
y = areshape (rndu (prodc (ord),1),ord);
```


## Expanding a Matrix into an Array Vector of Matrices

For computing the log-likelihood of a variance components model of panel data, it is necessary to expand a TxT matrix into an NTxT array of these matrices. This is easily accomplished using areshape. For example:

```
m={ 1.0 0.3 0.2,
    0.3 1.0 0.1,
        0.2 0.1 1.0 };
r = areshape (m, 3|3|3);
print r;
    Plane [1,.,.]
    1.0000 0.3000 0.2000
    0.3000 1.0000 0.1000
    0.2000 0.1000 1.0000
    Plane [2,.,.]
    1.0000 0.3000 0.2000
    0.3000 1.0000 0.1000
    0.2000 0.1000 1.0000
```

```
Plane [3,.,.]
1.0000 0.3000 0.2000
0.3000 1.0000 0.1000
0.2000 0.1000 1.0000
```


### 15.1.2 aconcat

aconcat creates arrays from conformable sets of matrices or arrays. With this function, contents are completely specified by the user. This example tries three concatenations, one along each dimension:

```
rndseed 345678;
x1 = rndn (2,2);
x2 = arrayinit(2|2,1);
/*
** along the first dimension or rows
*/
a = aconcat(x1,x2,1);
print a;
    -0.4300-0.2878 1.0000 1.0000
    -0.1327-0.0573 1.0000 1.0000
/*
** along the second dimension or columns
*/
a = aconcat(x1,x2,2);
print a;
    -0.4300 -0.2878
    -0.1327 -0.0573
    1.0000 1.0000
```

```
        1.0000 1.0000
/*
** along the third dimension
*/
a = aconcat(x1,x2,3);
print a;
Plane [1,.,.]
-0.4300 -0.2878
-0.1327 -0.0573
Plane [2,.,.]
1.0000 1.0000
1.0000 1.0000
```


### 15.1.3 aeye

aeye creates an array in which the principal diagonal of the two trailing dimensions is set to one. For example:

```
ord = 2 | 3 | 3;
a = aeye (ord);
print a;
Plane [1,.,.]
1.00000 0.00000 0.00000
0.00000 1.00000 0.00000
0.00000 0.00000 1.00000
Plane [2,.,.]
1.00000 0.00000 0.00000
0.00000 1.00000 0.00000
0.00000 0.00000 1.00000
```


### 15.1.4 arrayinit

arrayinit creates an array with all elements set to a specified value. For example:

```
ord = 3 | 2 | 3;
a = arrayinit(ord,1);
print a;
    Plane [1,.,.]
    1.0000 1.0000 1.0000
    1.0000 1.0000 1.0000
Plane [2,.,.]
1.0000 1.0000 1.0000
1.0000 1.0000 1.0000
Plane [3,.,.]
1.0000 1.0000 1.0000
1.0000 1.0000 1.0000
```


### 15.1.5 arrayalloc

arrayalloc creates an array with specified number and size of dimensions without setting elements to any values. This requires a vector specifying the order of the array. The length of the vector determines the number of dimensions, and each element determines the size of the corresponding dimensions. The array will then have to be filled using any of several methods described later in this chapter.

For example, to allocate a $2 \times 2 \times 3$ array:

```
rndseed 345678;
ord = 3 | 2 | 2;
a = arrayalloc(ord, 0);
for i(1,ord[1],1);
```

```
        a[i,.,.] = rndn(2, 3);
endfor;
print a;
    Plane [1,.,.]
    -0.4300-0.2878-0.1327
    -0.0573 -1.2900 0.2467
        Plane [2,.,.]
    -1.4249 -0.0796 1.2693
    -0.7530-1.7906-0.6103
        Plane [3,.,.]
        1.2586 -0.4773 0.7044
-1.2544 0.5002 0.3559
```

The second argument in the call to arrayalloc specifies whether the created array is real or complex. arrayinit creates only real arrays.

### 15.2 Assigning to Arrays

There are three methods used for assignment to an array:

| index operator | The same method as matrices, generalized to arrays. |
| :--- | :--- |
| putarray | Put a subarray into an N-dimensional array and <br> returns the result. |
| setarray | Set a subarray of an N-dimensional array in place. |

And there are several ways to extract parts of arrays:

| index operator | The same method as matrices, generalized to arrays. |
| :--- | :--- |
| getarray | Get a subarray from an array. |

```
getmatrix
getmatrix4D
getscalar4D
```

Get a matrix from an array.
Get a matrix from a 4-dimensional array.
Get a scalar from a 4-dimensional array.

The index operator is the slowest way to extract parts of arrays. The specialized functions are the fastest when the circumstances are appropriate for their use.

### 15.2.1 index operator

The index operator will put a subarray into an array in a manner analogous to the use of index operators on matrices:

```
a = arrayinit(3|2|2, 0);
b = arrayinit(3|1|2, 1);
a[.,2,.] = b;
print a;
```

```
Plane [1,.,.]
0.0000 0.0000
1.0000 1.0000
Plane [2,.,.]
0.0000 0.0000
1.0000 1.0000
Plane [3,.,.]
0.0000 0.0000
1.0000 1.0000
```

As this example illustrates, the assignment doesn't have to be contiguous. putMatrix and setMatrix require a contiguous assignment, but for that reason they are faster.

The right hand side of the assignment can also be a matrix:

```
a[1,.,.] = rndn(2, 2);
print a;
    Plane [1,.,.]
-1.7906502 -0.61038103
    1.2586160-0.47736360
    Plane [2,.,.]
    0.00000 0.00000
    1.00000 1.00000
    Plane [3,.,.]
    0.00000 0.00000
    1.00000 1.00000
```

The index operator will extract an array from a subarray in a manner analogous to the use of index operators on matrices:

```
a = areshape(seqa (1,1,12), 3|2|2);
b = a[.,1,.];
print a;
    Plane [1,.,.]
    1.0000 2.0000
    3.0000 4.0000
    Plane [2,.,.]
    5.0000 6.0000
    7.0000 8.0000
    Plane [3,.,.]
    9.0000 10.000
    11.000 12.000
print b;
```

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```
Plane [1,.,.]
1.0000 2.0000
Plane [2,.,.]
5.0000 6.0000
Plane [3,.,.]
9.0000 10.000
```

It is important to note that the result is always an array even if it's a scalar value:

```
c = a[1,1,1];
print c;
    Plane [1,.,.]
    1.0000
```

If you require a matrix result, and if the result has one or two dimensions, use arraytomat to convert to a matrix, or use getmatrix, or getmatrix4D. Or, if the result is a scalar, use getscalar3D or getscalar4D.

### 15.2.2 getarray

getarray is an additional method for extracting arrays:

```
a = areshape(seqa (1,1,12), 3|2|2);
b = getarray(a, 2|1);
print a;
    Plane [1,.,.]
    1.0000 2.0000
    3.0000 4.0000
    Plane [2,.,.]
    5.0000 6.0000
    7.0000 8.0000
```

```
    Plane [3,.,.]
    9.0000 10.000
    11.000 12.000
print b;
    5.0000 6.0000
```

getarray can only extract a contiguous part of an array. To get non-contiguous parts you must use the index operator.

### 15.2.3 getmatrix

If the result is one or two dimensions, getmatrix returns a portion of an array converted to a matrix. getmatrix is about 20 percent faster than the index operator:

```
a = areshape(seqa (1,1,12), 3|2|2);
b = getmatrix (a, 2);
print b;
    5.0000 6.0000
    7.0000 8.0000
```


### 15.2.4 getmatrix4D

This is a specialized version of getmatrix for 4-dimensional arrays. It behaves just like getmatrix but is dramatically faster for that type of array. The following illustrates the difference in timing:

```
a = arrayinit(100|100|10|10, 1);
t0 = date;
for i(1, 100, 1);
```

```
        for j(1, 100, 1);
        b = a[i,j,.,.];
        endfor;
endfor;
t1 = date;
e1 = ethsec(t0, t1);
print e1;
print;
t2 = date;
for i(1,100,1);
    for j(1,100,1);
        b = getmatrix4d(a, i, j);
    endfor;
endfor;
t3 = date;
e2 = ethsec(t2, t3);
print e2;
print;
print ftostrC(100*((e1-e2)/e1), "percent difference -
%6.2lf%%");
    13.000000
    5.0000000
percent difference - 61.54%
```


### 15.2.5 getscalar3D, getscalar4D

These are specialized versions of getmatrix for retrieving scalar elements of 3dimensional and 4-dimensional arrays, respectively. They behave just like getmatrix, with scalar results, but are much faster. For example:

```
a = arrayinit(100|10|10, 1);
t0 = date;
for i(1,100,1);
        for j(1,10,1);
            for k(1,10,1);
            b = a[i,j,k];
            endfor;
        endfor;
endfor;
t1 = date;
e1 = ethsec(t0, t1);
print e1;
print;
t2=date;
for i(1,100,1);
        for j(1,10,1);
        for k(1,10,1);
            b = getscalar3d(a, i, j, k);
        endfor;
    endfor;
endfor;
t3 = date;
e2 = ethsec(t2, t3);
print e2;
print;
print ftostrC(100*((e1-e2)/e1), "percent difference -
%6.2lf%%");
7.0000000
2.0000000
percent difference - 71.43%
```


### 15.2.6 putarray

putarray enters a subarray, matrix, or scalar into an N-dimensional array and returns the result in an array. This function is much faster than the index operator, but it requires the part of the array being assigned to be contiguous:

```
a = arrayinit(3|2|2, 3);
b = putarray(a, 2, eye(2));
print b;
    Plane [1,.,.]
    3.0000 3.0000
    3.0000 3.0000
Plane [2,.,.]
1.0000 0.00000
0.00000 1.0000
Plane [3,.,.]
3.0000 3.0000
3.0000 3.0000
```


### 15.2.7 setarray

setarray enters a subarray, matrix, or scalar into an N -dimensional array in place:

```
a = arrayinit(3|2|2,3);
setarray a,2, eye(2);
print b;
    Plane [1,.,.]
    3.0000 3.0000
    3.0000 3.0000
    Plane [2,.,.]
```

```
1.0000 0.0000
0.0000 1.0000
Plane [3,.,.]
3.0000 3.0000
3.0000 3.0000
```


### 15.3 Looping with Arrays

When working with arrays, for loops and do loops may be used in the usual way. In the following, let $Y$ be an Nx1xL array of $L$ time series, $X$ an Nx1xK array of $K$ independent variables, $b$ a KxL matrix of regression coefficients, phi a PxLxL array of garch coefficients, theta a QxLxL array of arch coefficients, and omega a LxL symmetric matrix of constants. The log-likelihood for a multivariate garch BEKK model can be computed using the index operator:

```
yord = getorders(Y);
xord = getorders(X);
gord = getorders(phi);
aord = getorders(theta);
N = yord[1]; // No. of observations
L = yord[3]; // No. of time series
K = xord[3]; // No. of independent variables // in mean equa-
tion
P = gord[1]; // order of garch parameters
Q = aord[1]; // order of arch parameters
r = maxc(P|Q);
E = Y - amult(X, areshape(B, N|K|L));
sigma = areshape(omega,N|L|L);
for i(r+1, N, 1);
    for j (1,Q,1);
        W = amult(theta[j,.,.],
            atranspose(E[i-j,.,.], 1|3|2));
```

```
        sigma[i,.,.] = sigma[i,.,.] + amult(W, atranspose
(W,1|3|2));
    endfor;
    for j(1, P, 1);
        sigma[i,.,.] = sigma[i,.,.] + amult(amult(phi[j,.,.],
sigma[i-j,.,.]),phi[j,.,.]);
    endfor;
endfor;
sigmai = invpd(sigma);
lndet = ln(det(sigma));
lnl = -0.5*( L* (N-R)*asum(ln(det(sigmai)),1) + asum(amult
(amult(E, sigmai), atranspose(E,1|3|2)), 3);
```

Instead of index operators, the above computation can be done using getarray and setarray:

```
yord = getorders(Y);
xord = getorders(X);
gord = getorders(phi);
aord = getorders(theta);
N = yord[1]; // No. of observations
L = yord[3]; // No. of time series
K = xord[3]; // No. of independent variables in mean equation
P = gord[1]; // order of garch parameters
Q = aord[1]; // order of arch parameters
r = maxc(P|Q);
E = Y - amult(X, areshape(B,N|K|L));
sigma = areshape(omega, N|L|L);
for i(r+1, N, 1);
        for j(1,Q,1);
            W = amult(getarray(theta, j),
            atranspose(getarray(E, i-j), 2|1));
            setarray sigma,i, getarray(sigma, i)+
```

```
        amult(W, atranspose(W, 2|1));
        endfor;
    for j(1, P, 1);
        setarray sigma,i, getarray(sigma,i)+
        areshape (amult(amult (getarray (phi, j),
        getarray(sigma, i-j)), getarray(phi, j)), 3|3);
        endfor;
endfor;
sigmai = invpd(sigma);
lndet = ln(det(sigma));
lnl = -0.5*( L*(N-R)*asum(ln(det(sigmai)),1)+
    asum(amult(amult(E,sigmai), atranspose(E,1|3|2)), 3)
```

Putting the two code fragments above into loops that called them a hundred times and measuring the time, produced the following results:
index operator: 2.604 seconds
getarray, setarray: 1.092 seconds
Thus, the getarray and setarray methods are more than twice as fast.

### 15.3.1 loopnextindex

Several keyword functions are available in GAUSS for looping with arrays. The problem in the previous section, for example, can be written using these functions rather than with for loops:

```
sigind = r + 1;
sigloop:
sig0ind = sigind[1];
thetaind = 1;
thetaloop:
```

```
sig0ind = sigOind - 1;
W = amult(getarray(theta,thetaind),
atranspose(getarray(E, sig0ind), 2|1));
setarray sigma,sigind, getarray(sigma, sigind)+
amult(W, atranspose (W, 2|1));
loopnextindex thetaloop,thetaind,aord;
sigOind = sigind;
phiind = 1;
philoop:
```

```
sig0ind[1] = sig0ind[1] - 1;
```

sig0ind[1] = sig0ind[1] - 1;
setarray sigma,sigind, getarray(sigma, sigind)+
setarray sigma,sigind, getarray(sigma, sigind)+
areshape (amult(amult(getarray(phi, phiind),
areshape (amult(amult(getarray(phi, phiind),
getArray(sigma, sig0ind)),
getArray(sigma, sig0ind)),
getArray(phi, phiind)), 3|3);
getArray(phi, phiind)), 3|3);
loopnextindex philoop,phiind,gord;
loopnextindex philoop,phiind,gord;
loopnextindex sigloop,sigind,sigord;

```
loopnextindex sigloop,sigind,sigord;
```

The loopnextindex function in this example isn't faster than the for loop used in the previous section primarily because the code is looping only through the first dimension in each loop. The advantages of loopnextindex, previousindex, nextindex, and walkindex are when the code is looping through the higher dimensions of a highly dimensioned array. In this case, looping through an array can be very complicated and difficult to manage using for loops. loopnextindex can be faster and more useful.

The next example compares two ways of extracting a subarray from a 5-dimensional array:

```
ord = 3|3|3|3|3;
a = areshape(seqa(1, 1, prodc(ord)) ,ord);
b = eye (3);
for i(1, 3, 1);
```

```
        for j(1, 3, 1);
        for k(1, 3, 1);
            setarray a,i|j|k,b;
        endfor;
        endfor;
endfor;
ind = { 1,1,1 };
loopi:
setarray a,ind,b;
loopnextindex loopi,ind,ord;
```

Calling each loop 10,000 times and measuring the time each takes, we get
for loop: 1.171 seconds
loopnextindex: 321 seconds
In other words, loopnextindex is about four times faster, a very significant difference.

### 15.4 Miscellaneous Array Functions

This section discusses miscellaneous array functions.

### 15.4.1 atranspose

This function changes the order of the dimensions. For example:

```
a = areshape(seqa(1, 1, 12), 2|3|2);
print a;
    Plane [1,.,.]
    1.0000 2.0000
```

```
        3.0000 4.0000
        5.0000 6.0000
        Plane [2,.,.]
        7.0000 8.0000
        9.0000 10.000
        11.000 12.000
/*
** swap 2nd and 3rd dimension
*/
print atranspose(a,1|3|2);
    Plane [1,.,.]
    1.0000 3.0000 5.0000
    2.0000 4.0000 6.0000
    Plane [2,.,.]
    7.0000 9.0000 11.000
    8.0000 10.000 12.000
/*
** swap 1st and 3rd dimension
*/
print atranspose(a,3|2|1);
    Plane [1,.,.]
    1.0000 7.0000
    3.0000 9.0000
    5.0000 11.000
    Plane [2,.,.]
    2.0000 8.0000
    4.0000 10.000
    6.0000 12.000
/*
```

```
** move 3rd into the front
*/
print atranspose(a,3|1|2);
    Plane [1,.,.]
    1.0000 3.0000 5.0000
    7.0000 9.0000 11.000
    Plane [2,.,.]
    2.0000 4.0000 6.0000
    8.0000 10.000 12.000
```


### 15.4.2 amult

This function performs a matrix multiplication on the last two trailing dimensions of an array. The leading dimensions must be strictly conformable, and the last two trailing dimensions must be conformable in the matrix product sense. For example:

```
a = areshape(seqa(1, 1, 12), 2|3|2);
b = areshape(seqa(1, 1, 16), 2|2|4);
c = amult(a, b);
print a;
    Plane [1,.,.]
    1.0000 2.0000
    3.0000 4.0000
    5.0000 6.0000
    Plane [2,.,.]
    7.0000 8.0000
    9.0000 10.000
    11.000 12.000
    print b;
```

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```
Plane [1,.,.]
1.0000 2.0000 3.0000 4.0000
5.0000 6.0000 7.0000 8.0000
Plane [2,.,.]
9.0000 10.000 11.000 12.000
13.000 14.000 15.000 16.000
print c;
Plane [1,.,.]
11.000 14.000 17.000 20.000
23.000 30.000 37.000 44.000
35.000 46.000 57.000 68.000
Plane [2,.,.]
167.00 182.00 197.00 212.00
211.00 230.00 249.00 268.00
255.00 278.00 301.00 324.00
```

Suppose we have a matrix of data sets, a 2 x 2 matrix of 100 x 5 data sets that we've stored in a $2 \times 2 \times 100 \times 5$ array called $x$. The moment matrices of these data sets can easily and quickly be computed using atranspose and amult:

```
VC = amult(atranspose(x, 1|2|4|3), x);
```


### 15.4.3 amean, amin, amax

These functions compute the means, minimums, and maximums, respectively, across a dimension of an array. The size of the selected dimension of the resulting array is shrunk to one and contains the means, minimums, or maximums depending on the function called. For example:

```
a = areshape(seqa (1,1,12), 2|3|2);
print a;
```

```
    Plane [1,.,.]
    1.0000 2.0000
    3.0000 4.0000
    5.0000 6.0000
    Plane [2,.,.]
    7.0000 8.0000
    9.0000 10.000
    11.000 12.000
/*
** compute means along third dimension
*/
print amean(a, 3);
    Plane [1,.,.]
    4.0000 5.0000
    6.0000 7.0000
    8.0000 9.0000
/*
** print means along the second dimension, i.e.,
** down the columns
*/
print amean(a, 2);
    Plane [1,.,.]
    3.0000 4.0000
    Plane [2,.,.]
    9.0000 10.000
/*
** print the minimums down the columns
*/
```

```
print amin(a, 2);
    Plane [1,.,.]
    1.0000 2.0000
    Plane [2,.,.]
    7.0000 8.0000
/*
** print the maximums along the third dimension
*/
print amax(a, 3);
    Plane [1,.,.]
    7.0000 8.0000
    9.0000 10.000
    11.000 12.000
```


### 15.4.4 getdims

This function returns the number of dimensions of an array:

```
a = arrayinit(4|4|5|2, 0);
print getdims(a);
    4.00
```


### 15.4.5 getorders

This function returns the sizes of each dimension of an array. The length of the vector returned by getorders is the dimension of the array:

```
a = arrayinit(4|4|5|2,0);
print getorders(a);
```

$$
\begin{aligned}
& 4.00 \\
& 4.00 \\
& 5.00 \\
& 2.00
\end{aligned}
$$

### 15.4.6 arraytomat

This function converts an array with two or fewer dimensions to a matrix:

```
a = arrayinit(2|2, 0);
b = arraytomat(a);
type(a);
    21.000
type (b);
    6 . 0 0 0 0
```


### 15.4.7 mattoarray

This function converts a matrix to an array:

```
b = rndn(2,2);
a = mattoarray(b);
type(b);
    6.0000
type(a);
    21.000
```


### 15.5 Using Arrays with GAUSS functions

Many of the GAUSS functions have been re-designed to work with arrays. There are two general approaches to this implementation. There are exceptions, however, and you are urged to refer to the documention if you are not sure how a particular GAUSS function handles array input.

In the first approach, the function returns an element-by-element result that is strictly conformable to the input. For example, cdfNc returns an array of identical size and shape to the input array:

```
a = areshape(seqa(-2, .5, 12), 2|3|2);
b = cdfnc(a);
print b;
Plane [1,.,.]
0.9772 0.9331
0.8413 0.6914
0.5000 0.3085
Plane [2,.,.]
0.1586 0.0668
0.0227 0.0062
0.0013 0.0002
```

In the second approach, which applies generally to GAUSS matrix functions, the function operates on the matrix defined by the last two trailing dimensions of the array. Thus, given a $5 \times 10 \times 3$ array, moment returns a $5 \times 3 \times 3$ array of five moment matrices computed from the five $10 \times 3$ matrices in the input array.

Only the last two trailing dimensions matter; i.e., given a $2 \times 3 \times 4 \times 5 \times 10 \times 6$ array, moment returns a $2 \times 3 \times 4 \times 5 \times 6 \times 6$ array of moment matrices.

For example, in the following the result is a $2 \times 3$ array of $3 \times 1$ vectors of singular values of a $2 \times 3$ array of $6 \times 3$ matrices:

```
a = areshape(seqa (1,1,108), 2| 3|6|3);
b=svds (a);
print b;
    Plane [1,1,.,.]
    45.894532
    1.6407053
    1.2063156e-015
    Plane [1,2,.,.]
    118.72909
    0.63421188
    5.8652600e-015
    Plane [1,3,.,.]
    194.29063
    0.38756064
    1.7162751e-014
    Plane [2,1,.,.]
    270.30524
    0.27857175
    1.9012118e-014
    Plane [2,2,.,.]
    346.47504
    0.21732995
    1.4501098e-014
    Plane [2,3,.,.]
    422.71618
    0.17813229
    1.6612287e-014
```

It might be tempting to conclude from this example that, in general, a GAUSS function's behavior on the last two trailing dimensions of an array is strictly analogous to the

GAUSS function's behavior on a matrix. This may be true with some of the functions, but not all. For example, the GAUSSmeanc function returns a column result for matrix input. However, the behavior for the GAUSSamean function is not analogous. This function takes a second argument that specifies on which dimension the mean is to be taken. That dimension is then collapsed to a size of 1 . Thus:

```
a = areshape(seqa(1, 1, 24), 2|3|4);
print a;
    Plane [1,.,.]
    1.000 2.000 3.000 4.000
    5.000 6.000 7.000 8.000
    9.000 10.000 11.000 12.000
    Plane [2,.,.]
    13.000 14.000 15.000 16.000
    17.000 18.000 19.000 20.000
    21.000 22.000 23.000 24.000
/*
** means computed across rows
*/
b = amean (a,1);
print b;
    Plane [1,.,.]
    2.500
    6.500
    10.500
    Plane [2,.,.]
    14.500
    18.500
    22.500
/*
```

```
** means computed down columns
*/
c = amean (a,2);
print c;
    Plane [1,.,.]
    5.000 6.000 7.000 8.000
    Plane [2,.,.]
    17.000 18.000 19.000 20.000
/*
** means computed along 3rd dimension
*/
d = amean (a,3);
print d;
    Plane [1,.,.]
    7.000 8.000 9.000 10.000
    11.000 12.000 13.000 14.000
    15.000 16.000 17.000 18.000
```


### 15.6 A Panel Data Model

Suppose we have N cases observed at T times. Let $y_{\text {it }}$ be an observation on a dependent variable for the $i t h$ case at time $t, X_{i t}$ an observation of $k$ independent variables for the $i$ th case at time $t, B, a \operatorname{Kxl}$ vector of coefficients. Then

$$
y_{i t}=X_{i t} B+\mu_{i}+\varepsilon_{i t}
$$

is a variance components model where $\mu_{i}$ is a random error term uncorrelated with $\varepsilon_{i t}$, but which is correlated within cases. This implies an NTxNT residual moment matrix that is block diagonal with N TxT moment matrices with the following form:

$$
\left[\begin{array}{cccc}
\sigma_{\mu}^{2}+\sigma_{\epsilon}^{2} & \sigma^{2} & \cdots & \sigma_{\mu}^{2} \\
\sigma_{\mu}^{2} & \sigma_{\mu}^{2}+\sigma_{\epsilon}^{2} & \cdots & \sigma_{\mu}^{2} \\
\vdots & \vdots & \vdots & \vdots \\
\sigma_{\mu}^{2} & \sigma_{\mu}^{2} & \ldots & \sigma_{\mu}^{2}+\sigma_{\epsilon}^{2}
\end{array}\right]
$$

The log-likelihood for this model is

```
lnL = -0.5(NT(ln(2п)) - ln | | | + (Y - XB)' ' -1 (Y - XB))
```

where $\Omega$ is the block-diagonal moment matrix of the residuals.

## Computing the Log-likelihood

Using GAUSS arrays, we can compute the log-likelihood of this model without resorting to do loops. Let $Y$ be a 100x3x1 array of observations on the dependent variable, and $X$ a $100 \times 3 \times 5$ array of observations on the independent variables. Further let b be a $5 \times 1$ vector of coefficients, and sigu and sige be the residual variances of $\mu$ and $\varepsilon$ respectively. Then, in explicit steps we compute

```
N = 100;
T = 3;
K = 5;
sigma = sigu * ones(T, T) + sige * eye(T); // TxT sigma
sigmai = invpd(sigma); // sigma inverse
lndet = N* ln(detl);
E = Y - amult(X, areshape(B, N|K|l)); // residuals
Omegai = areshape(sigmai, N|T|T); // diagonal blocks //
stacked in a vector array
R1 = amult(atranspose(E, 1|3|2), Omegai); // E'Omegai
R2 = amult(R1, E); // R1*E
lnL = -0.5*(N*T* ln (2*pi) - lndet + asum(R2, 3)); // log-likel-
hood
```

All of this can be made more efficient by nesting statements, which eliminates copying of temporary intervening arrays to local arrays. It is also useful to add a check for the positive definiteness of sigma:

```
N = 100;
T = 3;
K = 5;
const = -0.5*N*T* ln (2*pi);
oldt = trapchk(1);
trap 1,1;
sigmai = invpd(sigu*ones(T, T)+sige*eye(T));
trap oldt,1;
if not scalmiss(sigmai);
    E = Y - amult(X, areshape(B,N|K|I));
    lnl = const + 0.5*N*ln(detl) -
    0.5*asum (amult (amult (atranspose (E, 1| 3| 2),
    areshape(sigmai,N|T|T)),E), 3);
else;
    lnl = error(0);
endif;
```


### 15.7 Appendix

This is an incomplete list of special functions for working with arrays. Many GAUSS functions have been modified to handle arrays and are not listed here. For example, cdfnc computes the complement of the Normal cdf for each element of an array just as it would for a matrix. See the documentation for these GAUSS functions for information about their behavior with arrays.

| aconcat | Concatenate conformable matrices and arrays in a <br> user-specified dimension. |
| :--- | :--- |
| aeye | Create an array of identity matrices. |
| $\operatorname{amax}$ | Compute the maximum elements across a dimension |

of an array.

| amean | Compute the mean along one dimension of an array. |
| :--- | :--- |
| amin | Compute the minimum elements across a dimension <br> of an array. |
| amult | Perform a matrix multiplication on the last two <br> trailing dimensions of an array. |
| areshape | Reshape a scalar, matrix, or array into an array of <br> user-specified size. |
| arrayalloc | Create an N-dimensional array with unspecified <br> contents. |
| arrayinit | Create an N-dimensional array with a specified fill <br> value. |
| arraytomat | Change an array to type matrix. |
| asum | Transpose an N-dimensional array. |
| atranspose | Get a contiguous subarray from an N-dimensional |
| getarray | array. |
| getdims | Get the number of dimensions in an array. |

Create an N-dimensional array with a specified fill value.

Change an array to type matrix.
Compute the sum across one dimension of an array.
Transpose an N-dimensional array.
Get a contiguous subarray from an N -dimensional array.

Get the number of dimensions in an array.
Get a contiguous matrix from an N -dimensional array.

Get a contiguous matrix from a 4-dimensional array. Get the vector of orders corresponding to an array. Get a scalar from a 3-dimensional array.

| getscalar4D | Get a scalar form a 4-dimensional array. |
| :--- | :--- |
| loopnextindex | Increment an index vector to the next logical index <br> and jump to the specified label if the index did not <br> wrap to the beginning. |
| mattoarray | Change a matrix to a type array. |
| nextindex | Return the index of the next element or subarray in <br> an array. |
| previousindex | Return the index of the previous element or subarray <br> in an array. |
| putarray | Put a contiguous subarray into an N-dimensional <br> array and return the resulting array. |
| setarray | Set a contiguous subarray of an N-dimensional array. |
| walkindex | Walk the index of an array forward or backward <br> through a specified dimension. |

## 16 Structures

### 16.1 Basic Structures

### 16.1.1 Structure Definition

The syntax for a structure definition is

```
struct A { /* list of members */ };
```

The list of members can include scalars, arrays, matrices, strings, and string arrays, as well as other structures. As a type, scalars are unique to structures and don't otherwise exist.

For example, the following defines a structure containing the possible contents:

```
struct generic_example {
    scalar x;
    matrix y;
    string sl;
    string array s2;
    struct other_example t;
};
```


## Defining a structure in a program

A useful convention is to save the structure definition into a file with a . sdf extension. After the structure definition has been created and saved in a file, the next step is to
make the structure definition available for your program. This may be accomplished by either executing the structure definition file or by adding the structure definition to a library.

## Executing a structure definition file

You can execute a structure definition just like any other GAUSS program file.
However, any time that the new command is entered, the structure definition will be cleared from your workspace. To ensure that the structure definition is always available for your program, you can add an \#include statement like this:

```
#include filename.sdf
```

to the top of your program file. This will ensure that the structure definition is always available for your program.

## Adding a structure definition to a library

Starting in GAUSS version 13.1, you can also add structure definition files to a GAUSS library. You can add structure definitions to any GAUSS library with the lib command or using the Library Tool in the user interface. If a structure definition is in a library file, you can make all procedures and structure definitions available with one statement. For example:

```
library mylibrary;
```

instead of:

```
library mylibrary;
#include mystruct1.sdf
#include mystruct2.sdf
```

Also if a structure is defined in an active library, autocomplete will be available for the structure members.

The next section describes how to create an instance of a structure.

### 16.1.2 Declaring an Instance

To use a structure, it is necessary to declare an instance. The syntax for this is

```
struct structure_type structure_name;
```

For example:

```
#include example.sdf
struct generic_example p0;
```


### 16.1.3 Initializing an Instance

Members of structures are referenced using a "dot" syntax:

$$
\mathrm{p} 0 . \mathrm{x}=\operatorname{rndn}(20,3)
$$

The same syntax applies when referred to on the right-hand side:

```
mn = meanc (p0.x);
```


## Initialization of Global Structures

Global structures are initialized at compile time. Each member of the structure is initialized according to the following schedule:

| scalar | 0, a scalar zero |
| :--- | :--- |
| matrix | $\}$, an empty matrix with zero rows and zero <br> columns |
| array | 0, a 1-dimensional array set to zero |
| string | "", a null string |
| string array | "", a 1x1 string array set to null |
| sparse matrix | $\}$, an empty sparse matrix with zero rows and zero <br> columns |

If a global already exists in memory, it will not be reinitialized. It may be the case in your program that when it is rerun, the global variables may need to be reset to default values. That is, your program may depend on certain members of a structure being set to default values that are set to some other value later in the program. When you rerun this program, you will want to reinitialize the global structure. To do this, make an assignment to at least one of the members. This can be made convenient by writing a procedure that declares a structure and initializes one of its members to a default value, and then returns it. For example:

```
//ds.src
#include ds.sdf
proc dsCreate;
    struct DS dO;
    d0.dataMatrix = 0;
    retp(d0);
endp;
```

Calling this function after declaring an instance of the structure will ensure initialization to default values each time your program is run:

```
struct DS dO;
dO = dsCreate;
```


## Initializing Local Structures

Local structures, which are structures defined inside procedures, are initialized at the first assignment. The procedure may have been written in such a way that a subset of structures are used an any one call, and in that case time is saved by not initializing the unused structures. They will be initialized to default values only when the first assignment is made to one of its members.

### 16.1.4 Arrays of Structures

To create a matrix of instances, use the reshape command:

```
#include ds.sdf
struct DS p0;
p0 = reshape (dsCreate,5,1);
```

This creates a $5 \times 1$ vector of instances of DS structures, with all of the members initialized to default values.

When the instance members have been set to some other values, reshape will produce multiple copies of that instance set to those values.

Matrices or vectors of instances can also be created by concatenation:

```
#include trade.sdf
struct option p0,p1,p2;
p0 = optionCreate;
p1 = optionCreate;
p2 = p1 | p0;
```


### 16.1.5 Structure Indexing

Structure indexing may be used to reference a particular element in a structure array. The syntax follows that of matrix indexing. For example, given the following structure definition:

```
struct example1 {
    matrix x;
    matrix y;
    string str;
};
```

you could create an array of examplel structures and index it as follows:

```
struct example1 ela;
struct example1 e1b;
```

```
ela = ela | e1b;
ela[2,1].y = rndn (25,10);
```

In this example, ela and e1b are concatenated to create a $2 x 1$ array of example 1 structures that is assigned back to ela. Then the $y$ member of the $[2,1]$ element of ela is set to a random matrix.

Indexing of structure arrays can occur on multiple levels. For example, let's define the following structures:

```
struct example3 {
    matrix w;
    string array sa;
};
struct example2 {
    matrix z;
    struct example3 e3;
};
```

and let's redefine examplel to include an instance of an example2 structure:

```
struct example1 {
    matrix x;
    matrix y;
    string str;
    struct example2 e2;
};
```



Figure 16.1: Structure tree for e1

Let's assume that we have an examplel structure el like the one displayed in the figure above. We could then index the structure as follows:

$$
r=e 1 \cdot e 2[3,1] \cdot e 3[2,1] \cdot w
$$

You can also use indexing to reference the structure itself, rather than a member of that structure:

```
struct example3 e3tmp;
e3tmp = e1.e2[3,1].e3[2,1];
```

Or you can use indexing to reference a subarray of structures:

$$
\text { e3tmp }=\text { e1.e2[3,1].e3[., 1]; }
$$

In this case, e3tmp would be an array of $3 x 1$ example 3 structures, since the $[3,1]$ member of e1. e 2 contains a $3 \times 1$ array of example 3 structures.

It is important to remember, however, that when indexing a structure array on multiple levels, only the final index may resolve to an array of structures. For example:

$$
\text { e3tmp }=\text { e1.e2[., 1].e3[2,1]; }
$$

would be invalid, since e1.e2[.,1] resolves to a 3 x1 array of example 2 structures.

### 16.1.6 Saving an Instance to the Disk

Instances and vectors or matrices of instances of structures can be saved in a file on the disk, and later loaded from the file onto the disk. The syntax for saving an instance to the disk is

```
ret = savestruct(instance, filename);
```

The file on the disk will have an. fsr extension.
For example:

```
#include ds.sdf
struct DS p0;
p0 = reshape (dsCreate, 2,1);
retc = saveStruct(p2, "p2");
```

This saves the vector of instances in a file called p2.fsr. The variable retc will be zero if the save was successful; otherwise, nonzero.

### 16.1.7 Loading an Instance from the Disk

The syntax for loading a file containing an instance or matrix of instances is

```
{ instance, retc } = loadstruct(file_name, structure_name);
```

For example:

```
#include ds.sdf;
struct DS p3;
{ p3, retc } = loadstruct("p2", "ds");
```


### 16.1.8 Passing Structures to Procedures

Structures or members of structures can be passed to procedures. When a structure is passed as an argument to a procedure, it is passed by value. The structure becomes a local copy of the structure that was passed. The data in the structure is not duplicated unless the local copy of the structure has a new value assigned to one of its members. Structure arguments must be declared in the procedure definition:

```
struct rectangle {
        matrix ulx;
        matrix uly;
        matrix lrx;
        matrix lry;
    };
proc area(struct rectangle rect);
    retp((rect.lrx - rect.ulx).*(rect.uly - rect.lry));
endp;
```

Local structures are defined using a struct statement inside the procedure definition:

```
proc center(struct rectangle rect);
        struct rectangle cent;
        cent.lrx = (rect.lrx - rect.ulx) / 2;
        cent.ulx = -cent.lrx;
        cent.uly = (rect.uly - rect.lry) / 2;
        cent.lry = -cent.uly;
        retp(cent);
endp;
```


### 16.2 Structure Pointers

A structure pointer is a separate data type that contains the address of a structure and is used to reference that structure.

### 16.2.1 Creating and Assigning Structure Pointers

Given the following structure type definition:

```
struct example_struct {
    matrix x;
    matrix y;
};
```

a pointer to an example_struct structure can be created with the following syntax:

```
struct example_struct *esp;
```

However, at this point, esp is not yet pointing at anything. It has only been defined to be the kind of pointer that points at example_struct structures. To set it to point at a particular structure instance, we must first create the structure instance:

```
struct example_struct es;
```

and then we can set esp to point at es by setting esp to the address of es:

```
esp = &es;
```

The following code:

```
struct example_struct es2;
es2 = *esp;
```

copies the contents of the structure that esp is pointing at (i.e., the contents of es) to es2. It is the same as

```
struct example_struct es2;
es2 = es;
```


### 16.2.2 Structure Pointer References

To reference a member of a structure, we use a "dot" syntax. For example, we might use the following code to set the $x$ member of es.

```
es.x = rndn (3,3);
```

To reference a member of a structure using a pointer to that structure, we use an "arrow" syntax. For example, we might use the following code to set the $x$ member of es using the pointer esp:

```
esp->x = rndn(10,5);
```

This code will modify es, since esp is merely a pointer to es.
Structure pointers cannot be members of a structure. The following is illegal:

```
struct example_struct_2 {
    matrix z;
    struct example_struct *ep;
};
```

Therefore, since a structure pointer will never be a member of a structure, neither

```
sp1->sp2->x;
```

nor

```
s.sp1->x;
```

will ever be valid ( $s p 1$ and $s p 2$ are assumed to be structure pointers, $s$ a structure instance, and $x$ a matrix). The "arrow" ( $->$ ) will only be valid if it is used for the first (or furthest left) dereference, as in:

```
sp1->st.x;
```

At this point we do not support indexing of structure pointers. Thus, a structure pointer should point at a scalar structure instance, not a matrix of structures. However, you may index members of that scalar structure instance. So, for example, let us suppose that you defined the following structure types:

```
struct sb {
    matrix y;
    matrix z;
};
struct sa {
    matrix x;
    struct structb s;
};
```

```
struct sa *sap
sap = &a0;
sap->s[3,1].y = rndn (3,3);
```


### 16.2.3 Using Structure Pointers in Procedures

Structure pointers are especially useful in cases where structures are passed into and out of procedures. If a procedure takes a structure as an argument and modifies any members of that structure, then it makes a local copy of the entire structure before modifying it. Thus if you want to have the modified copy of the structure after running the procedure, you need to pass the structure out of the procedure as one of its return arguments. For example:

```
struct example_struct {
    matrix x;
    matrix y;
```

```
        matrix z;
};
proc product(struct example_struct es);
    es.z = (es.x).* (es.y);
    retp(es);
endp;
struct example_struct esl;
es1.x = rndn(1000,100);
es1.y = rndn(1000,1);
es1 = product(es1);
```

In this example, the structure es 1 is passed into the procedure, copied and modified. The modified structure is then passed out of the procedure and assigned back to esi.

Structure pointers allow you to avoid such excessive data copying and eliminate the need to pass a structure back out of a procedure in cases like this. When you pass a structure pointer into a procedure and then modify a member of the structure that it references, the actual structure is modified rather than a local copy of it. Thus there is no need to pass the modifed structure back out of the procedure. For example, the above example could be accomplished using structure pointers as follows:

```
struct example_struct {
    matrix x;
    matrix y;
    matrix z;
};
proc(0) = product(struct example_struct *esp);
    esp->z = (esp->x).* (esp->y);
endp;
struct example_struct esl;
struct example_struct *eslp;
eslp = &esl;
```

```
es1.x = rndn(1000,100);
es1.y = rndn(1000,1);
product(es1p);
```

In this case, the procedure modifies the structure es1, which eslp is pointing at, instead of a local copy of the structure.

### 16.3 Special Structures

There are three common types of structures that will be found in the GAUSS Run-Time Library and applications.

The DS and PV structures are defined in the GAUSS Run-Time Library. Their definitions are found in $d s . s d f$ and $p v . s d f$, respectively, in the src source code subdirectory.

Before structures, many procedures in the Run-Time Library and all applications had global variables serving a variety of purposes, such as setting and altering defaults. Currently, these variables are being entered as members of "control" structures.

### 16.3.1 The DS Structure

The DS structure, or "data" structure, is a very simple structure. It contains a member for each GAUSS data type. The following is found in $\mathrm{ds} . \mathrm{sdf}$ :

```
struct DS {
    scalar type;
    matrix dataMatrix;
    array dataArray;
    string dname;
    string array vnames;
} ;
```

This structure was designed for use by the various optimization functions in GAUSS, in particular, sqpSolvemt, as well as a set of gradient procedures, gradmt, hessmt, et al.

These procedures all require that the user provide a procedure computing a function (to be optimized or take the derivative of, etc.), which takes the DS structure as an argument. The Run-Time Library procedures such as sqpSol vemt take the DS structure as an argument and pass it on to the user-provided procedure without modification. Thus, the user can put into that structure whatever might be needed as data in the procedure.

To initialize an instance of a DS structure, the procedure dsCreate is defined in ds.src:

```
#include ds.sdf
struct DS dO;
dO = dsCreate;
```


### 16.3.2 The PV Structure

The PV structure, or parameter vector structure, is used by various optimization, modeling, and gradient procedures, in particular sqpSolvemt, for handling the parameter vector. The GAUSS Run-Time Library contains special functions that work with this structure. They are prefixed by "pv" and defined in pv. src. These functions store matrices and arrays with parameters in the structure, and retrieve various kinds of information about the parameters and parameter vector from it.

## "Packing" into a PV Structure

The various procedures in the Run-Time Library and applications for optimization, modelling, derivatives, etc., all require a parameter vector. Parameters in complex models, however, often come in matrices of various types, and it has been the responsibility of the programmer to generate the parameter vector from the matrices and vice versa. The PV procedures make this problem much more convenient to solve.

The typical situation involves two parts: first, "packing" the parameters into the $\mathbf{P V}$ structure, which is then passed to the Run-Time Library procedure or application; and
second, "unpacking" the $\mathbf{P V}$ structure in the user-provided procedure for use in computing the objective function. For example, to pack parameters into a $\mathbf{P V}$ structure:

```
#include sqpsolvemt.sdf
/* starting values */
b0 = 1; //constant in mean equation
garch = { .1,.1 }; //garch parameters
arch = { .1, .1 }; //arch parameters
omega =.1; //constant in variance equation
struct PV p0;
p0 = pvPack (pvCreate,b0, "b0");
p0 = pvPack (p0,garch, "garch");
p0 = pvPack (p0,arch, "arch");
p0 = pvPack(p0,omega, "omega");
/* data */
z = loadd("tseries");
struct DS dO;
dO.dataMatrix = z;
```

Next, in the user-provided procedure for computing the objective function, in this case minus the log-likelihood, the parameter vector is unpacked:

```
proc ll(struct PV p0, struct DS dO);
    local b0,garch, arch,omega,p,q,h,u,vc,w;
    b0 = pvUnpack (p0, "b0");
    garch = pvUnpack (p0, "garch");
    arch = pvUnpack (p0, "arch");
    omega = pvUnpack (p0, "omega");
    p = rows (garch);
    q = rows(arch);
    u = d0.dataMatrix - b0;
    vC = moment (u,0)/rows (u) ;
    w = omega + (zeros(q,q) | shiftr((u.*ones(1,q))',
```

```
        seqa(q-1,-1,q))) * arch;
        h = recserar( }\textrm{w},\textrm{vc}\mathrm{ *ones ( p,1),garch);
    logl = -0.5 * ((u.*u)./h + ln(2*pi) + ln(h));
    retp(logl);
endp;
```


## Masked Matrices

The pvUnpack function unpacks parameters into matrices or arrays for use in computations. The first argument is a $\mathbf{P V}$ structure containing the parameter vector. Sometimes the matrix or vector is partly parameters to be estimated (that is, a parameter to be entered in the parameter vector) and partly fixed parameters. To distinguish between estimated and fixed parameters, an additional argument is used in the packing function called a "mask", which is strictly conformable to the input matrix. Its elements are set to 1 for an estimated parameter and 0 for a fixed parameter. For example:

```
p0 = pvPackm(p0,.1*eye(3), "theta", eye(3));
```

Here just the diagonal of a $3 \times 3$ matrix is added to the parameter vector.
When this matrix is unpacked, the entire matrix is returned with current values of the parameters on the diagonal:

```
print
pvUnpack(p0, "theta");
\begin{tabular}{lll}
0.1000 & 0.0000 & 0.0000 \\
0.0000 & 0.1000 & 0.0000 \\
0.0000 & 0.0000 & 0.1000
\end{tabular}
```


## Symmetric Matrices

Symmetric matrices are a special case because even if the entire matrix is to be estimated, only the nonredundant portion is to be put into the parameter vector. Thus, for them there are special procedures. For example:

```
VC={ 1 . 6 .4, . 6 1 . 2, . 4 . 2 1 };
p0 = pvPacks(p0,vC, "vC");
```

There is also a procedure for masking in case only a subset of the nonredundant elements are to be included in the parameter vector:

```
VC={ 1 . 6 .4,.6 1 . 2, . 4 . 2 1 };
mask = { 1 1 0, 1 1 0, 0 0 1 };
p0 = pvPacksm(p0,vc, "vC",mask);
```


## Fast Unpacking

When unpacking matrices using a matrix name, pvUnpack has to make a search through a list of names, which is relatively time-consuming. This can be alleviated by using an index rather than a name in unpacking. To do this, though, requires using a special pack procedure that establishes the index:

```
p0 = pvPacki(p0,b0, "b0",1);
p0 = pvPacki(p0,garch, "garch",2);
p0 = pvPacki (p0,arch, "arch",3);
p0 = pvPacki(p0,omega, "omega",4);
//Now they may be unpacked using the index number:
b0 = pvUnpack (p0,1);
garch = pvUnpack (p0,2);
arch = pvUnpack (p0,3);
omega = pvUnpack(p0,4);
```

When packed with an index number, they may be unpacked either by index or by name, but unpacking by index is faster.

### 16.3.3 Miscellaneous PV Procedures

## pvList

This procedure generates a list of the matrices or arrays packed into the structure:

```
p0 = pvPack(p0,b0, "b0");
p0 = pvPack(p0,garch, "garch");
p0 = pvPack (p0,arch, "arch");
p0 = pvPack(p0,omega, "omega");
print pvList(pO);
    bo
    garch
    arch
    omega
```


## pvLength

This procedure returns the length of the parameter vector:

```
print
pvLength(p0);
    6.0000
```


## pvGetParNames

This procedure generates a list of parameter names:

```
print
pvGetParNames(p0);
    b0 [1, 1]
    garch[1,1]
    garch[2,1]
    arch[1,1]
    arch[2,1]
    omega[1,1]
```


## pvGetParVector

This procedure returns the parameter vector itself:

```
print
pvGetParVector(p0);
    1.0000
    0.1000
    0.1000
    0.1000
    0.1000
    1.0000
```


## pvPutParVector

This procedure replaces the parameter vector with the one in the argument:

```
newp = { 1.5, .2, .2, .3, .3, . 8 };
p0 = pvPutParVector(newp,p0);
print pvGetParVector(p0);
    1.5000
    0.2000
    0.2000
    0.3000
    0.3000
    0.8000
```


## pvGetIndex

This procedure returns the indices in the parameter vector of the parameters in a matrix. These indices are useful when setting linear constraints or bounds in sqpSolvemt. Bounds, for example, are set by specifying a Kx 2 matrix where K is the length of the parameter vector and the first column are the lower bounds and the second the upper bounds. To set the bounds for a particular parameter, then, requires knowing where that parameter is in the parameter vector. This information can be found using pvGetIndex. For example:

```
// get indices of lambda parameters in parameter vector
lind = pvGetIndex(par0, "lambda");
```

```
// set bounds constraint matrix to unconstrained default
c0.bounds = ones(pvLength (par0),1).*(-1e250~1e250);
// set bounds for lambda parameters to be positive
c0.bounds[lind,1] = zeros(rows(lind),1);
```


### 16.3.4 Control Structures

Another important class of structures is the "control" structure. Applications developed before structures were introduced into GAUSS typically handled some program specifications by the use of global variables which had some disadvantages, in particular, preventing the nesting of calls to procedures.

Currently, the purposes served by global variables are now served by the use of a control structure. For example, for sqpSol vemt:

```
struct
sqpSolvemtControl {
    matrix A;
    matrix B;
    matrix C;
    matrix D;
    scalar eqProc;
    scalar ineqProc;
    matrix bounds;
    scalar gradProc;
    scalar hessProc;
    scalar maxIters;
    scalar dirTol;
    scalar CovType;
    scalar feasibleTest;
    scalar maxTries;
    scalar randRadius;
    scalar trustRadius;
    scalar seed;
```

```
    scalar output;
    scalar printIters;
    matrix weights;
};
```

The members of this structure determine optional behaviors of sqpSolvemt.

## 16.4 sqpSolveMT

sqpSolveMT is a procedure in the GAUSS Run-Time Library that solves the general nonlinear programming problem using a Sequential Quadratic Programming descent method, that is, it solves

```
min f(\Theta)
```

subject to

$$
\begin{array}{ll}
A \Theta=B & \text { linear equality } \\
C \Theta>=D & \text { linear equality } \\
H(\Theta)=0 & \text { nonlinear equality } \\
G(\Theta)>=0 & \text { nonlinear equality } \\
\Theta_{\mathrm{lb}}<=\Theta<=\Theta_{\mathrm{ub}} & \text { bounds }
\end{array}
$$

The linear and bounds constraints are redundant with respect to the nonlinear constraints, but are treated separately for computational convenience.

The call to sqpSolveMT has four input arguments and one output argument:

```
out = sqPSolveMT(&fct, P, D, C);
```


### 16.4.1 Input Arguments

The first input argument is a pointer to the objective function to be minimized. The procedure computing this objective function has two arguments: a PV structure containing
the start values, and a DS structure containing data, if any. For example:

```
proc fct(struct PV p0, struct DS dO);
        local y, x, b0, b, e, s;
        y = d0[1].dataMatrix;
        x = d0[2].dataMatrix;
        b0 = pvUnpack (p0, "constant");
        b = pvUnpack(p0, "coefficients");
        e = y - b0 - x * b;
        s = sqrt(e'e/rows (e));
    retp (-pdfn(e/s);
endp;
```

Note that this procedure returns a vector rather than a scalar. When the objective function is a properly defined log-likelihood, returning a vector of minus log-probabilities permits the calculation of a QML covariance matrix of the parameters.

The remaining input arguments are structures:
P a PV structure containing starting values of the parameters

D a DS structure containing data, if any
C an sqpSolvemtControl structure

The DS structure is optional. sqpSolvemt passes this argument on to the userprovided procedure that $\& f c t$ is pointing to without modification. If there is no data, a default structure can be passed to it.
sqpSolvemtControl Structure
A default sqpSolvemtControl structure can be passed in the fourth argument for an unconstrained problem. The members of this structure are as follows:

A

B

C

D
eqProc

IneqProc

Bounds

GradProc

MxK matrix, linear equality constraint coefficients: $A \Theta=B$, where p is a vector of the parameters.

Mx1 vector, linear equality constraint constants: $A \Theta$ $=B$, where p is a vector of the parameters.

MxK matrix, linear inequality constraint coefficients: $C \Theta=D$, where p is a vector of the parameters.

Mx1 vector, linear inequality constraint constants: $C \Theta=D$, where p is a vector of the parameters.
scalar, pointer to a procedure that computes the nonlinear equality constraints. When such a procedure has been provided, it has two input arguments, instances of $\mathbf{P V}$ and DS structures, and one output argument, a vector of computed inequality constraints.

Default = .; i.e., no inequality procedure.
scalar, pointer to a procedure that computes the nonlinear inequality constraints. When such a procedure has been provided, it has two input arguments, instances of $\mathbf{P V}$ and DS structures, and one output argument, a vector of computed inequality constraints.

Default = .; i.e., no inequality procedure.
$1 \times 2$ or Kx2 matrix, bounds on parameters. If $1 \times 2$ all parameters have same bounds.

Default $=-1 \mathrm{e} 2561 \mathrm{e} 256$.
scalar, pointer to a procedure that computes the
gradient of the function with respect to the parameters. When such a procedure has been provided, it has two input arguments, instances of $\mathbf{P V}$ and DS structures, and one output argument, the derivatives. If the function procedure returns a scalar, the gradient procedure returns a 1 xK row vector of derivatives. If function procedure turns an Nx 1 vector, the gradient procedure returns an NxK matrix of derivatives.

This procedure may compute a subset of the derivatives. sqpSolvemt will compute numerical derivatives for all those elements set to missing values in the return vector or matrix.

Default = .; i.e., no gradient procedure has been provided.

## HessProc

MaxIters
scalar, pointer to a procedure that computes the Hessian; i.e., the matrix of second order partial derivatives of the function with respect to the parameters. When such a procedure has been provided, it has two input arguments, instances of $\mathbf{P V}$ and DS structures, and one output argument, a vector of computed inequality constraints.

Default = .; i.e., no Hessian procedure has been provided.

Whether the objective function procedure returns a scalar or vector, the Hessian procedure must return a KxK matrix. Elements set to missing values will be computed numerically by sqpSolvemt. scalar, maximum number of iterations. Default $=$

MaxTries

DirTol

CovType

FeasibleTest
randRadius
seed
trustRadius
$1 \mathrm{e}+5$.
scalar, maximum number of attemps in random search. Default $=100$.
scalar, convergence tolerance for gradient of estimated coefficients. Default $=1 \mathrm{e}-5$. When this criterion has been satisifed, sqpSolvemt exits the iterations.
scalar, if 2, QML covariance matrix, else if 0 , no covariance matrix is computed, else ML covariance matrix is computed. For a QML covariance matrix, the objective function procedure must return an Nx1 vector of minus log-probabilities.
scalar, if nonzero, parameters are tested for feasibility before computing function in line search. If function is defined outside inequality boundaries, then this test can be turned off. Default $=1$.
scalar, if zero, no random search is attempted. If nonzero, it is the radius of the random search. Default $=.001$.
scalar, if nonzero, seeds random number generator for random search, otherwise time in seconds from midnight is used.
scalar, radius of the trust region. If scalar missing, trust region not applied. The trust sets a maximum amount of the direction at each iteration. Default $=$ . 001 .
output
PrintIters
weights
scalar, if nonzero, results are printed. Default $=0$.
scalar, if nonzero, prints iteration information. Default $=0$.
vector, weights for objective function returning a vector. Default $=1$.

### 16.4.2 Output Argument

The single output argument is an sqpSolvemtOut structure. Its definition is:

```
struct SQPsolveMTOut {
    struct PV par;
    scalar fct;
    struct SQPsolveMTLagrange lagr;
    scalar retcode;
    matrix moment;
    matrix hessian;
    matrix xproduct;
};
```

The members of this structure are:

| par | instance of a PV structure containing the parameter <br> estimates are placed in the matrix member par. |
| :--- | :--- |
| fct | scalar, function evaluated at final parameter estimates. |
| lagr | an instance of an SQPLagrange structure containing <br> the Lagrangeans for the constraints. For an instance <br> named lagr, the members are: |


| lagr.lineq | Mx1 vector, Lagrangeans of linear <br> equality constraints |
| :--- | :--- |
| lagr.nlineq | Nx1 vector, Lagrangeans of <br> nonlinear equality constraints |
| lagr.linineq | Px1 vector, Lagrangeans of linear <br> inequality constraints |
| lagr.nlinineq | Qx1 vector, Lagrangeans of <br> nonlinear inequality constraints |
| lagr.bounds | Kx2 matrix, Lagrangeans of bounds |
| Whenever a constraint is active, its associated <br> Lagrangean will be nonzero. For any constraint that <br> is inactive throughout the iterations as well as at <br> convergence, the corresponding Lagrangean matrix <br> will be set to a scalar missing value. |  |
| return | normal convergence <br> forced exit |
| 1 | maximum number of iterations <br> exceeded <br> function calculation failed |
| 2 | gradient calculation failed <br> Hessian calculation failed <br> line search failed |
| 5 |  |


| 7 | error with constraints |
| :--- | :--- |
| 8 | function complex |
| 9 | feasible direction couldn't be found |

### 16.4.3 Example

## Define

$$
Y=\Lambda \eta+\Theta
$$

where $\Lambda$ is a KxL matrix of loadings, $\eta$ an Lx1 vector of unobserved "latent" variables, and $\Theta$ a Kx1 vector of unobserved errors. Then

$$
\Sigma=\Lambda \Phi \Lambda^{\prime} \Psi
$$

where $\Phi$ is the LxL covariance matrix of the latent variables, and $\Psi$ is the KxK covariance matrix of the errors.

The log-likelihood of the $i$ th observation is

$$
\log P(i)=-1 / 2\left[K \ln (2 \pi)+\ln |\pi|+Y(i) \Sigma Y(i)^{\prime}\right]
$$

Not all elements of $\Lambda, \Phi$, and $\Psi$ can be estimated. At least one element of each column of $\Lambda$ must be fixed to 1 , and $\Psi$ is usually a diagonal matrix.

## Constraints

To ensure a well-defined log-likelihood, constraints on the parameters are required to guarantee positive definite covariance matrices. To do this, a procedure is written that returns the eigenvalues of $\Sigma$ and $\Phi$ minus a small number. sqpSolvemt then finds parameters such that these eigenvalues are greater than or equal to that small number.

### 16.4.4 The Command File

This command file can be found in the file sqpfact.e in the examples subdirectory:

```
#include sqpsolvemt.sdf
lambda = { 1.0 0.0,
    0.5 0.0,
    0.0 1.0,
    0.0 0.5 };
lmask = { 0 0,
    1 0,
    0 0,
    0 1 };
phi = { 1.0 0.3,
    0.3 1.0 };
psi}={0.60.0 0.0 0.0
    0.0 0.6 0.0 0.0,
    0.0 0.0 0.6 0.0,
    0.0 0.0 0.0 0.6 };
tmask = { 1 0 0 0,
    0 1 0 0,
    0 0 1 0,
    0 0 0 1 };
struct PV par0;
par0 = pvCreate;
par0 = pvPackm(par0,lambda, "lambda",lmask);
par0 = pvPacks (par0,phi, "phi");
par0 = pvPacksm(par0,psi, "psi",tmask);
struct SQPsolveMTControl c0;
c0 = sqpSolveMTcontrolCreate;
//get indices of lambda; parameters in parameter vector
lind = pvGetIndex(par0, "lambda");
//get indices of psi; parameters in parameter vector
tind = pvGetIndex(par0, "psi");
```

```
c0.bounds = ones(pvLength (par0),1).* (-1e250~1e250);
c0.bounds[lind,1] = zeros(rows(lind),1);
c0.bounds[lind,2] = 10*ones(rows(lind),1);
c0.bounds[tind,1] = .001*ones(rows(tind),1);
c0.bounds[tind,2] = 100*ones(rows(tind),1);
c0.output = 1;
c0.printIters = 1;
c0.trustRadius = 1;
c0.ineqProc = &ineq;
c0.covType = 1;
struct DS dO;
dO = dsCreate;
d0.dataMatrix = loadd("maxfact");
output file = sqpfact.out reset;
struct SQPsolveMTOut out0;
out0 = SQPsolveMT(&lpr,par0,d0,c0);
lambdahat = pvUnpack(out0.par, "lambda");
phihat = pvUnpack(out0.par, "phi");
psihat = pvUnpack(out0.par, "psi");
print "estimates";
print;
print "lambda" lambdahat;
print;
print "phi" phihat;
print;
print "psi" psihat;
struct PV stderr;
stderr = out0.par;
if not scalmiss(out0.moment);
```

```
    stderr = pvPutParVector(stderr,sqrt(diag(out0.moment)));
    lambdase = pvUnpack(stderr, "lambda");
    phise = pvUnpack(stderr, "phi");
    psise = pvUnpack(stderr, "psi");
    print "standard errors";
    print;
    print "lambda" lambdase;
    print;
    print "phi" phise;
print;
print "psi" psise;
endif;
output off;
proc lpr(struct PV par1, struct DS data1);
    local lambda,phi,psi,sigma,logl;
    lambda = pvUnpack(par1, "lambda");
    phi = pvUnpack(par1, "phi");
    psi = pvUnpack(par1, "psi");
    sigma = lambda*phi*lambda' + psi;
    logl = -lnpdfmvn(data1.dataMatrix,sigma);
    retp(logl);
endp;
proc ineq(struct PV par1, struct DS datal);
    local lambda,phi,psi,sigma,e;
    lambda = pvUnpack(par1, "lambda");
    phi = pvUnpack(par1, "phi");
    psi = pvUnpack (par1, "psi");
    sigma = lambda*phi*lambda' + psi;
    e = eigh(sigma) - .001; //eigenvalues of sigma
    e = e | eigh(phi) - .001; //eigenvalues of phi
    retp(e);
endp;
```


## 17 Run-Time Library Structures

Two structures are used by several GAUSSRun-Time Library functions for handling parameter vectors and data: the $\mathbf{P V}$ parameter structure and the $\mathbf{D S}$ data structure.

### 17.1 The PV Parameter Structure

The members of an instance of structure of type $\mathbf{P V}$ are all "private," that is, not accessible directly to the user. It is designed to handle parameter vectors for thread-safe optimization functions. Entering and receiving parameter vectors, and accessing properties of this vector, are accomplished using special functions.

Suppose you are optimizing a function containing a KxL matrix of coefficients. The optimization function requires a parameter vector but your function uses a KxL matrix. Your needs and the needs of the optimization function can be both satisfied by an instance of the structure of type PV. For example:

```
struct PV p1;
p1 = pvCreate;
//on input contains start values
//on exit contains estimates
x = zeros(4,3);
p1 = pvPack(p1,x, "coefficients");
```

The pvCreate function initializes p1 to default values. pvPack enters the $4 \times 3$ matrix stored row-wise as a $12 \times 1$ parameter vector for the optimization function. The optimization program will pass the instance of the structure of type $\mathbf{P V}$ to your objective function.

By calling pvUnpack your $4 \times 3$ coefficient matrix is retrieved from the parameter vector. For example, in your procedure you have

```
x = pvUnpack(p1, "coefficients");
```

and now $x$ is a $4 x 3$ matrix of coefficients for your use in calculating the object function.
Suppose that your objective function has parameters to be estimated in a covariance matrix. The covariance matrix is a symmetric matrix where only the lower left portion contains unique values for estimation. To handle this, use pvPacks. For example:

```
struct PV p1;
p1 = pvCreate;
COV = { 1.0 0.1 0.1,
    0.1 1.0 0.1,
    0.1 0.1 1.0 };
p1 = pvPacks(p1,cov, "covariance");
```

Only the lower left portion of cov will be stored in the parameter vector. When the covariance matrix is unpacked, the parameters in the parameter vector will be entered into both the lower and upper portions of the matrix.

There may be cases where only a portion of a matrix being used to compute the objective function are parameters to be estimated. In this case use pvPackm with a "mask" matrix that contains ones where parameters are to be estimated and zeros otherwise. For example,

```
struct PV p1;
p1 = pvCreate;
cov = { 1.0 0.5,
    0.5 1.0 };
mask = { 0 1,
```

```
    1 0 };
p1 = pvPacksm(p1,cov, "correlation",mask);
```

Here only the one element in the lower left of $\mathbf{c o v}$ is stored in the parameter vector. Suppose the optimization program sends a trial value for that parameter of, say, . 45 . When the matrix is unpacked in your procedure it will contain the fixed values associated with the zeros in the mask as well as the trial value in that part of the matrix associated with the ones. Thus,

```
print unpack(p1, "correlation");
1.0000 . 4500
.4500 1.0000
```

A mask may also be used with general matrices to store a portion of a matrix in the parameter vector.

```
struct PV p1;
p1 = pvCreate;
m={ 0.0 0.5 1.0,
    0.5 0.0 0.3 };
mask = { 0 1 1,
    1 0 0};
p1 = pvPackm(p1,m, "coefficients",mask);
```

A PV instance can, of course, hold parameters from all these types of matrices: symmetric, masked symmetric, rectangular, and masked rectangular. For example:

```
lambda = { 1.0 0.0,
        0.5 0.0,
        0.0 1.0,
        0.0 0.5 };
lmask = { 0 0,
    1 0,
    0 0,
    0 1 };
```

```
phi={ 1.0 0.3,
    0.3 1.0 };
theta}={0.60.0 0.0 0.0
    0.0 0.6 0.0 0.0,
    0.0 0.0 0.6 0.0,
    0.0 0.0 0.0 0.6 };
tmask ={ 1 0 0 0,
    0 1 0 0,
    0 0 1 0,
    0 0 0 1 };
struct PV par0;
par0 = pvCreate;
par0 = pvPackm(par0,lambda, "lambda",lmask);
par0 = pvPacks (par0,phi, "phi");
par0 = pvPacksm(par0,theta, "theta",tmask);
```

It isn't necessary to know where in the parameter vector the parameters are located in order to use them in your procedure calculating the objective function. Thus:

```
lambda = pvUnpack(par1, "lambda");
phi = pvUnpack(par1, "phi");
theta = pvUnpack(par1, "theta");
sigma = lambda*phi*lambda' + theta;
```

Additional functions are available to retrieve information on the properties of the parameter vector. pvGetParVector and pvPutParVector get and put parameter vector from and into the PV instance, pvGetParNames retrieves names for the elements of the parameter vector, pvList returns the list of matrix names in the PV instance, pvLength the length of the parameter vector.

```
struct PV p1;
p1 = pvCreate;
cov = { 0.1 0.5,
    0.5 1.0 };
mask = { 0 1,
    1 0 };
```

```
p1 = pvPacksm(p1,cov, "correlation",mask);
print pvGetParVector(pl);
    0.5000
p1 = pvPutParVector(p1,.8);
print pvGetParVector(p1);
    0.8000
print pvUnpack(p1, "correlation");
    1.0000 . 8000
    0.8000 1.0000
print pvGetParNames(p1);
correlation[2,1]
print pvLength(p1);
    1.0000
```

Also, pvTest tests an instance to make sure it is properly constructed. pvCreate generates an initialized instance, and pvGetIndex returns the indices of the parameters of an input matrix in the parameter vector. This last function is most useful when constructing linear constraint indices for the optimization programs.

### 17.2 Fast Pack Functions

Unpacking matrices using matrix names is slow because it requires a string search through a string array of names. A set of special packing functions are provided that avoid the search altogether. These functions use a "table" of indices that you specify to find the matrix in the $\mathbf{P V}$ instance. For example:

```
struct PV p1;
p1 = pvCreate;
y = rndn (4,1);
x = rndn (4,4);
```

```
p1 = pvPacki(p1,y, "Y",1);
p1 = pvPacki (p1,x, "X",2);
print pvUnpack (p1,1);
    . 3422
    .0407
    .5611
    .0953
print pvUnpack(p1, "Y");
    . 3422
    .0407
    .5611
    .0953
```

The call to pvPacki puts an entry in the table associating the matrix in its second argument with the index 1. As indicated above the matrix can be unpacked either by index or by name. Unpacking by index, however, is much faster than by name.

Note that the matrix can be unpacked using either the index or the matrix name.
There are index versions of all four of the packing functions, pvPacki, pvPackmi, pvPacksi, and pvPacksmi.

### 17.3 The DS Data Structure

An instance of the DS data structure contains the following members:

```
struct DS d0;
```

$$
\begin{array}{ll}
\text { d0.dataMatrix } & \text { MxK matrix, data } \\
\text { d0.dataArray } & \text { N-dimensional array, data } \\
\text { d0.type } & \text { scalar }
\end{array}
$$

$$
\begin{array}{ll}
\text { d0.dname } & \text { string } \\
\text { d0.vnames } & \text { string array }
\end{array}
$$

The definition and use of the elements of $\mathbf{d} \mathbf{0}$ are determined by the particular application and are mostly up to the user. A typical use might use a vector of structures. For example, suppose the objective function requires a vector of observations on a dependent variable as well as on K independent variables. Then:

```
struct DS dO;
dO = dsCreate;
y = rndn (20,1);
x = rndn (20,5);
d0 = reshape (d0,2,1);
d0[1].dataMatrix = y;
d0[2].dataMatrix = X;
```

The d0 instance would be passed to the optimization program which then passes it to your procedure computing the objective function. For example:

```
proc
    lpr(struct PV p1, struct DS d1);
    local u;
    u = d0[1].dataMatrix - d0[2].dataMatrix * pvUnpack(p1,
"beta");
    retp(u'u);
endp;
```

A particular application may require setting other members of the DS instance for particular purposes, but in general you may use them for your own purposes. For example, d0.dname could be set to a GAUSS dataset name from which you read the data in the objective function procedure, or d0.vnames could be set to the variable names of the columns of the data stored in d0.dataMatrix, or d0.type could be an indicator variable for the elements of a vector of $\mathbf{D S}$ instances.

The following are complete examples of the use of the PV and DS structures. The first example fits a set of data to the Micherlitz model. It illustrates packing and unpacking by index.

```
#include sqpsolvemt.sdf
struct DS Y;
Y = dsCreate;
Y.dataMatrix = 3.1831
    3.0591
        2.871|
        2.622।
        2.541।
        2.184।
        2.110।
        2.075।
        2.018।
        1.9031
        1.7701
        1.762।
        1.550;
struct DS X;
X = dsCreate;
X.dataMatrix = seqa (1, 1, 13);
struct DS Z;
Z = reshape (Z,2,1);
Z[1] = Y;
Z[2] = X;
struct SQPsolveMTControl c1;
c1 = sqpSolveMTcontrolCreate; // initializes to default val-
ues
c1.bounds = 0~100; // constrains parameters to be
positive
c1.CovType = 1;
```

```
c1.output = 1;
c1.printIters = 0;
c1.gradProc = &grad;
struct PV par1;
par1 = pvCreate;
start = { 2, 4, 2 };
par1 = pvPacki(par1,start, "Parameters",1);
struct SQPsolveMTout out1;
out1 = SQPsolveMT(&Micherlitz,par1,Z,c1);
estimates = pvGetParVector(out1.par);
print " parameter estimates ";
print estimates;
print;
print " standard errors ";
print sqrt(diag(out1.moment));
proc Micherlitz(struct PV parl,struct DS Z);
    local p0,e,s2;
    p0 = pvUnpack (par1,1);
    e = Z[1].dataMatrix - p0[1] - p0[2]*exp(-p0[3]
    *Z[2].dataMatrix);
        s2 = moment (e,0) / (rows (e) -1);
    retp( (2/rows (e))*(e.*e/s2 + ln(2*pi*s2)));
endp;
proc grad(struct PV par1, struct DS Z);
    local p0,e,e1,e2,e3,w,g,s2;
    p0 = pvUnpack (par1,1);
    w = exp (-p0[3]*Z[2].dataMatrix);
    e = z[1].dataMatrix - p0[1] - p0[2] * w;
    s2 = moment (e,0) / rows(e);
    e1 = -ones (rows (e),1);
    e2 = -w;
```

```
    e3 = p0[2]*Z[2].dataMatrix.**W;
    w =(1 - e.*e / s2) / rows(e);
    g = e.*e1 + w* (e'e1);
    g = g ~ (e.*e2 + w* (e'e2));
    g = g ~ (e.*e3 + w* (e'e3));
    retp(4*g/(rows (e)*s2));
endp;
```

This example estimates parameters of a "confirmatory factor analysis" model.

```
#include sqpsolvemt.sdf
lambda ={ 1.0 0.0,
        0.5 0.0,
        0.0 1.0,
        0.0 0.5 };
lmask = { 0 0,
    1 0,
    0 0,
    0 1 };
phi}={1.0 0.3
        0.3 1.0 };
theta}={0.60.0 0.0 0.0
    0.0 0.6 0.0 0.0,
    0.0 0.0 0.6 0.0,
    0.0 0.0 0.0 0.6 };
tmask}={1000
    0 1 0 0,
    0 0 1 0,
    0 0 0 1 };
struct PV par0;
par0 = pvCreate;
par0 = pvPackm(par0,lambda, "lambda",lmask);
par0 = pvPacks (par0,phi, "phi");
par0 = pvPacksm(par0,theta, "theta",tmask);
struct SQPsolveMTControl c0;
```

```
c0 = sqpSolveMTcontrolCreate;
lind = pvGetIndex(par0, "lambda"); // get indices of lambda
parameters // in parameter vector
tind = pvGetIndex(par0, "theta"); // get indices of theta
parameters // in parameter vector
c0.bounds = ones(pvLength(par0),1).*(-1e250~1e250);
c0.bounds[lind,1] = zeros(rows(lind),1);
c0.bounds[lind,2] = 10*ones(rows(lind),1);
c0.bounds[tind,1] = .001*ones(rows (tind),1);
c0.bounds[tind,2] = 100*ones(rows(tind),1);
c0.ineqProc = &ineq;
c0.covType = 1;
struct DS dO;
dO = dsCreate;
d0.dataMatrix = loadd("maxfact");
struct SQPsolveMTOut out0;
out0 = SQPsolveMT(&lpr,par0,d0,c0);
lambdahat = pvUnpack(out0.par, "lambda");
phihat = pvUnpack(out0.par, "phi");
thetahat = pvUnpack(out0.par, "theta");
print "estimates";
print;
print "lambda" lambdahat;
print;
print "phi" phihat;
print;
print "theta" thetahat;
struct PV stderr;
```

```
stderr = out0.par;
if not scalmiss(out0.moment);
    stderr = pvPutParVector(stderr,sqrt(diag(out0.moment)));
    lambdase = pvUnpack(stderr, "lambda");
    phise = pvUnpack(stderr, "phi");
    thetase = pvUnpack(stderr, "theta");
    print"standard errors";
    print;
    print"lambda" lambdase;
    print;
    print"phi" phise;
    print;
    print"theta" thetase;
endif;
proc lpr(struct PV par1, struct DS datal);
    local lambda,phi,theta,sigma,logl;
    lambda = pvUnpack(par1, "lambda");
    phi = pvUnpack(par1, "phi");
    theta = pvUnpack(par1, "theta");
    sigma = lambda*phi*lambda' + theta;
    logl = -lnpdfmvn(data1.dataMatrix,sigma);
    retp(logl);
endp;
proc ineq(struct PV par1, struct DS data1);
    local lambda,phi,theta,sigma,e;
    lambda = pvUnpack (par1, "lambda");
    phi = pvUnpack(par1, "phi");
    theta = pvUnpack (par1, "theta");
    sigma = lambda*phi*lambda' + theta;
    e = eigh(sigma) - .001; // eigenvalues of sigma
    e = e | eigh(phi) - .001; // eigenvalues of phi
    retp(e);
endp;
```


## 18 Multi-Threaded Programming in GAUSS

The term thread comes from the phrase "thread of execution"--simply, it denotes a section of code that you want to execute. A single-threaded program has only one thread of execution, i.e., the program itself. A multi-threaded program is one that can have multiple threads--sections of code--executing simultaneously. Since these threads are part of the same program, they share the same workspace, and see and operate on the same symbols. Threads allow you to take full advantage of the hardware processing resources available on hyper-threaded, multi-core, and multi-processor systems, executing independent calculations simultaneously, combining and using the results of their work when done.

### 18.1 The Functions

GAUSS includes four keywords for multi-threading your programs:

| ThreadStat | Marks a single statement to be <br> executed as a thread. |
| :--- | :--- |
| ThreadBegin | Marks the beginning of a block <br> of code to be executed as a <br> thread. |

ThreadEnd<br>threadfor, threadendfor ThreadJoin

Marks the end of a block of code to be executed as a thread.

Begins a parallel for loop.
Completes the definition of a set of threads, waits until they are done.

ThreadStat defines a single statement to be executed as a thread:

```
ThreadStat n = m'm;
```

ThreadBegin and ThreadEnd define a multi-line block of code to be executed as a thread:

```
ThreadBegin;
    y = x'x;
    z = y'y;
```

ThreadEnd;

Together these define sets of threads to be executed concurrently:

```
ThreadStat n = m'm;
ThreadBegin; // Thread 2
    // Thread 1
    y = x'x;
    z = y'y;
ThreadEnd;
ThreadBegin; // Thread 3
    q = r'r;
    r = q'q;
ThreadEnd;
ThreadStat p = o'o; // Thread 4
```

Finally, ThreadJoin completes the definition of a set of threads. It waits for the threads in a set to finish and rejoin the creating (the parent) thread, which can then continue, making use of their individual calculations:

```
ThreadBegin;
    y = x'x;
    z = y'y;
ThreadEnd;
ThreadBegin; // Thread 2
    q = r'r;
    r = q'q;
ThreadEnd;
ThreadStat n = m'm; // Thread 3
ThreadStat p = o'o; // Thread 4
ThreadJoin; // waits for Threads 1-4 to finish
b = z + r + n'p; // Using the results
```


### 18.2 GAUSS Threading Concepts

This is really the one and only thing you need to know about threads: threads are separate sections of the same program, executing simultaneously, operating on the same data. In fact, it's so fundamental it's worth saying again: threads are separate sections of code in a program, running at the same time, using the same workspace, referencing and operating on the same symbols.

This raises basic issues of workflow and data integrity. How do you manage the creation and execution of threads, and make use of the work they do? And how do you maintain data integrity? (You do not want two threads assigning to the same symbol at the same time.)

To handle thread workflow, GAUSS employs a split-and-join approach. At various points in your program (as many as you like), you define a set of threads that will be created and run as a group. When created, the threads in the set execute simultaneously, each doing useful work. The parent thread waits for the created threads to complete, then continues, the results of their work now available for further use.

To maintain data integrity, we introduce the writer-must-isolate (informally, the any-thread-can-read-unless-some-thread-writes) programming rule. That is to say, symbols that are read from but not assigned to can be referenced by as many threads in a set as you like. Symbols that are assigned to, however, must be wholly owned by a single thread. No other thread in the set can reference that symbol. They cannot assign to it, nor can they read from it. They cannot refer to it at all.

Note: the writer-must-isolate rule only applies to the threads within a given set (including any child thread sets they may create). It does not apply between thread sets that have no chance of running simultaneously.

For threads defined in the main code, the writer-must-isolate rule applies to the global symbols. For threads defined in procedures or keywords, it applies to the global symbols, local symbols, and the procedure/keyword arguments.

### 18.3 Coding With Threads

There are two main points to coding with threads.

1. You can define threads anywhere.

You can define them in the main code, you can define them in proc's and keyword's, and yes, you can define them inside other threads.
2. You can call proc's and keyword's from threads.

This is what really ties everything together. You can call a proc from a thread, and that proc can create threads, and any of those threads can call proc's, and any of those proc's can create threads, and ... you get the picture.

So--you can do things like this:

```
q = chol(b);
ThreadBegin;
    x = q + m;
    ThreadBegin;
            y = x'x;
            z = q'm;
```

```
    ThreadEnd;
    ThreadBegin;
        a = b + x;
        c = a + m;
    ThreadEnd;
    ThreadJoin;
q = m'c;
ThreadEnd;
ThreadBegin;
    ThreadStat r = m'm;
    ThreadStat s = m + inv(b);
    ThreadJoin;
t = r's;
ThreadEnd;
ThreadJoin;
x = r+s+q+z-t;
```

More importantly, you can do things like this:

```
proc
    bef(x);
    local y,t;
    ThreadStat y = nof(x);
    ThreadStat t = dof(x'x);
    ThreadJoin;
    t = t+y;
    retp(t);
endp;
proc abr(m);
    local x,y,z,a,b;
    a = m'm;
    ThreadStat x = inv(m);
    ThreadStat y = bef(m);
    ThreadStat z = dne(a);
    ThreadJoin;
```

```
        b = chut(x,y,z,a);
        retp(inv(b));
endp;
s = rndn(500,500);
ThreadStat t = abr(s);
ThreadStat q = abr(s^2);
ThreadStat r = che(s);
ThreadJoin;
w = del (t,q,r);
print w[1:10,1:10];
```

This means you can multi-thread anything you want, and call it from anywhere. You can multi-thread all the proc's and keyword's in your libraries, and call them freely anywhere in your multi-threaded programs.

### 18.4 Coding Restrictions

A few points on coding restrictions. First, you can't interlace thread definition statements and regular statements. You can't do this:

```
ThreadStat a = b'b;
n = q;
ThreadStat c = d'd;
ThreadJoin;
```

Or this:

```
if k == 1;
    ThreadStat a = b'b;
elseif k == 2;
    ThreadStat a = c'c;
endif;
if j == 1;
    ThreadStat d = e'e;
elseif j == 2;
```

```
    ThreadStat d = f'f;
endif;
ThreadJoin;
```

Each set of threads is defined as a group, and always completed by a ThreadJoin, like this:

```
n = q;
ThreadStat a = b'b;
ThreadStat c = d'd;
ThreadJoin;
```

And this:

```
ThreadBegin;
    if k == 1;
        a = b'b;
    elseif k == 2;
        a = c'c;
    endif;
ThreadEnd;
ThreadBegin;
    if j == 1;
        d = e'e;
    elseif j == 2;
        d = f'f;
    endif;
ThreadEnd;
ThreadJoin;
```

Second--as stated above, you can reference read-only symbols in as many threads within a set as you like, but any symbols that are assigned to must be wholly owned by a single thread. A symbol that is assigned to by a thread cannot be written or read by any other thread in that set. This is the writer-must-isolate rule.

So, you can do this:

```
ThreadStat x = y'y;
ThreadStat z = y+y;
ThreadStat a = b-y;
ThreadJoin;
```

You cannot do this:

```
ThreadStat x = y'y;
Threadstat z = x'x;
ThreadStat a = b-y;
ThreadJoin;
```

This is because the threads within a set run simultaneously. Thus, there is no way of knowing when an assignment to a symbol has taken place, no way of knowing in one thread the "state" of a symbol in another.

Let's revisit the nested thread example for a minute and see how the writer-must-isolate rule applies to it :

```
q = chol(b);
ThreadBegin;
Th2
    x = q + m;
    ThreadBegin; // Th1.1: isolates y,z from 1.2
        y = x'x;
        z = q'm;
    ThreadEnd;
    ThreadBegin;
        a = b + x;
        c = a + m;
    ThreadEnd;
    ThreadJoin; // Joins 1.1, 1.2
    q = m'c;
ThreadEnd;
ThreadBegin;
ThreadStat r = m'm; // Th2.1: isolates r from 2.2
ThreadStat // Th2.2: isolates s from 2.1
// main code, no threads yet
// Th1: isolates x,y,z,a,c,q from
    // Th1.2: isolates a,c from 1.1
// Th2: isolates r,s,t from Th1
```

```
        s = m + inv(b);
    ThreadJoin; // Joins 2.1, 2.1
    t = r's;
ThreadEnd;
ThreadJoin; // Joins Th1, Th2
x = r+s+q+z-t;
```

The main point here is that any symbols a thread or its children assign to must be isolated from all the other threads (and their children) of the same nesting level in that set. On the other hand, the children of a thread can freely read/write symbols that are read/written by their parent, because there is no risk of simultaneity; they must only isolate written symbols from their siblings and siblings' offspring.

If you break the writer-must-isolate rule, your program (and probably GAUSS) will crash. Worse, until it crashes, it will be happily producing indeterminate results.

Finally--the ThreadEnd command is what tells a thread to terminate, so you mustn't write code that keeps a thread from reaching it. For example, don't retp from the middle of a thread:

```
ThreadStat m = imt(9);
ThreadBegin;
    x = q[1];
    if x = 1;
        retp(z);
    else;
        r = z + 2;
    endif;
ThreadEnd;
ThreadJoin;
```

And don't use goto to jump into or out of the middle of a thread:

```
retry:
ThreadBegin;
    { err, x } = fna(q);
    if err;
```

```
        goto badidea;
    endif;
    x = fnb (x);
ThreadEnd;
ThreadStat y = fnb(y);
ThreadJoin;
z = fnc(x,y);
save z;
end;
badidea:
errorlog "Error computing fna(q)";
q = fnd(q);
goto retry;
```

Basically, don't do anything that will keep a thread from reaching its ThreadEnd command. That's the only way it knows its work is done. end and stop are okay to call, though--they will bring the program to an end as usual, and terminate all running threads in the process.
(You can use goto and labels to jump around within a thread--that is, within the confines of a ThreadBegin/ThreadEnd pair.)

### 18.5 Parallel for Loops

The GAUSS threadFor keyword allows you to create compact code that will run in parallel. In order for a for loop construct to execute correctly concurrently in separate threads, the threadFor loop has a few special rules. In this section, we will explain these rules by working through a simple example.

### 18.5.1 Basic syntax

The syntax of a threadFor loop is the same as a standard for loop:

```
threadFor loop_counter(start, stop, step);
    //loop bodythreadEndFor;
```

Below is one of the most simple, specific examples of a threadFor loop. It will print out the loop counter from one to ten:

```
threadFor i(1, 10, 1);
    print i;
threadEndFor;
```


### 18.5.2 Single threaded example

As we learn how to use threadFor loops, we will illustrate the concepts by converting the following single-threaded for loop to a threadFor loop:

```
//Using the trapezoidal rule to integrate//the cosine func-
tion from 0 to 0.5
n_slices = 1000;
a = 0;
b = 0.5;
h = (a - b) ./ n_slices;
approx = zeros(n_slices + 1, 1);
approx[1] = (\boldsymbol{cos}(a) + cos(b)) ./ 2;
for i(1, n_slices, 1);
    x_tmp = a + i*h;
    approx[i+1] = cos(x_tmp);
endfor;
```

```
final = sumc(approx) .* h;
```


### 18.5.3 threadFor variables

A threadFor loop contains three types of variables: temporary variables, broadcast variables and slice variables. The next sections will explain how they are defined and how they operate. Before we start it is important to point out that the assignment of a variable to a category is permanent for the remainder of the threadFor loop. Variables cannot change to different categories during a threadFor loop.

### 18.5.4 Temporary variables

One of the most important rules of parallel programming is that you should not assign to the same global variable from multiple threads that are running at the same time. This can cause a "race condition" in which the output from your program will depend upon which thread "wins the race" and assigns to the variable first. It can also cause your program to crash if they try to assign at the same time.

With that in mind, it may appear that we have a problem when we try to convert the first line inside the for loop from our program above to a threadFor loop:

```
threadFor i(1, n slices, 1);
    x_tmp = a + i*h;
    approx[i+1] = cos(x_tmp);
threadEndFor;
```

In the sequential version, every iteration of the for loop is certainly assigning to the same global variable, x_tmp. While we might expect that this is not allowed in the threadFor loop, it is actually acceptable.

The reason that this works is because GAUSS will make a separate temporary version of 'x_tmp' for each thread. When a variable in a threadFor loop is assigned to in it's entirety, not simply a portion of it by index, it becomes a temporary variable.

The rules for temporary variables are:

1. A temporary variable may have any legal variable name

In our example above, our variable name ended in " tmp", but this is not required.
2. A temporary variable is not the same as a variable with the same name outside the 'threadFor' loop.

Temporary variables exist only in the scope of the threadFor loop. They do not start the loop with any value and their value is not available outside the threadFor loop. For example:

```
x = 100;
threadFor i(1, 4, 1);
    x = i;
threadEndFor;
print "x = " x;
```

will print out:

```
x = 100
```

3. The first reference to a temporary variable must be an assignment.

Since temporary variables do not exist outside the loop and are not related to variables outside the loop with the same name, they will not have a value until they are assigned to inside of the 'threadFor' loop. For example:

```
x = 100;
threadFor i(1, 4, 1);
```

```
    a = x; //'x' does not have a value until the next line
    x = i; //This line makes 'x' a temporary
variablethreadEndfor;
```


### 18.5.5 Broadcast variables

```
threadFor i(1, n_slices, 1);
    x_tmp = a + i*h; //'a' and 'h' are broadcast variables
    approx[i+1] = cos(x_tmp);
threadEndFor;
```

Besides 'x_tmp' which we discussed above, were two other variables on the first line of our loop, 'h' and 'a' which were only referenced. They were not assigned to on that line or anywhere else in the loop. These variables are called broadcast variables, because the same value is "broadcast" to every thread. If a variable is not assigned to and it is not the loop counter, it will be, by default, a broadcast variable.

### 18.5.6 Slice variables

Next we will look at the indexed assignment of 'approx' on the second line inside our loop.

```
threadFor i(1, n_slices, 1);
    x_tmp = a + i*h; //'a' and 'h' are broadcast variables
    approx[i+1] = cos(x_tmp);
threadEndFor;
```

Earlier we discussed that you are not allowed to assign to the same global variable from more than one thread at one time. It is allowable to assign to portions of a variable, however, as long as multiple threads never assign to the same location.

If a variable is assigned to by index it becomes a slice variable. In order to ensure correct multi-threaded programs, the rules for 'slice variables' are:

1. The dimension that is assigned to using the threadFor loop counter defines the slice. The index into this dimension may contain, in addition to the loop counter, a commutative operator, such as + , - or .*, a constant or a variable that is constant during the threadFor loop. For example, assuming that ' $i$ ' is the threadFor loop counter and that 'approx' is an nx1 vector, any of these statements would be correct:
```
approx[i] = cos (x_tmp);
approx[i+1]=\operatorname{cos}(x_tmp);
approx[n-i] = cos (x_tmp);
```

These statements, however, would be incorrect:

```
approx[maxc(idx)] = cos(x_tmp); //function call cannot be
an index
approx[8] = cos(x_tmp); //each iteration would assign to
the same location
approx[i:i+5] = cos(x_tmp); //ranges are not allowed to
define the slice
```

2. The dimension or dimensions that do not define the slice may be assigned to freely. These statements would all be legal:
```
approx[i, maxc(idx) = cos(x_tmp);
approx[i+1, .] = cos(x_tmp);
approx[i+3, 1:10] = cos(x_tmp);
```


### 18.5.7 Reduction variables

A reduction variable is a variable that accumulates the result of a commutative operator over all the iterations of a threadFor loop. For example, if we changed our example loop to this:

```
approx = (\boldsymbol{cos}(a)+\boldsymbol{cos}(b))./ 2;
for i(1, n_slices, 1);
    x_tmp = a + i*h;
    approx = approx + cos (x_tmp);
endfor;
```

then 'approx' would be a an reduction variable. Reduction variables are not yet supported in GAUSS threadFor statements as of the release of this version. To perform a reduction, instead assign the result from each iteration to an element of an array and perform a 'sumc' or 'prodc' on this final vector as is shown in this example.

### 18.5.8 Categorizing the variables in our example

Take a moment and look through the loop below. Can you identify which classification each of the variables belongs to? Based upon what we have covered, is this a legal threadFor loop?

```
for i(1, n_slices, 1);
    x_tmp = a + i*h;
    approx[i+1] = cos(x_tmp);
endfor;
```

After you have tried to categorize the variables, look at the table below to compare your answers and see if your reasoning is correct:

| i | The loop counter. |
| :--- | :--- |
| $x_{-}$tmp | Temporary variable, it is assigned to in its entirety. |
| a | Broadcast variable, it is never assigned to. |
| h | Broadcast variable, it is never assigned to. |
| approx | Slice variable, it is assigned by index, using the loop <br> counter. |

To the second question, yes the code above is a legal threadFor loop. Below is the entire program converted to use threadFor.

```
//Using the trapezoidal rule to integrate//the cosine func-
tion from 0 to 0.5
n_slices = 1000;
a = 0;
b = 0.5;
h = (a - b) ./ n_slices;
approx = zeros(n_slices + 1, 1);
approx[1] = (\boldsymbol{cos}(a)+\operatorname{cos}(b)) ./ 2;
threadFor i(1, n_slices, 1);
    x_tmp = a + i*h;
    approx[i+1] = cos(x_tmp);
threadEndFor;
final = sumc(approx) .* h;
```


### 18.6 Controlling thread count

By default when dividing up the iterations of a threadFor loop, GAUSS will create one thread for each core on your machine. This is a good setting in many cases. You may, however, override this behavior if you like with the sysstate command, case 42. Here is an example of setting the number of threads that threadFor will create to 16:

```
new_num = 16;
old_num = sysstate(42,new_num);
```

After the above code, old num will be a $2 \times 1$ vector. The first element will be the old thread count used by threadFor and the second element is reserved for future use.

## 19 Libraries

The GAUSS library system allows for the creation and maintenance of modular programs. The user can create "libraries" of frequently used functions that the GAUSS system will automatically find and compile whenever they are referenced in a program.

### 19.1 Autoloader

The autoloader resolves references to procedures, keywords, matrices, and strings that are not defined in the program from which they are referenced. The autoloader automatically locates and compiles the files containing the symbol definitions that are not resolved during the compilation of the main file. The search path used by the autoloader is first the current directory, and then the paths listed in the src_path configuration variable in the order they appear. src_path can be defined in the GAUSS configuration file.

### 19.1.1 Forward References

When the compiler encounters a symbol that has not previously been defined, that is called a "forward reference." GAUSS handles forward references in two ways, depending on whether they are "left-hand side" or "right-hand side" references.

## Left-Hand Side

A left-hand side reference is usually a reference to a symbol on the left-hand side of the equal sign in an expression.

$$
x=5 ;
$$

Left-hand side references, since they are assignments, are assumed to be matrices. In the statement above, $x$ is assumed to be a matrix and the code is compiled accordingly. If, at execution time, the expression actually returns a string, the assignment is made and the type of the symbol $x$ is forced to string.

Some commands are implicit left-hand side assignments. There is an implicit left-hand side reference to $x$ in each statement below:

```
clear x;
load x;
open x = myfile;
```


## Right-Hand Side

A right-hand side reference is usually a reference to a symbol on the right-hand side of the equal sign in an expression such as:

```
z = 6;
y = z + dog;
print y;
```

In the program above, since dog is not previously known to the compiler, the autoloader will search for it in the active libraries. If it is found, the file containing it will be compiled. If it is not found in a library, the autoload/autodelete state will determine how it is handled.

### 19.1.2 The Autoloader Search Path

If the autoloader is OFF, no forward references are allowed. Every procedure, matrix, and string referenced by your program must be defined before it is referenced. An external statement can be used above the first reference to a symbol, but the definition of the symbol must be in the main file or in one of the files that are \#include'd. No global symbols are deleted automatically.

If the autoloader is ON, GAUSS searches for unresolved symbol references during compilation using a specific search path as outlined below. If the autoloader is OFF, an Undefined symbol error message will result for right-hand side references to unknown symbols.

When autoload is ON, the autodelete state controls the handling of references to unknown symbols.

The following search path will be followed to locate any symbols not previously defined:

## Autodelete ON

1. user library
2. user-specified libraries.
3. gauss library
4. current directory, then src_path for files with a $\cdot g$ extension.

Forward references are allowed and.$g$ files need not be in a library. If there are symbols that cannot be found in any of the places listed above, an Undefined symbol error message will be generated and all uninitialized variables and all procedures with global references will be deleted from the global symbol table. This autodeletion process is transparent to the user, since the symbols are automatically located by the autoloader the next time the program is run. This process results in more compile time, which may or may not be significant, depending on the speed of the computer and the size of the program.

## Autodelete OFF

1. user library
2. user-specified libraries.
3. gauss library

All . g files must be listed in a library. Forward references to symbols that are not listed in an active library are not allowed. For example:

```
x = rndn(10,10);
y = sym(x); // Forward reference to sym
proc sym(x);
    retp(x+x');
endp;
```

Use an external statement for anything referenced above its definition if autodelete is OFF:

```
external proc sym;
x = rndn(10,10);
y = sym(x);
proc sym(x);
    retp(x+x');
endp;
```

When autodelete is OFF, symbols not found in an active library will not be added to the symbol table. This prevents the creation of uninitialized procedures in the global symbol table. No deletion of symbols from the global symbol table will take place.

## Libraries

The first place GAUSS looks for a symbol definition is in the "active" libraries. A
GAUSS library is a text file that serves as a dictionary to the source files that contain the symbol definitions. When a library is active, GAUSS will look in it whenever it is
looking for a symbol it is trying to resolve. The library statement is used to make a library active. Library files should be located in the subdirectory listed in the lib_ path configuration variable. Library files have an .lcg extension.

Suppose you have several procedures that are all related and you want them all defined in the same file. You can create such a file, and, with the help of a library, the autoloader will be able to find the procedures defined in that file whenever they are called.

First, create the file that is to contain your desired procedure definitions. By convention, this file is usually named with a . src extension, but you may use any name and any file extension. In this file, put all the definitions of related procedures you wish to use. Here is an example of such a file. It is called norm.src:

```
/*
** norm.src
**
** This is a file containing the definitions of three
** procedures which return the norm of a matrix x.
** The three norms calculated are the 1-norm, the
** inf-norm and the E-norm.
*/
proc onenorm(x);
    retp (maxc (sumc (abs (x))));
endp;
proc infnorm(x);
    retp (maxc (sumc (abs (x'))));
endp;
proc Enorm(x);
    retp (sumc (sumc (x.**)));
endp;
```

Next, create a library file that contains the name of the file you want access to, and the list of symbols defined in it. This can be done with the lib command. (For details, see lib in the GAUSS LANGUAGE REFERENCE.)

A library file entry has a filename that is flush left. The drive and path can be included to speed up the autoloader. Indented below the filename are the symbols included in the file. There can be multiple symbols listed on a line, with spaces between. The symbol type follows the symbol name, with a colon delimiting it from the symbol name. The valid symbol types are:

```
fn user-defined single line function.
keyword
proc
matrix
array
string
sparse matrix
struct
```

user-defined single line function. keyword. procedure. matrix, numeric or character.

N -dimensional array. string.
sparse matrix.
structure.

A structure is always denoted by struct followed by the structure type name.
If the symbol type is missing, the colon must not be present and the symbol type is assumed to be proc. Both library files below are valid:

## Example 1

```
/*
** math
    **
    ** This library lists files and procedures for mathematical
    routines.
    */
    norm.src
    onenorm:proc infnorm:proc Enorm:proc
```

```
complex.src
    cmmult:proc cmdiv:proc cmadd:proc cmsoln:proc
poly.src
    polychar:proc polyroot:proc polymult:proc
```


## Example 2

```
/*
** math
**
** This library lists files and procedures for mathematical
routines.
* /
c:\gauss\src\norm.src
    onenorm : proc
    infnorm : proc
    Enorm : proc
c:\gauss\src\complex.src
    cmmult : proc
    cmdiv : proc
    cmadd : proc
    cmsoln : proc
c:\gauss\src\fcomp.src
    feq : proc
    fne : proc
    flt : proc
    fgt : proc
    fle : proc
    fge : proc
c:\gauss\src\fcomp.dec
    fcmptol : matrix
```

Once the autoloader finds, via the library, the file containing your procedure definition, everything in that file will be compiled. For this reason, you should combine related procedures in the same file in order to minimize the compiling of procedures not needed by
your program. In other words, you should not combine unrelated functions in one . src file because if one function in a . src file is needed, the whole file will be compiled.

## User Library

This is a library for user-created procedures. If the autoloader is ON, the user library is the first place GAUSS looks when trying to resolve symbol references.

You can update the user library with the lib command as follows:

```
lib user myfile.src
```

This will update the user library by adding a reference to myfile.src.
No user library is shipped with GAUSS. It will be created the first time you use the lib command to update it.

For details on the parameters available with the lib command, see the GAUSS LANGUAGE REFERENCE.

## . $g$ Files

If autoload and autodelete are ON and a symbol is not found in a library, the autoloader will assume it is a procedure and look for a file that has the same name as the symbol and a . g extension. For example, if you have defined a procedure called square, you could put the definition in a file called square.g in one of the subdirectories listed in your src_path. If autodelete is OFF, the . $g$ file must be listed in an active library; for example, in the user library.

### 19.2 Global Declaration Files

If your application makes use of several global variables, create a file containing declare statements. Use files with the extension . dec to assign default values to global matrices and strings with declare statements and to declare global N-dimensional arrays, sparse matrices, and structures, which will be initialized as follows:

## Variable Type

N -dimensional array
sparse matrix
structure $\quad 1 \times 1$ structure containing empty and/or zeroed out members

In order to declare structures in a . dec file, you must \#include the file(s) containing the definitions of the types of structures that you wish to declare at the top of your . dec file. For example, if you have the following structure type definition in a file called mystruct.sdf:

```
struct mystruct {
    matrix m;
    array a;
    scalar scal;
    string array sa;
};
```

You could declare an instance of that structure type, called ms, in a . dec file as follows:

```
#include mystruct.sdf
declare struct mystruct ms;
```

See declare in the COMMAND REFERENCE for more information.
A file with a .ext extension containing the same symbols in external statements can also be created and \#include'd at the top of any file that references these global variables. An appropriate library file should contain the name of the . dec files and the names of the globals they declare. This allows you to reference global variables across source files in an application.

Here is an example that illustrates the way in which . dec, .ext, . lcg and .src files work together. Always begin the names of global matrices or strings with '_' to distinguish them from procedures.
.src File:

```
/*
** fcomp.src
**
** These functions use _fcmptol to fuzz the comparison oper-
ations
** to allow for roundoff error.
**
** The statement: y = feq(a,b);
**
** is equivalent to: y = a eq b;
**
** Returns a scalar result, 1 (true) or 0 (false)
**
** y = feq(a,b);
** y = fne(a,b);
*/
    #include fcomp.ext
proc feq(a,b);
    retp(abs(a-b) <= _fcmptol);
endp;
proc fne(a,b);
    retp(abs(a-b) > _fcmptol);
endp;
```

. dec File:

```
/*
** fcomp.dec - global declaration file for fuzzy
comparisons.
*/
```

```
declare matrix _fcmptol != 1e-14;
```

.ext File:

```
/*
** fcomp.ext - external declaration file for fuzzy
comparisons.
* /
external matrix _fcmptol;
```

. lcg File:

```
/*
** fcomp.lcg - fuzzy compare library
* /
fcomp.dec
    fcmptol:matrix
fcomp.src
    feq:proc
    fne:proc
```

With the exception of the library (.lcg) files, these files must be located along your src_path. The library files must be on your lib_path. With these files in place, the autoloader will be able to find everything needed to run the following programs:

```
library fcomp;
x = rndn (3,3);
xi = inv(x);
xix = xi*x;
if feq(xix, eye(3));
    print "Inverse within tolerance.";
else;
    print "Inverse not within tolerance.";
endif;
```

If the default tolerance of $1 \mathrm{e}-14$ is too tight, the tolerance can be relaxed:

```
library fcomp;
x = rndn (3,3);
xi = inv(x);
xix = xi*x;
    fcmptol = 1e-12; // reset tolerance
if feq(xix, eye(3));
    print "Inverse within tolerance.";
else;
    print "Inverse not within tolerance.";
endif;
```


### 19.3 Troubleshooting

Below is a partial list of errors you may encounter in using the library system, followed by the most probable cause.

## (4) : error G0290 : '/gauss/lib/prt.lcg' : Library not found

The autoloader is looking for a library file called prt. 1 cg , because it has been activated in a library statement. Check the subdirectory listed in your lib_ path configuration variable for a file called prt.lcg.

## (0) : error G0292 : 'prt.dec' : File listed in library not found

The autoloader cannot find a file called prt. dec. Check for this file. It should exist somewhere along your src_path, if you have it listed in prt.lcg

Undefined symbols:
PRTVEC /gauss/src/tstprt.g(2)
The symbol prtvec could not be found. Check if the file containing prtvec is in the src_path. You may have not activated the library that contains your symbol definition. Do so in a library statement.

```
/gauss/src/prt.dec(3) : Redefinition of ' vnames'
(proc)__vnames being declared external matrix
```

You are trying to illegally force a symbol to another type. You probably have a name conflict that needs to be resolved by renaming one of the symbols.

```
/gauss/lib/prt.lcg(5) : error G0301 : 'prt.dec' :
Syntax error in library
Undefined symbols:
    VNAMES /gauss/src/prt.src(6)
```

Check your library to see that all filenames are flush left and that all the symbols defined in that file are indented by at least one space.

### 19.3.1 Using . dec Files

Below is some advice you are encouraged to follow when constructing your own library system:

- Whenever possible, declare variables in a file that contains only declare statements. When your program is run again without clearing the workspace, the file containing the variable declarations will not be compiled and declare warnings will be prevented.
- Provide a function containing regular assignment statements to reinitialize the global variables in your program if they ever need to be reinitialized during or between runs. Put this in a separate file from the declarations:

```
proc (0) = globset;
        vname = "X";
        con = 1;
    _row = 0;
    title = "";
endp;
```

- Never declare any global in more than one file.
- To avoid meaningless redefinition errors and declare warnings, never declare a global more than once in any one file. Redefinition error messages and declare warnings are meant to help you prevent name conflicts, and will be useless to you if your code generates them normally.

By following these guidelines, any declare warnings and redefinition errors you get will be meaningful. By knowing that such warnings and errors are significant, you will be able to debug your programs more efficiently.

## 20 The Library Tool

Libraries are collections of GAUSS procedures that are grouped together. The GAUSS Library Tool makes it easy for users to create and manage GAUSS libraries. The Library Tool is available on the Source Page and may be opened from the application menu View->Library Tool.

### 20.1 Creating New Libraries



Figure 20.1: Create new library

At the top right corner of the Library Tool is a plus icon $(+)$. Click this icon to create a new library. A file system window will open and ask you to enter a name for the library. Do not add a file extension as GAUSS will automatically add the correct file extension (.lcg).


Figure 20.2: File browser

Once you have create a new empty library, you need to add some files. Click the wrench icon next to the library to which you would like to add a file and select 'Add Files' from the menu. This will open up a file browser window. Locate and select the file or files that you would like to add to the library.


Figure 20.3: Add Files

### 20.2 Loading a Library

Loading a library makes all of its procedures available in GAUSS. It also allows you to navigate to the definition of a procedure by clicking on the name of a procedure and using the hotkey CTRL+F1, or selecting 'Open function definition' from the source editor's context menu.

To load the library, click the wrench icon and select 'Load Library' from the menu. The newly loaded library's name will be moved towards the top of the list of libraries and it will be bolded.

The library may be unloaded from the same menu accessible from the wrench icon.

### 20.3 Viewing Procedures

Expanding the node of any library in the tree will reveal a list of the included files. Double-clicking on one of the file names will open that file a source editor. Loaded libraries have an additional expandable node for each file. Expand this node to view each procedure stored in that file. Double-click the procedure name to open the file at the location of that procedure.


Figure 20.4: Library Tool Tree

### 20.4 Refreshing a Library

Changes made to files in a library such as adding procedures will be made available to GAUSS. However, to view and navigate correctly to new and changed library files
requires a library refresh. To perform this action, click on the corresponding wrench icon and select 'Refresh'.

## 21 Compiler

GAUSS allows you to compile your large, frequently used programs to a file that can be run over and over with no compile time. The compiled image is usually smaller than the uncompiled source. GAUSS is not a native code compiler; rather, it compiles to a form of pseudocode. The file will have a.$g c g$ extension.

The compile command will compile an entire program to a compiled file. An attempt to edit a compiled file will cause the source code to be loaded into the editor if it is available to the system. The run command assumes a compiled file if no extension is given, and that a file with a .gcg extension is in the src_path. A saveall command is available to save the current contents of memory in a compiled file for instant recall later. The use command will instantly load a compiled program or set of procedures at the beginning of an ASCII program before compiling the rest of the ASCII program file.

Since the compiled files are encoded binary files, the compiler is useful for developers who do not want to distribute their source code.

### 21.1 Compiling Programs

Programs are compiled with the compile command.

### 21.1.1 Compiling a File

Source code program files that can be run with the run command can be compiled to . gcg files with the compile command:

```
compile qxy.e;
```

All procedures, global matrices, arrays, strings and string arrays, and the main program segment will be saved in the compiled file. The compiled file can be run later using the run command. Any libraries used in the program must be present and active during the compile, but not when the program is run. If the program uses the dlibrary command, the . dll files must be present when the program is run and the dlibrary path must be set to the correct subdirectory. This will be handled automatically in your configuration file. If the program is run on a different computer than it was compiled on, the . dll files must be present in the correct location. sysstate (case 24) can be used to set the dlibrary path at run-time.

### 21.2 Saving the Current Workspace

The simplest way to create a compiled file containing a set of frequently used procedures is to use saveall and an external statement:

```
library pgraph;
external proc xy,logx,logy,loglog,hist;
saveall pgraph;
```

Just list the procedures you will be using in an external statement and follow it with a saveall statement. It is not necessary to list procedures that you do not explicitly call, but are called from another procedure, because the autoloader will automatically find them before the saveall command is executed. Nor is it necessary to list every procedure you will be calling, unless the source will not be available when the compiled file is use'd.

Remember, the list of active libraries is NOT saved in the compiled file, so you may still need a library statement in a program that is use'ing a compiled file.

### 21.3 Debugging

If you are using compiled code in a development situation in which debugging is important, compile the file with line number records. After the development is over, you can recompile without line number records if the maximum possible execution speed is important. If you want to guarantee that all procedures contain line number records, put a new statement at the top of your program and turn line number tracking on.

## 22 File I/O

The following is a partial list of the I/O commands in the GAUSS programming language:

| close | Close a file. |
| :--- | :--- |
| closeall | Close all open files. |
| colsf | Number of columns in a file. |
| create | Create GAUSS data set. |
| eof | Test for end of file. |
| fcheckerr | Check error status of a file. |
| fclearerr | Check error status of a file and clear error flag. |
| fflush | Read a line of text from a file's output buffer. |
| fgets | Read multiple lines of text from a file. |
| fgetsa | Read multiple lines of text from a file, discarding <br> newlines. |
| fgetsat |  |


| fgetst | Read a line of text from a file, discarding newline. |
| :---: | :---: |
| fileinfo | Return names and information of files matching a specification. |
| files | Return a directory listing as a character matrix. |
| filesa | Return a list of files matching a specification. |
| fopen | Open a file. |
| fputs | Write strings to a file. |
| fputst | Write strings to a file, appending newlines. |
| fseek | Reposition file pointer. |
| fstrerror | Get explanation of last file I/O error. |
| ftell | Get position of file pointer. |
| getf | Load a file into a string. |
| getname | Get variable names from data set. |
| iscplxf | Return whether a data set is real or complex. |
| load | Load matrix file or small ASCII file (same as loadm). |
| loadd | Load a small GAUSS data set into a matrix. |
| loadm | Load matrix file or small ASCII file. |
| loads | Load string file. |
| open | Open a GAUSS data set. |
| output | Control printing to an auxiliary output file or device. |


| readr | Read a specified number of rows from a file. |
| :--- | :--- |
| rowsf | Number of rows in file. |
| save | Save matrices, strings, procedures. |
| saved | Save a matrix in a GAUSS data set. |
| seekr | Reset read/write pointer in a data set. |
| sortd | Sort a data set. |
| typef | Return type of data set (bytes per element). |
| writer | Write data to a data set. |

### 22.1 ASCII Files

GAUSS has facilities for reading and writing ASCII files. Since most software can also read and write ASCII files, this provides one method of sharing data between GAUSS and many other kinds of programs.

### 22.1.1 Matrix Data

## Reading

Files containing numeric data that are delimited with spaces or commas and are small enough to fit into a single matrix or string can be read with load. Larger ASCII data files can be converted to GAUSS data sets with the ATOG utility program (see ATOG, CHAPTER 28 ). ATOG can convert packed ASCII files as well as delimited files.

For small delimited data files, the load statement can be used to load the data directly into a GAUSS matrix. The resulting GAUSS matrix must be no larger than the limit for a single matrix.

For example,

```
load x[] = dat1.asc;
```

will load the data in the file dat1.asc into an Nx1 matrix $x$. This method is preferred because rows(x) can be used to determine how many elements were actually loaded, and the matrix can be reshape'd to the desired form:

```
load x[] = dat1.asc;
if rows(x) eq 500;
    x = reshape (x,100,5);
else;
    errorlog "Read Error";
    end;
endif;
```

For quick interactive loading without error checking, use

```
load x[100,5] = dat1.asc;
```

This will load the data into a $100 \times 5$ matrix. If there are more or fewer than 500 numbers in the data set, the matrix will automatically be reshaped to $100 \times 5$.

## Writing

To write data to an ASCII file the print or printfm command is used to print to the auxiliary output. The resulting files are standard ASCII files and can be edited with GAUSS's editor or another text editor.

The output and outwidth commands are used to control the auxiliary output. The print or printfm command is used to control what is sent to the output file.

The window can be turned on and off using screen. When printing a large amount of data to the auxiliary output, the window can be turned off using the command

```
screen off;
```

This will make the process much faster, especially if the auxiliary output is a disk file.

It is easy to forget to turn the window on again. Use the end statement to terminate your programs; end will automatically perform screen on and output off.

The following commands can be used to control printing to the auxiliary output:

```
format Specify format for printing a matrix.
output Open, close, rename auxiliary output file or device.
outwidth Set auxiliary output width.
printfm Formatted matrix print.
print Print matrix or string.
screen Turn printing to the window on and off.
```

This example illustrates printing a matrix to a file:

```
format /rd 8,2;
outwidth 132;
output file = myfile.asc reset;
screen off;
print x;
output off;
screen on;
```

The numbers in the matrix $x$ will be printed with a field width of 8 spaces per number, and with 2 places beyond the decimal point. The resulting file will be an ASCII data file. It will have 132 column lines maximum.

A more extended example follows. This program will write the contents of the GAUSS file mydata.dat into an ASCII file called mydata.asc. If there is an existing file by the name of mydata.asc, it will be overwritten:

```
output file = mydata.asc reset;
screen off;
format /rd 1,8;
```

```
open fp = mydata;
do until eof(fp);
    print readr(fp,200);;
endo;
fp = close(fp);
end;
```

The output . . . reset command will create an auxiliary output file called mydata. asc to receive the output. The window is turned off to speed up the process. The GAUSS data file mydata. dat is opened for reading and 200 rows are read per iteration until the end of the file is reached. The data read are printed to the auxiliary output mydata.asc only, because the window is off.

### 22.1.2 General File I/O

getf will read a file and return it in a string variable. Any kind of file can be read in this way as long as it will fit into a single string variable.

To read files sequentially, use fopen to open the file and use fgets, fputs, and associated functions to read and write the file. The current position in a file can be determined with ftell. The following example uses these functions to copy an ASCII text file:

```
proc copy(src, dest);
    local fin, fout, str;
    fin = fopen(src, "rb");
    if not fin;
        retp(1);
    endif;
    fout = fopen(dest, "wb");
    if not fin;
        call close(fin);
        retp(2);
```

```
        endif;
        do until eof(fin);
        str = fgets(fin, 1024);
        if fputs(fout, str) /= 1;
            call close(fin);
            call close(fout);
            retp(3);
        endif;
    endo;
    call close(fin);
    call close(fout);
    retp(0);
endp;
```


### 22.2 Data Sets

GAUSS data sets are the preferred method of storing data contained in a single matrix for use within GAUSS. Use of these data sets allows extremely fast reading and writing of data. Many library functions are designed to read data from these data sets.

If you want to store multiple variables of various types in a single file, see GAUSS Data Archives, Section 22.5.12.

### 22.2.1 Layout

GAUSS data sets are arranged as matrices; that is, they are organized in terms of rows and columns. The columns in a data file are assigned names, and these names are stored in the header, or, in the case of the $v 89$ format, in a separate header file.

The limit on the number of rows in a GAUSS data set is determined by disk size. The limit on the number of columns is limited by RAM. Data can be stored in 2, 4 , or 8 bytes per number, rather than just 8 bytes as in the case of GAUSS matrix files.

The ranges of the different formats are:

| Bytes | Type | Significant Digits | Range |
| :--- | :--- | :--- | :---: |
| 2 | integer | 4 | $-32768<=\mathrm{X}<=32767$ |
| 4 | single | $6-7$ | $8.43 \mathrm{E}-37<=\|\mathrm{X}\|<=3.37 \mathrm{E}+38$ |
| 8 | double | $15-16$ | $4.193 \mathrm{E}-307<=\|\mathrm{X}\|<=1.67 \mathrm{E}+308$ |

### 22.2.2 Creating Data Sets

Data sets can be created with the create or datacreate command. The names of the columns, the type of data, etc., can be specified. (For details, see create in the GAUSS LANGUAGE REFERENCE.)

Data sets, unlike matrices, cannot change from real to complex, or vice-versa. Data sets are always stored a row at a time. The rows of a complex data set, then, have the real and imaginary parts interleaved, element by element. For this reason, you cannot write rows from a complex matrix to a real data set--there is no way to interleave the data without rewriting the entire data set. If you must, explicitly convert the rows of data first, using the real and imag functions (see the GAUSS LANGUAGE REFERENCE), and then write them to the data set. Rows from a real matrix CAN be written to a complex data set; GAUSS simply supplies 0's for the imaginary part.

To create a complex data set, include the complex flag in your create command.

### 22.2.3 Reading and Writing

The basic functions in GAUSS for reading data files are open and readr:

```
open f1 = dat1;
x = readr(f1,100);
```

The call to readr in this example will read in 100 rows from dat1.dat. The data will be assigned to a matrix $x$.
loadd and saved can be used for loading and saving small data sets.

The following example illustrates the creation of a GAUSS data file by merging (horizontally concatenating) two existing data sets:

```
file1 = "dat1";
file2 = "dat2";
outfile = "daty";
open fin1 = ^file1 for read;
open fin2 = ^file2 for read;
varnames = getname(file1)|getname(file2);
otyp = maxc(typef(fin1)|typef(fin2));
create fout = ^outfile with ^varnames,0,otyp;
nr = 400;
do until eof(fin1) or eof(fin2);
    y1 = readr(fin1,nr);
    y2 = readr(fin2,nr);
    r = maxc (rows (y1)|rows (y2));
    y = y1[1:r,.] ~ y2[1:r,.];
    call writer(fout,y);
endo;
closeall fin1,fin2,fout;
```

In this example, data sets dat1.dat and dat2.dat are opened for reading. The variable names from each data set are read using getname, and combined in a single vector called varnames. A variable called otyp is created, which will be equal to the larger of the two data types of the input files. This will insure that the output is not rounded to less precision than the input files. A new data set daty. dat is created using the create . . . with . . . command. Then, on every iteration of the loop, 400 rows are read in from each of the two input data sets, horizontally concatenated, and written out to daty. dat. When the end of one of the input files is reached, reading and writing will stop. The closeall command is used to close all files.

### 22.2.4 Distinguishing Character and Numeric Data

Although GAUSS itself does not distinguish between numeric and character columns in a matrix or data set, some of the GAUSS Application programs do. When creating a data set, it is important to indicate the type of data in the various columns. The following discusses two ways of doing this.

## Using Type Vectors

The v89 data set format distinguished between character and numeric data in data sets by the case of the variable names associated with the columns. The v96 data set format, however, stores this type information separately, resulting in a much cleaner and more robust method of tracking variable types, and greater freedom in the naming of data set variables.

When you create a data set, you can supply a vector indicating the type of data in each column of the data set. For example:

```
data = { M 32 21500,
    F 27 36000,
    F 28 19500,
    M 25 32000 };
vnames = { "Sex" "Age" "Pay" };
vtypes = { 0 1 1 };
create f = mydata with ^vnames, 3, 8, vtypes;
call writer(f,data);
f = close(f);
```

To retrieve the type vector, use vartypef.

```
open f = mydata for read;
vn = getnamef(f);
vt = vartypef(f);
print vn';
print vt';
```

```
Sex Age Pay
O 1 1
```

The call to getnamef in this example returns a string array rather than a character vector, so you can print it without the '\$' prefix.

## Using the Uppercase/ Lowercase Convention (v89 Data Sets)

Historically, some GAUSS Application programs recognized an "uppercase/lowercase" convention: if the variable name was uppercase, the variable was assumed to be numeric, and if it was lowercase, the variable was assumed to be character.

However, this is now obsolete; use vartypef and v96 data sets to be compatible with future versions.

### 22.3 GAUSS Data Archives

The GAUSS Data Archive (GDA) is extremely powerful and flexible, giving you much greater control over how you store your data. There is no limitation on the number of variables that can be stored in a GDA, and the only size limitation is the amount of available disk space. Moreover, GDA's are designed to hold whatever type of data you want to store in them. You may write matrices, arrays, strings, string arrays, sparse matrices, and structures to a GDA, and the GDA will keep track of the type, size and location of each of the variables contained in it. Since GAUSS now supports reading and writing to GDA's that were created on other platforms, GDA's provide a simple solution to the problem of sharing data across platforms.

See GAUSS Data Archives, Section 22.5.12, for information on the layout of a GDA.

### 22.3.1 Creating and Writing Variables to GDA's

To create a GAUSS Data Archive, call gdaCreate, which creates a GDA containing only header information. It is recommended that file names passed into gdaCreate have a . gda extension; however, gdaCreate will not force an extension.

To write variables to the GDA, you must call gdaWrite. A single call to gdaWrite writes only one variable to the GDA. Writing multiple variables requires multiple calls to gdaWrite.

For example, the following code:

```
ret = gdaCreate("myfile.gda",1);
ret = gdaWrite("myfile.gda",rndn(100,50), "x1");
ret = gdaWrite("myfile.gda", "This is a string", "str1");
ret = gdaWrite("myfile.gda",394, "x2");
```

produces a GDA containing the following variables:

| Index | Name | Type | Size |
| :--- | :--- | :--- | :--- |
| 1 | x 1 | matrix | $100 \times 50$ |
| 2 | str1 | string | 16 chars |
| 3 | x 2 | matrix | $1 \times 1$ |

### 22.3.2 Reading Variables from GDA's

The following table details the commands that you may use to read various types of variables from a GAUSS Data Archive:

| Variable Type | Read Command(s) |
| :--- | :--- |
| matrix |  |
| array | gdaRead |
| string <br> string array | gdaReadByIndex |


| sparse matrix | gdaReadSparse |
| :--- | :--- |
| structure | gdaReadStruct |

gdaRead, gdaReadSparse, and gdaReadStruct take a variable name and return the variable data. gdaReadBy Index returns the variable data for a specified variable index.

For example, to get the variable $x 1$ out of myfile.gda, you could call:

```
y = gdaRead("myfile.gda", "x1");
```

or

```
y = gdaReadByIndex("myfile.gda",1);
```

If you want to read only a part of a matrix, array, string, or string array from a GDA, call gdaReadSome. Sparse matrices and structures may not be read in parts.

### 22.3.3 Updating Variables in GDA's

To overwrite an entire variable in a GDA, you may call gdaUpdate or gdaUpdateAndPack. If the new variable is not the same size as the variable that it is replacing, gdaUpdate will leave empty bytes in the file, while gdaUpdateAndPack will pack the file (from the location of the variable that is being replaced to the end of the file) to remove those empty bytes.
gdaUpdate is usually faster, since it does not move data in the file unnecessarily. However, calling gdaUpdate several times for one file may result in a file with a large number of empty bytes.

On the other hand, gdaUpdateAndPack uses disk space efficiently, but it may be slow for large files (especially if the variable to be updated is one of the first variables in the file).

If speed and disk space are both concerns and you are going to update several variables, it will be most efficient to use gdaUpdate to update the variables and then call gdaPack once at the end to pack the file.

The syntax is the same for both gdaUpdate and gdaUpdateAndPack:

```
ret = gdaUpdate("myfile.gda",rndn(1000,100), "x1");
```

```
ret = gdaUpdateAndPack("myfile.gda",rndn(1000,100), "x1");
```

To overwrite part of a variable in a GDA, call gdaWriteSome.

### 22.4 Matrix Files

GAUSS matrix files are files created by the save command.
The save command takes a matrix in memory, adds a header that contains information on the number of rows and columns in the matrix, and stores it on disk. Numbers are stored in double precision just as they are in matrices in memory. These files have the extension.fmt.

Matrix files can be no larger than a single matrix. No variable names are associated with matrix files.

GAUSS matrix files can be load'ed into memory using the load or loadm command or they can be opened with the open command and read with the readr command. With the readr command, a subset of the rows can be read. With the load command, the entire matrix is load'ed.

GAUSS matrix files can be open'ed for read, but not for append, or for update.

If a matrix file has been opened and assigned a file handle, rowsf and colsf can be used to determine how many rows and columns it has without actually reading it into
memory. seekr and readr can be used to jump to particular rows and to read them into memory. This is useful when only a subset of rows is needed at any time. This procedure will save memory and be much faster than load'ing the entire matrix into memory.

### 22.5 File Formats

This section discusses the GAUSS binary file formats.
There are four currently supported matrix file formats:

| Version | Extension | Support |
| :--- | :--- | :--- |
| Small Matrix v89 | .$f m t$ | Obsolete, use v96. |
| Extended Matrix v89 | .$f m t$ | Obsolete, use v96. |
| Matrix v92 | .$f m t$ | Obsolete, use v96. |
| Universal Matrix v96 | .$f m t$ | Supported for read/write. |

There are four currently supported string file formats:

| Version | Extension | Support |
| :--- | :--- | :--- |
| Small String v89 | .fst | Obsolete, use v96. |
| Extended String v89 | .fst | Obsolete, use v96. |
| String v92 | .fst | Obsolete, use v96. |
| Universal String v96 | .fst | Supported for read/write. |

There are four currently supported data set formats:

| Version | Extension | Support |
| :--- | :--- | :--- |
| Small Data Set v89 | . dat, <br> . dht | Obsolete, use v96. |
| Extended Data Set v89 | . dat, <br> . dht | Obsolete, use v96. |
| Data Set v92 | . dat | Obsolete, use v96. |
| Universal Data Set v96 | . dat | Supported for read/write. |

### 22.5.1 Small Matrix v89 (Obsolete)

Matrix files are binary files, and cannot be read with a text editor. They are created with save. Matrix files with up to 8190 elements have a .fmt extension and a 16-byte header formatted as follows:

| Offset | Description |
| :--- | :--- |
| $0-1$ | DDDD hex, identification flag |
| $2-3$ | rows, unsigned 2-byte integer |
| $4-5$ | size of file minus 16-byte header, unsigned 2-byte integer <br> matrices |
| $6-7$ | reserved, all 0's |
| $8-9$ |  |

The body of the file starts at offset 16 and consists of IEEE format double precision floating point numbers or character elements of up to 8 characters. Character elements take up 8 bytes and are padded on the right with zeros. The size of the body of the file is 8 *rows*cols rounded up to the next 16-byte paragraph boundary. Numbers are stored row by row. A $2 \times 3$ real matrix will be stored on disk in the following way, from the lowest addressed element to the highest addressed element:

$$
[1,1][1,2][1,3][2,1][2,2][2,3]
$$

For complex matrices, the size of the body of the file is $16 *$ rows*cols. The entire real part of the matrix is stored first, then the entire imaginary part. A $2 \times 3$ complex matrix will be stored on disk in the following way, from the lowest addressed element to the highest addressed element:

| (real part) | $[1,1][1,2][1,3][2,1][2,2][2,3]$ |
| :--- | :--- |
| (imaginary part) | $[1,1][1,2][1,3][2,1][2,2][2,3]$ |

### 22.5.2 Extended Matrix v89 (Obsolete)

Matrices with more than 8190 elements are saved in an extended format. These files have a 16-byte header formatted as follows:

| Offset | Description |
| :--- | :--- |
| $0-1$ | EEDD hex, identification flag |
| $2-3$ | type of file, 0086 hex for real matrices, 8086 hex for complex <br> matrices |
| $4-7$ | rows, unsigned 4-byte integer |


| 8-11 | columns, unsigned 4-byte integer |
| :--- | :--- |
| $12-15$ | size of file minus 16-byte header, unsigned 4-byte integer |

The size of the body of an extended matrix file is $8 *$ rows*cols (not rounded up to a paragraph boundary). Aside from this, the body is the same as the small matrix v89 file.

### 22.5.3 Small String v89 (Obsolete)

String files are created with save. String files with up to 65519 characters have a 16byte header formatted as follows:


The body of the file starts at offset 16. It consists of the string terminated with a null byte. The size of the file is the 16-byte header plus the length of the string and null byte rounded up to the next 16-byte paragraph boundary.

### 22.5.4 Extended String v89 (Obsolete)

Strings with more than 65519 characters are saved in an extended format. These files have a 16 -byte header formatted as follows:

| Offset | Description |
| :--- | :--- |
| $0-1$ | EEDF hex, identification flag |
| $2-3$ | 001D hex, type of file |
| $4-7$ | 1, unsigned 4-byte integer |
| $8-11$ | length of string plus null byte, unsigned 4-byte integer |
| $12-15$ | size of file minus 16-byte header, unsigned 4-byte integer |

The body of the file starts at offset 16. It consists of the string terminated with a null byte. The size of the file is the 16 -byte header plus the length of the string and null byte rounded up to the next 8 -byte boundary.

### 22.5.5 Small Data Set v89 (Obsolete)

All data sets are created with create. v89 data sets consist of two files; one . dht contains the header information; the second (.dat) contains the binary data. The data will be one of three types:

8-byte IEEE floating point
4-byte IEEE floating point
2-byte signed binary integer, twos complement
Numbers are stored row by row.

The . dht file is used in conjunction with the . dat file as a descriptor file and as a place to store names for the columns in the . dat file. Data sets with up to 8175 columns have a.dht file formatted as follows:


Column names begin at offset 128 and are stored 8 bytes each in ASCII format. Names with less than 8 characters are padded on the right with bytes of 0 .

The number of rows in the . dat file is calculated in GAUSS using the file size, columns, and data type. This means that users can modify the . dat file by adding or deleting rows with other software without updating the header information.

Names for the columns should be lowercase for character data, to be able to distinguish them from numeric data with vartype.

GAUSS currently examines only the 4 's bit of the control flags. This bit is set to 0 for real data sets, 1 for complex data sets. All other bits are 0 .

Data sets are always stored a row at a time. A real data set with 2 rows and 3 columns will be stored on disk in the following way, from the lowest addressed element to the highest addressed element:

$$
\begin{aligned}
& {[1,1][1,2][1,3]} \\
& {[2,1][2,2][2,3]}
\end{aligned}
$$

The rows of a complex data set are stored with the real and imaginary parts interleaved, element by element. A $2 \times 3$ complex data set, then, will be stored on disk in the following way, from the lowest addressed element to the highest addressed element:

$$
\begin{array}{llllll}
{[1,1] r} & {[1,1] i} & {[1,2] r} & {[1,2] i} & {[1,3] r} & {[1,3] i} \\
{[2,1] r} & {[2,1] i} & {[2,2] r} & {[2,2] i} & {[2,3] r} & {[2,3] i}
\end{array}
$$

### 22.5.6 Extended Data Set v89 (Obsolete)

Data sets with more than 8175 columns are saved in an extended format that cannot be read by the 16 -bit version. These files have a . dht descriptor file formatted as follows:

| Offset | Description |
| :--- | :--- |
| $0-1$ | EEDA hex, identification flag |
| $2-3$ | data type in . dat file (2 4 8), unsigned 2-byte integer |
| $4-7$ | reserved, all 0's |
| $8-11$ | columns, unsigned 4-byte integer |


| $12-15$ | row size in bytes, unsigned 4-byte integer |
| :--- | :--- |
| $16-19$ | header size in bytes, unsigned 4-byte integer |
| $20-23$ | reserved, all 0's |
| $24-27$ | reserved, all 0's |
| $28-29$ | control flags, unsigned 2-byte integer |
| $30-127$ | reserved, all 0's |

Aside from the differences in the descriptor file and the number of columns allowed in the data file, extended data sets conform to the v89 data set description specified above.

### 22.5.7 Matrix v92 (Obsolete)

| Offset | Description |
| :---: | :---: |
| 0-3 | always 0 |
| 4-7 | always 0xEECDCDCD |
| 8-11 | reserved |
| 12-15 | reserved |
| 16-19 | reserved |
| 20-23 | 0 - real matrix, 1 - complex matrix |
| 24-27 | number of dimensions |


|  | $0-$ scalar <br> $1-$ row vector <br> $2-$ column vector, matrix |
| :--- | :--- |
| $28-31$ | header size, $128+$ number of dimensions * 4, padded to 8-byte <br> boundary |
| $32-127$ | reserved |

If the data is a scalar, the data will directly follow the header.
If the data is a row vector, an unsigned integer equaling the number of columns in the vector will precede the data, along with 4 padding bytes.

If the data is a column vector or a matrix, there will be two unsigned integers preceding the data. The first will represent the number of rows in the matrix and the second will represent the number of columns.

The data area always begins on an even 8-byte boundary. Numbers are stored in double precision ( 8 bytes per element, 16 if complex). For complex matrices, all of the real parts are stored first, followed by all the imaginary parts.
22.5.8 String v92 (Obsolete)

| Offset | Description |
| :--- | :--- |
| $0-3$ | always 0 |
| $4-7$ | always 0xEECFCFCF |
| $8-11$ | reserved |
| $12-15$ | reserved |


| $16-19$ | reserved |
| :--- | :--- |
| $20-23$ | size of string in units of 8 bytes |
| $24-27$ | length of string plus null terminator in bytes |
| $28-127$ | reserved |

The size of the data area is always divisible by 8 , and is padded with nulls if the length of the string is not evenly divisible by 8 . If the length of the string is evenly divisible by 8 , the data area will be the length of the string plus 8 . The data area follows immediately after the 128 -byte header.

### 22.5.9 Data Set v92 (Obsolete)

| Offset | Description |
| :---: | :---: |
| 0-3 | always 0 |
| 4-7 | always 0xEECACACA |
| 立 8 -11 | reserved |
| 12-15 | reserved |
| 16-19 | reserved |
| 20-23 | rows in data set |
| 24-27 | columns in data set |
| 28-31 | 0 - real data set, 1 - complex data set |


| $32-35$ | type of data in data set, 2,4, or 8 |
| :--- | :--- |
| $36-39$ | header size in bytes is $128+$ columns $* 9$ |
| $40-127$ | reserved |

The variable names begin at offset 128 and are stored 8 bytes each in ASCII format. Each name corresponds to one column of data. Names less than 8 characters are padded on the right with bytes of zero.

The variable type flags immediately follow the variable names. They are 1-byte binary integers, one per column, padded to an even 8 -byte boundary. A 1 indicates a numeric variable and a 0 indicates a character variable.

The contents of the data set follow the header and start on an 8-byte boundary. Data is either 2-byte signed integer, 4-byte single precision floating point or 8 -byte double precision floating point.

### 22.5.10 Matrix v96

| Offset | Description |
| :--- | :--- |
| $0-3$ | always 0xFFFFFFFF |
| $4-7$ | always 0 |
| $8-11$ | always 0xFFFFFFFF |
| $12-15$ | always 0xFFFFFFFF |
| $16-19$ | 0xFFFFFFFF for forward byte order, 0 for backward byte order |
| $20-23$ |  |



If the data is a scalar, the data will directly follow the header.
If the data is a row vector, an unsigned integer equaling the number of columns in the vector will precede the data, along with 4 padding bytes.

If the data is a column vector or a matrix, there will be two unsigned integers preceding the data. The first will represent the number of rows in the matrix and the second will represent the number of columns.

The data area always begins on an even 8-byte boundary. Numbers are stored in double precision ( 8 bytes per element, 16 if complex). For complex matrices, all of the real parts are stored first, followed by all the imaginary parts.

### 22.5.11 Data Set v96

| Offset | Description |
| :--- | :--- |
| $0-3$ | always 0xFFFFFFFF |
| $4-7$ | always 0 |
| $8-11$ | always 0xFFFFFFFF |
| $12-15$ | axFFFFFFFF for forward byte order, 0 for backward byte order |
| $16-19$ | $0 x F F F F F F F F$ for forward bit order, 0 for backward bit order |
| $20-23$ | 0xABCDEF02 |
| $24-27$ | version, currently 1 |
| $28-31$ |  |

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| 36-39 | reserved |
| :---: | :---: |
| 40-43 | floating point type, 1 for IEEE 754 |
| 44-47 | 12 - signed 2-byte integer <br> 1004 - single precision floating point <br> 1008 - double precision float |
| 48-51 | 2,4 , or 8 , the size of an element in bytes |
| 52-55 | 0 - real matrix, 1 - complex matrix |
| 56-59 | 1 - imaginary part of matrix follows real part (standard GAUSS style) <br> 2 - imaginary part of each element immediately follows real part (FORTRAN style) |
| 60-63 | always 2 |
| 64-67 | 1 for row major ordering of elements, 2 for column major |
|  | always 0 |
| 72-75 | header size, $128+$ columns * 33, padded to 8-byte boundary |
| 76-79 | reserved |
| 80-83 | rows in data set |
| 84-87 | columns in data set |
| 88-127 | reserved |

The variable names begin at offset 128 and are stored 32 bytes each in ASCII format. Each name corresponds to one column of data. Names less than 32 characters are padded on the right with bytes of zero.

The variable type flags immediately follow the variable names. They are 1-byte binary integers, one per column, padded to an even 8-byte boundary. A 1 indicates a numeric variable and a 0 indicates a character variable.

Contents of the data set follow the header and start on an 8-byte boundary. Data is either 2-byte signed integer, 4-byte single precision floating point or 8 -byte double precision floating point.

### 22.5.12 GAUSS Data Archives

A GAUSS Data Archive consists of a header, followed by the variable data and, finally, an array of variable descriptors containing information about each variable.

## Header

The header for a GAUSS Data Archive is laid out as follows:

| Offset | Type | Description |
| :--- | :--- | :--- |
| $0-3$ | 32 -bit unsigned integer | always 0xFFFFFFFF |
| $4-7$ | 32 -bit unsigned integer | always 0 |
| $8-11$ | 32 -bit unsigned integer | always 0xFFFFFFFF |
| $16-19$ | 32 -bit unsigned integer | always 0xFFFFFFFF |
| $20-23$ | 32 -bit unsigned integer | 0xFFFFFFFF for forward byte <br> order, <br> 0 for backward byte order |


| 24-27 | 32-bit unsigned integer | always 0 |
| :---: | :---: | :---: |
| 28-31 | 32-bit unsigned integer | always 0xABCDEF08 |
| 32-35 | 32-bit unsigned integer | version, currently 1 |
| 36-39 | 32-bit unsigned integer | reserved |
| 40-43 | 32-bit unsigned integer | floating point type, 1 for IEEE 754 |
| 44-55 | 32-bit unsigned integers | reserved |
| 56-63 | 64-bit unsigned integer | number of variables |
| 64-67 | 32-bit unsigned integer | header size, 128 |
| 68-95 | 32-bit unsigned integers | reserved |
| 96-103 | 64-bit unsigned integer | offset of variable descriptor table from end of header |
| 104-127 | 64-bit unsigned integers | reserved |

## Variable Data

After the header comes the variable data. Matrices are laid out in row-major order, and strings are written with a null-terminating byte.

For string arrays, an array of rowsx columns struct satable's is written out first, followed by the string array data in row-major order with each element null terminated. A struct satable consists of two members:

| Member | Type | Description |
| :--- | :--- | :--- |
| off | size_ . | offset of element data from beginning of string |


|  |  | array data |
| :--- | :--- | :--- |
| len | size_t | length of element data, including null-terminating <br> byte |

On a 32 -bit machine, a size_t is 4 bytes. On a 64-bit machine, it is 8 bytes.
Arrays are written with the orders (sizes) of each dimension followed by the array data. For example, the following $2 \times 3 \times 4$ array:
$[1,1,1]$ through $[1,3,4]=$

| 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: |
| 5 | 6 | 7 | 8 |
| 9 | 10 | 11 | 12 |

$[2,1,1]$ through $[2,3,4]=$

| 13 | 14 | 15 | 16 |
| :--- | :--- | :--- | :--- |
| 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 |

would be written out like this:
123456789101112131415161718192021222324

## Variable Structures

The variable data is followed by an array of variable descriptors. For each variable in the GDA, there is a corresponding variable descriptor in this array. A variable descriptor is laid out as follows:

| Offset | Type | Description |
| :--- | :--- | :--- |
| $0-3$ | 32-bit unsigned integer | variable type |
| $4-7$ | 32-bit unsigned integer | data type, 10 for 8 byte floating <br> point |
| 8-11 | 32-bit unsigned integer | dimensions, used only for arrays |
| $12-15$ | 32-bit unsigned integer unsigned integer | complex flag, 1 for real data, 0 for <br> complex |
| $20-19$ | 32-bit unsigned integer of pointer, indicates whether |  |
| the variable was written on a 32-bit |  |  |
| or 64-bit platform |  |  |

The variable type (bytes 0-3) may be any of the following:

| $\mathbf{2 0}$ | array |
| ---: | :--- |
| $\mathbf{3 0}$ | matrix |
| $\mathbf{4 0}$ | string |
| $\mathbf{5 0}$ | string array |

The size of pointer element (bytes 16-19) is the size of a pointer on the machine on which the variable was written to the GDA. It will be set to 4 on 32 -bit machines and 8 on 64-bit machines. This element is used only for string array variables. If a GDA containing string arrays is created on a 32-bit machine and then read on a 64-bit machine, or vice versa, then the size of pointer element indicates how the members of the struct satable's must be converted in order to be read on the current machine.

The huge flag (bytes 20-23) is set to 1 if the variable size is greater than INT_MAX, which is defined as 2147483647 . A variable for which the huge flag is set to 1 may not be read into GAUSS on a 32-bit machine.

The variable index element (bytes 40-47) contains the index of the variable in the GDA. Although the variable data is not necessarily ordered by index (see gdaUpdate), the variable descriptors are. Therefore, the indices are always in ascending order.

## 23 Databases with GAUSS

The database functionality within GAUSS is designed with simplicity in mind. This chapter assumes a basic knowledge of SQL. You should be able to understand simple SELECT, INSERT, UPDATE, and DELETE statements.

### 23.1 Connecting to Databases

In order to operate on a database, a connection must first be created and then opened. Database connections are created using the dbAddDatabase method and identified by the id number returned. It is possible to have multiple connections to the same database.

Note that the creation of a connection is different from opening the connection. The database can not be accessed until the connection is opened after it is created. The following example shows how to create a connection and open it.

```
id = dbAddDatabase("MYSQL");
dbSetHostName(id, "sql.mycompany.net");
dbSetDatabaseName(id, "testdb");
dbSetUserName(id, "webuser");
dbSetPassword(id, "f2DAf3E");
ret = dbOpen(id);
```

The first line returns an identifier for a MYSQL connection, and the last line opens the actual connection. Between those actions we set up the connection properties, such as the host name, database name, username and password. There is an additional shorthand method available to initialize the properties, described in the help page for dbAddDatabase.

It is also possible to omit the dbSetUserName and dbSetPassword calls and specify both in the dbOpen call, as follows:

```
ret = dbOpen(id, "webuser", "f2DAf3E");
```

The following example shows how to specify all connection properties in a single string, as well as how to connect to the same database twice using the same properties.

```
url =
"mysql://webuser:f2DAf3E@sql.mycompany.net:3306/testdb";
id1 = dbAddDatabase(url);
id2 = dbAddDatabase(url);
```

$i d 1$ and id2 are now separate connections to the same database. Since we've encapsulated all of the connection properties in the 'url' string, we can immediately call dbOpen on either idl or id2.

If dbOpen fails for any reason, it should be visible in the error output view. You can also call dbGetLastErrorNum or dbGetLastErrorText and pass in the appropriate id to get that information programmatically in GAUSS.

Once the connection has been established, it can be removed and all resources freed by calling dbRemoveDatabase with the corresponding connection id. If you'd like to only temporarily close the connection, you can also call dbClose, which allows for subsequent calls to dbOpen to re-open the connection.

### 23.2 Executing SQL Statements

GAUSS provides an intuitive interface for executing SQL statements and retrieving data either all at once or iteratively.

### 23.2.1 Creating a Query

A query can be created through two available methods. The first is direct-execution using the dbExecQuery method, assuming 'id' is a valid connection id:

```
qid = dbExecQuery(id, "SELECT symbol,
    price FROM stocks");
```

If you wish for your query to be more selective about the results being returned and the condition is user supplied, parameter binding is supported by GAUSS and easy to use:

```
print
    "Enter stock symbol: ";;
symbol = cons();
qid = dbExecQuery(id, "SELECT symbol,
    price FROM stocks WHERE symbol = ?",
    symbol);
```

The above example will immediately execute the query. If you'd like to set up the query more carefully, you can prepare it first and execute at your discretion.

```
qid = dbCreateQuery(id, "SELECT symbol,
    price FROM stocks WHERE symbol = :sym");
print "Enter stock symbol: ";;
symbol = cons();
dbQueryBindValue(qid, ":sym", symbol);
dbQueryExecPrepared(qid);
```

Note the specific call to dbQueryExecPrepared that is required when using dbCreateQuery instead of dbExecQuery. dbQueryExecPrepared can also be used for re-execution of a query created using dbExecQuery.

If the query fails to execute, output should be displayed in the error view but can also be fetched programatically using either dbQueryGetLastErrorNum or dbQueryGetLastErrorText.

### 23.2.2 Fetching Query Results

Once the query has been executed, retrieving the result is trivial.
To fetch all results directly into a matrix:

```
results = dbQueryFetchAllM(qid);
```

To store the symbol names into a string array and the price into a matrix:

```
symbols = dbQueryFetchAllSA(qid, "symbol");
prices = dbQueryFetchAllM(qid, "price");
```

GAUSS also has methods to provide access to the results one row at a time. Following the execution of a query, its internal pointer is located one position before the first record. An initial call to dbQuerySeekNext is required to position on the first row. Additional calls to dbQuerySeekNext will increment the current row, until the function returns false and no more rows are available.

A typical iteration of the results is as follows:

```
do while
    dbQuerySeekNext(qid);
    symbol = dbQueryFetchOneSA(qid, "symbol");
    price = dbQueryFetchOneM(qid, "price");
endo;
```

Multiple functions are available for flexible navigation of the result set. You can iterate forward and backward with dbQuerySeekNext and dbQuerySeekPrevious. dbQuerySeekFirst and dbQuerySeekLast will navigate to the first and last record, respectively. dbQueryGetPosition returns the current row index. The total number of rows can be retrieved via the dbQueryRows method.

Note that a performance increase can be achieved if you are only using dbQuerySeekNext, and never navigating backwards. This is most noticeable on large result sets.

In order to take advantage of the performance improvement, the driver must support it, and you must call dbQuerySetForwardOnly before executing the query, as such:

```
qid = dbCreateQuery("SELECT * FROM stocks");
dbQuerySetForwardOnly (qid) ;
dbQueryExecPrepared(qid) ;
```


### 23.2.3 Inserting, Updating, and Deleting Records

While SELECT statements are quite common, GAUSS is capable of executing any arbitrary SQL statement.

To insert a new stock symbol, you could do the following:

```
qid = dbExecQuery("INSERT INTO stocks (id,
    symbol, price) VALUES (100, 'TEST', 30)");
```

In the event of multiple inserts, this can be improved through usage of parameter binding:

```
string stocks = { "MSFT", "FB", "GOOG" };
prices = { 32.78, 45.95, 897.96 };
qid = dbCreateQuery("INSERT INTO stocks (id,
    symbol, price) VALUES (:id, :sym, :price)");
for i(1, rows(stocks), 1);
    dbQueryBindValue(qid, ":id", i);
    dbQueryBindValue(qid, ":sym", stocks[i]);
    dbQueryBindValue(qid, ":price", prices[i]);
    dbQueryExecPrepared(qid);
```

endfor;

The following is an identical example, using the same data, but using different style placeholders:

```
qid = dbCreateQuery("INSERT INTO stocks (id,
    symbol, price) VALUES (?, ?, ?)");
for i(1, rows (stocks), 1);
    dbQueryBindValue (qid, 1, i);
    dbQueryBindValue(qid, 2, stocks[i]);
    dbQueryBindValue(qid, 3, prices[i]);
    dbQueryExecPrepared(qid);
endfor;
```

This operation is even possible using a short-hand method:

```
for i(1, rows(stocks), 1);
    string args = itos(i) $| stocks[i] $| itos(prices[i]);
    qid = dbExecQuery("INSERT INTO stocks (id,
        symbol, price) VALUES (?, ?, ?)", args);
endfor;
```


### 23.2.4 Transactions

If the underlying database engine supports transactions, dbHasFeature(id, DB_ TRANSACTIONS) will return 1. You can use dbTransaction(id) to start a transaction, proceeded by SQL commands you wish to execute. At any time within the context of an open transaction, you can dbCommit(id) to finalize the executed commands or dbRollback(id) to reverse all commands executed since the start of the transaction. When using transactions you must start the transaction before you create or execute a query.

Transactions can be used to ensure that a complicated operation is atomic, meaning every part of the operation is completed or none at all.

For example, in the context of 1000 separate inserts, dbRollback can be called to cancel all of them, even if called on the 999th insert:

```
dbTransaction(id);
```

```
for i (1, 1000, 1);
    dbExecQuery(id, "INSERT INTO temp (num) VALUES (?)", i);
    if i == 999;
            dbRollback(id);
            break;
        endif;
endfor;
```


## 24 Foreign Language Interface

The Foreign Language Interface (FLI) allows users to create functions written in C, FORTRAN, or other languages, and call them from a GAUSS program. The functions are placed in dynamic libraries (DLLs, .so's, .dylib's, or shared libraries or shared objects) and linked in at run-time as needed. The FLI functions are:
dlibrary
dllcall

Link and unlink dynamic libraries at run-time.
Call functions located in dynamic libraries.

GAUSS recognizes a default dynamic library directory, a directory where it will look for your dynamic-link libraries when you call dlibrary. You can specify the default directory in gauss.cfg by setting dlib_path. As it is shipped, gauss.cfg specifies $\$($ GAUSSDIR $) /$ dlib as the default directory.

### 24.1 Writing FLI Functions

Your FLI functions should be written to the following specifications:

```
1. Take 0 or more pointers to doubles as arguments.
    This does not mean you cannot pass strings to an FLI
```

```
    function. Just recast
    the double pointer to a char pointer inside the func-
    tion.
2. Take those arguments either in a list or a vector.
3. Return an integer.
```

In C syntax, then, your functions would take one of the following forms:

```
1. int func(void);
2. int func(double *arg1 [, double *arg2,...]);
3. int func(double *arg[]);
```

Functions can be written to take a list of up to 100 arguments, or a vector (in C terms, a 1-dimensional array) of up to 1000 arguments. This does not affect how the function is called from GAUSS; the dllcall statement will always appear to pass the arguments in a list. That is, the dllcall statement will always look as follows:

```
dllcall func(a,b,c,d[,e...]);
```

For details on calling your function, passing arguments to it, getting data back, and what the return value means, see dllcall in the GAUSS LANGUAGE REFERENCE.

### 24.2 Creating Dynamic Libraries

The following describes how to build a dynamic library called hyp.dll (on Windows) or libhyp. so (on Linux) from the source file hyp.c.

As mentioned in the previous section, your FLI functions may take only pointers to doubles as arguments. Therefore, you should define your FLI functions to be merely wrapper functions that cast their arguments as necessary and then call the functions that actually do the work. This is demonstrated in the source file hyp. c:

```
#include <stdio.h>
#include <stdlib.h>
#include <math.h>
// This code is not meant to be efficient. It is meant
// to demonstrate the use of the FLI.
// This does all the work, not exported
static int hypo(double *x, double *y, double *h, int r,
int c)
{
    double *wx;
    double *wy;
    double *dp;
    double *sp1;
    double *sp2;
    int i, elems;
    elems = r*c;
        // malloc work arrays
    if ((wx =(double *)malloc(elems*sizeof(double))) ==
    NULL)
        return 30; // out of memory
    if ((wy =(double *)malloc(elems*sizeof(double))) ==
    NULL)
    {
        free (wx);
        return 30; // out of memory
    }
    dp = wx;
```

```
sp1 = x;
    // square x into work area wx
    for (i=0; i<elems; i++)
    {
        *dp = *sp1 * *sp1;
        ++sp1;
        ++dp;
    }
    dp = wy;
    sp2 = y;
    // square y into work area wy
    for (i=0; i<elems; i++)
    {
        *dp = *sp2 * *sp2;
        ++sp2;
        ++dp;
    }
    dp = h;
    sp1 = wx;
    sp2 = wy;
    // compute hypotenuse into h which was allocated by GAUSS
    for (i=0; i<elems; i++)
    {
        *dp = sqrt(*sp1 + *sp2);
        ++sp1;
        ++sp2;
        ++dp;
    }
    // free whatever you malloc
    free(wx);
```

```
        free(wy);
        return 0;
}
/* exported wrapper, all double * arguments, calls the real
** function with whatever data types it expects
*/
int hypotenuse(double *x, double *y, double *h, double *r,
double *c)
{
    return hypo( x, y, h, (int)*r, (int)*c);
}
```

The following Makefiles contain the compile and link commands you would use to build the dynamic library on various platforms. For explanations of the various flags used, see the documentation for your compiler and linker.

## Windows

```
hyp.dll: hyp.obj
    link /dll /out:hyp.dll hyp.obj
hyp.obj: hyp.c
    cl -c -MD -GX hyp.c
```


## Linux

\$ (CCOPTS) indicates any optional compilation flags you might add.

```
CCOPTIONS = -g -O2 -fpic -lm -lc -shared
CC = gcc
libhyp.so: hyp.cpp
$(CC) $(CCOPTIONS) -o $@ hyp.c
```

For details on linking your dynamic library, see dlibrary in the GAUSS LANGUAGE REFERENCE.

## 25 Data Transformations

GAUSS allows expressions that directly reference variables (columns) of a data set. This is done within the context of a data loop:

```
dataloop infile outfile;
    drop wages interest_rate;
    csed = ln(sqrt(csed));
    select exports > 3.35 and married $== "y";
    make chfac = hcfac + wcfac;
    keep unemployment chfac exports;
endata;
```

GAUSS translates the data loop into a procedure that performs the required operations, and then calls the procedure automatically at the location (in your program) of the data loop. It does this by translating your main program file into a temporary file and then executing the temporary file.

A data loop may be placed only in the main program file. Data loops in files that are \#include'd or autoloaded are not recognized.

### 25.1 Data Loop Statements

A data loop begins with a dataloop statement and ends with an endata statement. Inside a data loop, the following statements are supported:

| code |  |
| :--- | :--- |
| delete | Create variable based on a set of logical expressions. |
| drop |  |
| extern | Delete rows (observations) based on a logical <br> expression. |
| keep | Specify variables NOT to be written to data set. |
| lag | Allow access to matrices and strings in memory. |
| listwise | Specify variables to be written to output data set. |
| make | Control deletion of missing values. <br> outtyp |
| Create new variable. |  |
| recode | Specify output file precision. <br> Change variable based on a set of logical <br> expressions. |
| select | Select rows (observations) based on a logical <br> expression. |
| vector | Create new variable from a scalar returning <br> expression. |

In any expression inside a data loop, all text symbols not immediately followed by a left parenthesis '(' are assumed to be data set variable (column) names. Text symbols followed by a left parenthesis are assumed to be procedure names. Any symbol listed in an extern statement is assumed to be a matrix or string already in memory.

### 25.2 Using Other Statements

All program statements in the main file and not inside a data loop are passed through to the temporary file without modification. Program statements within a data loop that are
preceded by a '\#' are passed through to the temporary file without modification. The user familiar with the code generated in the temporary file can use this to do out-of-the-ordinary operations inside the data loop.

### 25.3 Debugging Data Loops

The translator that processes data loops can be turned on and off. When the translator is on, there are three distinct phases in running a program:

Translation Translation of main program file to temporary file.
Compilation Compilation of temporary file.
Execution Execution of compiled code.

### 25.3.1 Translation Phase

In the translation phase, the main program file is translated into a temporary file. Each data loop is translated into a procedure and a call to this procedure is placed in the temporary file at the same location as the original data loop. The data loop itself is commented out in the temporary file. All the data loop procedures are placed at the end of the temporary file.

Depending upon the status of line number tracking, error messages encountered in this phase will be printed with the file name and line numbers corresponding to the main file.

### 25.3.2 Compilation Phase

In the compilation phase, the temporary file is compiled. Depending upon the status of line number tracking, error messages encountered in this phase will be printed with the file name and line numbers corresponding to both the main file and the temporary file.

### 25.3.3 Execution Phase

In the execution phase, the compiled program is executed. Depending on the status of line number tracking, error messages will include line number references from both the main file and the temporary file.

### 25.4 Reserved Variables

The following local variables are created by the translator and used in the produced code:

| X_CV | x_iptr | x_ncol | x_plag |
| :---: | :---: | :---: | :---: |
| x_drop | x_keep | x_nlag | x_ptrim |
| x_fpin | $x$ _Ival | x_nrow | x_shft |
| x_fpout | x_lvar | x_ntrim | x_tname |
| x_i | $x \_n$ | s_out | x_vname |
| $x$ _in | x_name | x_outtyp | $X_{-} X$ |

These variables are reserved, and should not be used within a dataloop... endata section.

## 26 The GAUSS Profiler

GAUSS includes a profiler, which enables you to determine exactly how much time your programs are spending on each line and in each called procedure, thereby providing you with the information you need to increase the efficiency of your programs. The GAUSS Profiler (gaussprof)and tcollect are both run from a command prompt window, not at a GAUSS prompt.

### 26.1 Using the GAUSS Profiler

There are two steps to using the GAUSS Profiler: collection and analysis.

### 26.1.1 Collection

To collect profiling information, you must run your GAUSS program in tcollect, an executable shipped with GAUSS that is identical to tgauss except that it generates a file containing profiling information each time it is run:

```
tcollect -b myfile.e
```

The output displayed by tcollect includes the name of the output file containing the profiling information. tcollect output files have a gaussprof prefix and a .gco extension.

Note that running tcollect on long programs may generate a very large . gco output file. Thus you may want to delete the. gco files on your machine regularly.

### 26.1.2 Analysis

To analyze the information stored in the tcollect output file, you must run the gaussprof executable, which is also shipped with GAUSS, on that file. gaussprof produces an organized report, displaying the time usage by procedure and by line.

Assuming that running myfile.e in tcollect produced an output file called gaussprof_001.gco, you could analyze the results in that file as follows:

```
gaussprof gaussprof_001.gco
```

The syntax for gaussprof is:

```
gaussprof [flags] profile_data_file ...
```

where [flags] may be any of the following:

| $-p$ | profile procedure calls |
| :--- | :--- |
| -1 | profile line numbers |
| $-h$ | suppress headers |
| $-s p$ order | procedure call sort order where order contains one <br> or more of the following: |
|  | $e$ |
| $t$ | exclusive time |
|  | $p$ | | total time |
| :--- |
|  |


| a | ascending order |
| :--- | :--- | :--- |
| Csl order | Columns are sorted all ascending or all descending. <br> line number sort order where order contains one or <br> more of the following: |
| $t$ | time spent on line |
| C | number of times line was executed |
| f | line number |
| a | ascending order |
| C | descending order (default) |

The default, with no flags, is: $-p 1-s p d e p-s l d t f$.

## 27 Time and Date

GAUSS offers a comprehensive set of time and date functions. These functions afford the user the ability to return the current time and date, to carry out most related calculations and format the results for output. GAUSS also allows the user to perform timed iterations.

In the year 1 AD the calendar in general use was the Julian calendar. The Gregorian calendar that we use today was not invented until the late 1500 's. This new calendar changed the method of calculating leap years on century marks. With the Julian system simply every fourth year was a leap year. The Gregorian system made every fourth year a leap year with the exception of century marks which are only leap years if divisible by 400. The British adoption of this calendar, which the GAUSS date functions are based on, did not happen until the year 1752. In that year eleven days were removed; September 2, 1752 was followed by September 14, 1752.
dtvnormal and utctodtv are accurate back to 1 AD. The rest of the GAUSS date functions assume a normal Gregorian system regardless of year. Thus, they will not account for the days taken out in September of 1752, nor will they account for all century marks being leap years before the adoption of the Gregorian system in 1752.

The time is given by your operating system, daylight savings time is not automatically accounted for by GAUSS in calculations.

### 27.1 Time and Date Formats

The Time and Date formats in GAUSS fall into one of two major categories, matrix/vector and string. The matrix/vector formats can be used for either calculations or if desired for output. The string formats are, however, mostly for use as ouput. Some manipulation of strings is possible with the use of the stof function.

A $4 \times 1$ vector is returned by both the date and time functions.

```
d = date;
d;
1997.00 // Year
5.00000 // Month
29.0000 // Day
56.4700 // Hundredths of a second since midnight
t = time;
t;
10.00 // Hours since midnight
17.00 // Minutes
33.00 // Seconds
13.81 // Hundredths of a second
```

These vectors can be written to a string of the desired form by passing them through the corresponding function.

```
d = { 1997, 5, 29, 56.47};
datestr(d);
5/29/97
datestrymd(d);
19970529
t = { 10, 17, 33, 13.81 };
timestr(t);
10:17:33
```

A list and brief description of these, and other related functions is provided in the table in Section 25.2 .

Another major matrix/vector format is the dtv, or date and time vector. The dtv vector is a 1x8 vector used with the dtvnormal and utctodtv functions. The format for the dtv vector is:

$$
\begin{array}{cccccccc}
\text { Year } & \text { Month } & \text { Day } & \text { Hour } & \text { Min } & \text { Sec } & \text { DoW } & \text { DiY } \\
1955 & 4 & 21 & 4 & 16 & 0 & 4 & 110
\end{array}
$$

Where:

| Year | Year, four digit integer. |
| :--- | :--- |
| Month | $1-12$, Month in year. |
| Day | $1-31$, Day of month. |
| Hour | $0-23$, Hours since midnight. |
| Min | $0-59$, Minutes. |
| Sec | $0-59$, Seconds. |
| Dow | $0-6$, Day of week, $0=$ Sunday. |
| DiY | $0-365$, Days since Jan 1 of current year. |

dtvnormal normalizes a date. The last two elements are ignored for input, as shown in the following example. They are set to the correct values on output. The input can be 1 x 8 or Nx 8 .

```
dtv = { 1954 3 17 4 16 0 0 0 };
dtv = dtvnormal(dtv);
```

```
dtv[3] = dtv[3] + 400;
print dtv;
```

$$
\begin{array}{llllllll}
1954 & 3 & 417 & 4 & 16 & 0 & 3 & 75
\end{array}
$$

$d t v=$ dtvnormal (dtv);
print dtv;

$$
\begin{array}{llllllll}
1955 & 4 & 21 & 4 & 16 & 0 & 4 & 110
\end{array}
$$

### 27.2 Time and Date Functions

Following is a partial listing of the time and date functions available in GAUSS.

| datestr | Formats a Date vector to a string (mo/dy/yr). |
| :--- | :--- |
| datestrymd | Formats a Date vector to an eight character string of <br> the type yyyymmdd. |
| dayinyr | Returns day number in the year of a given date. |
| _daypryr | Returns the number of days in the years given as <br> input. |
| dtvnormal | Normalizes a 1x8 dtv vector. |
| etdays | Computes the difference in days between two dates. |
| ethsec | Computes the difference between two times in <br> hundredths of a second. |
| etstr | Formats a time difference measured in hundreths of a <br> second to a string. |


| _isleap | Returns a vector of ones and zeros, 1 if leap year 0 if <br> not. |
| :--- | :--- |
| timestr | Formats a Time vector to a string hr:mn:sc. |
| timeutc | Universal time coordinate, number of seconds since <br> January 1, 1970 Greenwich Mean Time. |
| utctodtv | Converts a scalar, number of seconds since, or <br> before, Jan 1 1970 Greenwich mean time, to a dtv <br> vector. |

Below is an example of two ways to calculate a time difference.

```
d1 = { 1996, 12, 19, 82 };
d2 = { 1997, 4, 28, 4248879.3 };
dif = ethsec(d1,d2);
ds = etstr(dif);
```

$$
d i f=1.1274488 e+09
$$

$$
d s=130 \text { days } 11 \text { hours } 48 \text { minutes } 7.97 \text { seconds }
$$

If only the number of days is needed use etdays.

```
d1 = { 1996, 12, 19, 82 };
d2 = { 1997, 4, 28, 4248879.3 };
dif = etdays(d1,d2);
```

$$
\text { dif }=130.00000
$$

The last element of d 1 is optional when used as an input for etdays._isleap returns a matrix of ones and zeros, ones when the corresponding year is a leap year.

```
x = seqa(1970,1,20);
y = _isleap(x);
delif(x,abs(y-1));
1972.0000 // Vector containing all leap years
1976.0000 // between 1970 - 1989
1980.0000
1984.0000
1988.0000
```

To calculate the days of a number of consecutive years:

```
x = seqa(1983,1,3);
y = _daypryr(x);
sumc(y);
1096.0000
```

To add a portion of the following year:

```
g = { 1986, 2, 23, 0 };
dy = dayinyr(g);
sumc(y)+dy;
1150.0000
```

For more information on any of these functions see their respective pages in the command reference.

### 27.2.1 Timed Iterations

Iterations of a program can be timed with the use of the hsec function in the following manner.

```
et = hsec; // Start timer
/* Segment of code to be timed */
et =(hsec-et)/100; // Stop timer, convert to seconds
```

In the case of a program running from one day into the next you would need to replace the hsec function with the date function. The ethsec function should be used to compute the time difference; a straight subtraction as in the previous example will not give the desired result.

```
dstart = date; // Start timer
/* Segment of code to be timed */
dend = date; // Stop timer
// Convert time difference to seconds
dif = ethsec(dstart,dend)/100;
```


## 28 ATOG

ATOG is a stand-alone conversion utility that converts ASCII files into GAUSS data sets. ATOG can convert delimited and packed ASCII files into GAUSS data sets. ATOG can be run from a batch file or the command line; it is not run from a GAUSS prompt but rather from a command prompt window.

The syntax is:
atog cmdfile
where cmdfile is the name of the command file. If no extension is given, . cmd will be assumed. If no command file is specified, a command summary will be displayed.

### 28.1 Command Summary

The following commands are supported in ATOG:

| append | Append data to an existing file. |
| :--- | :--- |
| complex | Treat data as complex variables. |
| input | The name of the ASCII input file. |
| invar | Input file variables (column names). |


| msym | Specify missing value character. |
| :--- | :--- |
| nocheck | Don't check data type or record length. |
| output | The name of the GAUSS data set to be created. |
| outtyp | Output data type. |
| outvar | List of variables to be included in output file. |
| preservecase | Preserve case of variable names in output file. |

The principle commands for converting an ASCII file that is delimited with spaces or commas are given in the following example:

```
input agex.asc;
output agex;
invar $ race # age pay $ sex region;
outvar region age sex pay;
outtyp d;
```

In this example, a delimited ASCII file agex. asc is converted to a double precision GAUSS data file agex. dat. The input file has five variables. The file will be interpreted as having five columns:

| column | name | data type |
| :---: | :--- | :--- |
| 1 | race | character |
| 2 | AGE | numeric |
| 3 | PAY | numeric |
| 4 | region | character |
| 5 |  |  |

The output file will have four columns since the first column of the input file (race) is not included in the output variables. The columns of the output file are:

| column | name | data type |
| :---: | :--- | :--- |
| 1 | region | character |
| 2 | AGE | numeric |
| 3 | sex | character |
| 4 | PAY | numeric |

The variable names are saved in the file header. Unless preservecase has been specified, the names of character variables will be saved in lowercase, and the names of numeric variables will be saved in uppercase. The $\$$ in the invar statement specifies that the variables that follow are character type. The \# specifies numeric. If \$ and \# are not used in an invar statement, the default is numeric.

Comments in command files must be enclosed between '@' characters.

### 28.2 Commands

A detailed explanation of each command follows.

## append

Instructs ATOG to append the converted data to an existing data set:

```
append;
```

No assumptions are made regarding the format of the existing file. Make certain that the number, order, and type of data converted match the existing file. ATOG creates v96 format data files, so will only append to v96 format data files.

## complex

Instructs ATOG to convert the ASCII file into a complex GAUSS data set:

```
complex;
```

Complex GAUSS data sets are stored by rows, with the real and imaginary parts interleaved, element by element. ATOG assumes the same structure for the ASCII input file, and will thus read TWO numbers out for EACH variable specified.
complex cannot be used with packed ASCII files.

## input

Specifies the file name of the ASCII file to be converted. The full path name can be used in the file specification.

For example, the command:

```
input data.raw;
```

will expect an ASCII data file in the current working directory.
The command:

```
input /research/data/myfile.asc;
```

specifies a file to be located in the /research/data subdirectory.

## invar

## Soft Delimited ASCII Files

Soft delimited files may have spaces, commas, or cr/lf as delimiters between elements. Two or more consecutive delimiters with no data between them are treated as one delimiter. For example:

```
invar age $ name sex # pay var[1:10] x[005];
```

The invar command above specifies the following variables:

| column | name | data type |
| :---: | :---: | :---: |
| 1 | AGE | numeric |
| 2 | name | character |
| 3 | sex | character |
| 4 | PAY | numeric |
| 5 | VAR01 | numeric |
| 6 | VAR02 | numeric |
| 7 | VAR03 | numeric |
| 8 | VAR04 | numeric |
| 9 | VAR05 | numeric |
| 10 | VAR06 | numeric |
| 11 | VAR07 | numeric |
| 12 | VAR08 | numeric |
| 13 | VAR09 | numeric |
| 14 | VAR10 | numeric |
| 15 | X001 | numeric |
| 16 | X002 | numeric |


| 17 | X 003 | numeric |
| :---: | :--- | :--- |
| 18 | X 004 | numeric |
| 19 | X005 | numeric |

As the input file is translated, the first 19 elements will be interpreted as the first row (observation), the next 19 will be interpreted as the second row, and so on. If the number of elements in the file is not evenly divisible by 19 , the final incomplete row will be dropped and a warning message will be given.

## Hard Delimited ASCII Files

Hard delimited files have a printable character as a delimiter between elements. Two delimiters without intervening data between them will be interpreted as a missing. If $\backslash \mathrm{n}$ is specified as a delimiter, the file should have one element per line and blank lines will be considered missings. Otherwise, delimiters must be printable characters. The dot '.' is illegal and will always be interpreted as a missing value. To specify the backslash as a delimiter, use $\backslash \backslash$. If $\backslash r$ is specified as a delimiter, the file will be assumed to contain one case or record per line with commas between elements and no comma at the end of the line.

For hard delimited files the delimit subcommand is used with the invar command. The delimit subcommand has two optional parameters. The first parameter is the delimiter. The default is a comma. The second parameter is an ' N '. If the second parameter is present, ATOG will expect N delimiters. If it is not present, ATOG will expect $\mathrm{N}-1$ delimiters.

This example:

```
invar delimit(, N) $ name # var[5];
```

will expect a file like this:

```
BILL , 222.3, 123.2, 456.4, 345.2, 533.2,
STEVE, 624.3, 340.3, , 624.3, 639.5,
TOM , 244.2, 834.3, 602.3, 333.4, 822.5,
```

while

```
invar delimit(,) $ name # var[5];
```

or

```
invar delimit $ name # var[5];
```

will expect a file like this:

```
BILL , 222.3, 123.2, 456.4, 345.2, 533.2,
STEVE, 624.3, 340.3, , 624.3, 639.5,
TOM , 244.2, 834.3, 602.3, 333.4, 822.5
```

The difference between specifying N or $\mathrm{N}-1$ delimiters can be seen here:

```
456.4, 345.2, 533.2,
    , 624.3, 639.5,
602.3, 333.4,
```

If the invar statement specified three variables and N-1 delimiters, this file would be interpreted as having three rows containing a missing in the [2,1] element and the $[3,3]$ element like this:

$$
\begin{array}{ccc}
456.4 & 345.2 & 533.2 \\
. & 624.3 & 639.5 \\
602.3 & 333.4 & .
\end{array}
$$

If N delimiters had been specified, this file would be interpreted as having two rows, and a final incomplete row that is dropped:

$$
\begin{array}{lll}
456.4 & 345.2 & 533.2
\end{array}
$$

$$
624.3 \quad 639.5
$$

The spaces were shown only for clarity and are not significant in delimited files so:

```
BILL,222.3,123.2,456.4,345.2,533.2,
STEVE,624.3,340.3,,624.3,639.5,
TOM,244.2,834.3,602.3,333.4,822.5
```

would work just as well.
Linefeeds are significant only if $\backslash \mathrm{n}$ is specified as the delimiter, or when using $\backslash \mathrm{r}$. This example:

```
invar delimit(\r) $ name # var[5];
```

will expect a file with no comma after the final element in each row:

```
BILL , 222.3, 123.2, 456.4, 345.2, 533.2
STEVE, 624.3, 340.3, 245.3, 624.3, 639.5
TOM , 244.2, 834.3, 602.3, 333.4, 822.5
```


## Packed ASCII Files

Packed ASCII files must have fixed length records. The record subcommand is used to specify the record length, and variables are specified by giving their type, starting position, length, and the position of an implicit decimal point if necessary.
outvar is not used with packed ASCII files. Instead, invar is used to specify only those variables to be included in the output file.

For packed ASCII files the syntax of the invar command is as follows:

```
invarrecord = reclen (format) variables (format)
variables;
```

where,
reclen the total record length in bytes, including the final carriage return/line feed if applicable. Records must be fixed length.
(start,length.prec) where:
start starting position of the field in the record, 1 is the first position. The default is 1 .
length the length of the field in bytes. The default is 8 .
precoptional; a decimal point will be inserted automatically prec places in from the RIGHT edge of the field.

If several variables are listed after a format definition, each succeeding field will be assumed to start immediately after the preceding field. If an asterisk is used to specify the starting position, the current logical default will be assumed. An asterisk in the length position will select the current default for both length and prec. This is illegal: $(3,8 . *)$.

The type change characters \$ and \# are used to toggle between character and numeric data type.

Any data in the record that is not defined in a format is ignored.
The examples below assume a 32-byte record with a carriage return/line feed occupying the last 2 bytes of each record. The data below can be interpreted in different ways using different invar statements:


This example:

```
invar record=32 $(1,3) group dept #(11,4.2) x[3] (*,5)
y;
```

will result in:

## GAUSS User Guide

| variable | value | type |
| :--- | :--- | :--- |
| group | ABC | character |
| dept | DEF | character |
| X1 | 12.34 | numeric |
| X2 | 96.78 | numeric |
| X3 | 34567 | numeric |
| Y |  | numeric |

This example：

```
invar record=32 $ dept (*,2) id # (*,5) wage (*,2) area
```

will result in：

| variable | value | type |
| :--- | :--- | :--- |
| dept | ABCDEFGH | character |
| id | IJ | character |
| WAGE | 12345 | numeric |
| AREA | 67 | numeric |

## msym

Specifies the character in the input file that is to be interpreted as a missing value．This example：

```
msym &;
```

defines the character ' $\&$ ' as the missing value character. The default '. ' (dot) will always be interpreted as a missing value unless it is part of a numeric value.

## nocheck

Optional; suppresses automatic checking of packed ASCII record length and output data type. The default is to increase the record length by 2 bytes if the second record in a packed file starts with cr/lf, and any files that have explicitly defined character data will be output in double precision regardless of the type specified.

## output

The name of the GAUSS data set. A file will be created with the extension . dat. For example:

```
output /gauss/dat/test;
```

creates the file test. dat on the /gauss/dat directory.

## outtyp

Selects the numerical accuracy of the output file. Use of this command should be dictated by the accuracy of the input data and storage space limitations. The format is:
outtyp fmt;
where fmt is:

| D or 8 | double precision |
| :---: | :--- |
| F or 4 | single precision (default) |
| I or 2 | integer |

The ranges of the different formats are:

| Bytes | Type | Significant Digits | Range |
| :--- | :--- | :--- | :---: |
| 2 | integer | 4 | $-32768<=\mathrm{X}<=32767$ |
| 4 | single | $6-7$ | $8.43 \mathrm{E}-37<=\|\mathrm{X}\|<=3.37 \mathrm{E}+38$ |
| 8 | double | $15-16$ | $4.193 \mathrm{E}-307<=\|\mathrm{X}\|<=1.67 \mathrm{E}+308$ |

If the output type is integer, the input numbers will be truncated to integers. If your data has more than 6 or 7 significant digits, specify outtyp as double.

Character data require outtyp d. ATOG automatically selects double precision when character data is specified in the invar statement, unless you have specified nocheck.

The precision of the storage selected does not affect the accuracy of GAUSS calculations using the data. GAUSS converts all data to double precision when the file is read.

## outvar

Selects the variables to be placed in the GAUSS data set. The outvar command needs only the list of variables to be included in the output data set. They can be in any order. In this example:

```
invar $name #age pay $sex #var[1:10] x[005];
outvar sex age x001 x003 var[1:8];
```

the outvar statement selects the following variables:

| column | name | data type |
| :---: | :--- | :--- |
| 1 | sex | character |
| 2 | AGE | numeric |
| 3 | X001 | numeric |


| 4 | X003 | numeric |
| :---: | :--- | :--- |
| 5 | VAR01 | numeric |
| 6 | VAR02 | numeric |
| 7 | VAR03 | numeric |
| 8 | VAR04 | numeric |
| 9 | VAR07 | numeric |
| 10 | VAR08 | numeric |
| 11 | numeric |  |
| 12 |  |  |

outvar is not used with packed ASCII files.

## preservecase

Optional; preserves the case of variable names. The default is nopreservcase, which will force variable names for numeric variables to upper case and character variables to lower case.

### 28.3 Examples

Example 1 The first example is a soft delimited ASCII file called agex1. asc. The file contains seven columns of ASCII data:

```
Jan 167.3 822.4 6.34E06 yes 84.3 100.4
Feb 165.8 987.3 5.63E06 no 22.4 65.6
Mar 165.3 842.3 7.34E06 yes 65.4 78.3
```

The ATOG command file is agex1.cmd:

```
input /gauss/agex1.asc;
output agex1;
invar $month #temp pres vol $true var[02];
outvar month true temp pres vol;
```

The output data set will contain the following information:

| name | month |  |  | true | TEMP |
| :--- | :--- | :--- | :--- | :--- | :--- |
| PRES | VOL |  |  |  |  |
| case 1 | Jan | yes | 167.3 | 822.4 | $6.34 \mathrm{e}+6$ |
| case 2 | Feb | no | 165.8 | 987.3 | $5.63 \mathrm{e}+6$ |
| case 3 | Mar | yes | 165.3 | 842.3 | $7.34 \mathrm{e}+6$ |
| type | char | char | numeric | numeric | numeric |

The data set is double precision since character data is explicitly specified.
Example 2 The second example is a packed ASCII file xlod.asc The file contains 32-character records:


The ATOG command file is xlod.cmd:

```
input /gauss/dat/xlod.asc;
output xlod2;
invar record=32 $(1,3) client[2] zone (*,1) reg # (20,5) zip;
```

The output data set will contain the following information:

| name | client1 | client2 | zone | reg | ZIP |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| case 1 | AEG | DRF | CST | y | 60631 |
| case 2 | EDJ | TAJ | PST | n | 98064 |


| case 3 | GWD | NAD | MST | y | 59725 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| type | char | char | char | char | numeric |

The data set is double precision since character data is explicitly specified.
Example 3 The third example is a hard delimited ASCII file called cplx.asc. The file contains six columns of ASCII data:

```
456.4, 345.2, 533.2, -345.5, 524.5, 935.3,
-257.6, 624.3, 639.5, 826.5, 331.4, 376.4,
602.3, -333.4, 342.1, 816.7, -452.6, -690.8
```

The ATOG command file is cplx.cmd:

```
input /gauss/cplx.asc;
output cplx;
invar delimit #cvar[3];
complex;
```

The output data set will contain the following information:

| name | cvar1 | cvar2 | cvar3 |
| :--- | :--- | :--- | :--- |
| case 1 | $456.4+345.2 \mathrm{i}$ | $533.2-345.5 \mathrm{i}$ | $524.5+935.3 \mathrm{i}$ |
| case 2 | $-257.6+624.3 \mathrm{i}$ | $639.5+826.5 \mathrm{i}$ | $331.4+376.4 \mathrm{i}$ |
| case 3 | $602.3-333.4 \mathrm{i}$ | $342.1+816.7 \mathrm{i}$ | $-452.6-690.8 \mathrm{i}$ |
| type | numeric | numeric | numeric |

The data set defaults to single precision, since no character data is present, and no outtyp command is specified.

### 28.4 Error Messages

## atog - Can't find input file

The ASCII input file could not be opened.

## atog - Can't open output file

The output file could not be opened.

## atog - Can't open temporary file

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## atog - Can't read temporary file

Notify Aptech Systems.

## atog - Character data in output file Setting output file to double precision

The output file contains character data. The type was set to double precision automatically.

## atog - Character data longer than 8 bytes were truncated

The input file contained character elements longer than 8 bytes. The conversion continued and the character elements were truncated to 8 bytes.

## atog - Disk Full

The output disk is full. The output file is incomplete.

## atog - Found character data in numeric field

This is a warning that character data was found in a variable that was specified as numeric. The conversion will continue.

## atog - Illegal command

An unrecognizable command was found in a command file.

## atog-Internal error

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```
atog - Invalid delimiter
```

The delimiter following the backslash is not supported.

## atog - Invalid output type

Output type must be I, F, or D.

## atog - Missing value symbol not found

No missing value was specified in an msym statement.

## atog - No Input file

No ASCII input file was specified. The input command may be missing.

## atog - No input variables

No input variable names were specified. The invar statement may be missing.

## atog - No output file

No output file was specified. The output command may be missing.

## atog - output type d required for character data Character data in output file will be lost

Output file contains character data and is not double precision.

```
atog - Open comment
```

The command file has a comment that is not closed. Comments must be enclosed in @'s:
@ comment @

## atog - Out of memory

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## atog - read error

A read error has occurred while converting a packed ASCII file.
atog - Record length must be 1-16384 bytes
The record subcommand has an out of range record length.

## atog - Statement too long

Command file statements must be less than 16384 bytes.

```
atog - Syntax error at:
```

There is unrecognizable syntax in a command file.

## atog - Too many input variables

More input variables were specified than available memory permitted.

## atog - Too many output variables

More output variables were specified than available memory permitted. atog - Too many variables

More variables were specified than available memory permitted. atog - Undefined variable

A variable requested in an outvar statement was not listed in an invar statement.

## atog WARNING: missing ')' at:

The parentheses in the delimit subcommand were not closed.

## atog WARNING: some records begin with cr/If

A packed ASCII file has some records that begin with a carriage return/linefeed. The record length may be wrong.

## atog - complex illegal for packed ASCII file.

A complex command was encountered following an invar command with record specified.

## atog - Cannot read packed ASCII. (complex specified)

An invar command with record specified was encountered following a complex command.

## 29 Error Messages

The following is a list of error messages intrinsic to the GAUSS programming language. Error messages generated by library functions are not included here.

## G0002 File too large

## G0003 Indexing a matrix as a vector

A single index can be used only on vectors. Vectors have only one row or only one column.

## G0004 Compiler stack overflow - too complex

An expression is too complex. Break it into smaller pieces. Notify Aptech Systems.

## G0005 File is already compiled

## G0006 Statement too long

Statement longer than 4000 characters.
G0007 End of file encountered
G0008 Syntax error
compiler Unrecognizable or incorrect syntax. Semicolon
missing on previous statement.
Unrecognizable statement in command file, or numvar or outvar statement error.

## G0009 Compiler pass out of memory

Compiler pass has run out of memory. Notify Aptech Systems.

## G0010 Can't open output file

## G0011 Compiled file must have correct extension

GAUSS requires a . gcg extension.
G0012 Invalid drive specifier
G0013 Invalid filename
G0014 File not found
G0015 Directory full
G0016 Too many \#include's
\#include'd files are nested too deep.

## G0017 WARNING: local outside of procedure

A local statement has been found outside a procedure definition. The local statement will be ignored.

## G0018 Read error in program file

G0019 Can't edit .gcg file

## G0020 Not implemented yet

Command not supported in this implementation.

## G0021 use must be at the beginning of a program

G0022 User keyword cannot be used in expression
G0023 Illegal attempt to redefine symbol to an index variable

G0024 Invalid use of ->, probably should be .
G0025 Undefined symbol
A symbol has been referenced that has not been given a definition.

## G0026 Too many symbols

The global symbol table is full. (To set the limit, see new in the GAUSS LANGUAGE Reference.)

## G0027 Invalid directory

## G0028 Can't open configuration file

GAUSS cannot find the configuration file.

## G0029 Missing left parenthesis

## G0030 Insufficient workspace memory

The space used to store and manipulate matrices and strings is not large enough for the operations attempted. (To make the main program space smaller and reclaim enough space to continue, see new in the GAUSS LANGUAGE REFERENCE.)

## G0031 Execution stack too deep - expression too complex

An expression is too complex. Break it into smaller pieces. Notify Aptech Systems.

G0032 fn function too large
G0033 Missing right index bracket

## G0034 Missing arguments

G0035 Argument too large
G0036 Matrices are not conformable
For a description of the function or operator being used and conformability rules, see Matrix Operators, Section 10.2 , or the GAUSS LANGUAGE REFERENCE MANUAL.

## G0037 Result too large

The size of the result of an expression is greater than the limit for a single matrix.
G0038 Not all the eigenvalues can be computed
G0039 Matrix must be square to invert
G0040 Not all the singular values can be computed
G0041 Argument must be scalar
A matrix argument was passed to a function that requires a scalar.
G0042 Matrix must be square to compute determinant
G0043 Not implemented for complex matrices
G0044 Matrix must be real

## G0045 Attempt to write complex data to real data set

Data sets, unlike matrices, cannot change from real to complex after they are created. Use create complex to create a complex data set.

G0046 Columns don't match
The matrices must have the same number of columns.

## G0047 Rows don't match

The matrices must have the same number of rows.

## G0048 Matrix singular

The matrix is singular using the current tolerance.

## G0049 Target matrix not complex G0050 Out of memory for program

The main program area is full. (To increase the main program space, see new in the GAUSS LANGUAGE REFERENCE.)

## G0051 Program too large

The main program area is full. (To increase the main program space, see new in the GAUSS LANGUAGE REFERENCE.)

## G0052 No square root - negative element

## G0053 Illegal index

An illegal value has been passed in as a matrix index.

## G0054 Index overflow

An illegal value has been passed in as a matrix index.

## G0055 retp outside of procedure

A retp statement has been encountered outside a procedure definition.

## G0056 Too many active locals

The execution stack is full. There are too many local variables active. Restructure your program. Notify Aptech Systems.

G0057 Procedure stack overflow - expression too complex
The execution stack is full. There are too many nested levels of procedure calls. Restructure your program. Notify Aptech Systems.

## G0058 Index out of range

You have referenced a matrix element that is out of bounds for the matrix being referenced.

## G0059 exec command string too long

G0060 Nonscalar index
G0061 Cholesky downdate failed
G0062 Zero pivot encountered
crout The Crout algorithm has encountered a diagonal element equal to 0 . Use croutp instead.

## G0063 Operator missing

An expression contains two consecutive operands with no intervening operator.

## G0064 Operand missing

An expression contains two consecutive operators with no intervening operand.

## G0065 Division by zero!

## G0066 Must be recompiled under current version

You are attempting to use compiled code from a previous version of GAUSS. Recompile the source code under the current version.

G0068 Program compiled under GAUSS-386 real version
G0069 Program compiled under GAUSS-386i complex version

G0070 Procedure calls too deep
You may have a runaway recursive procedure.

## G0071 Type mismatch

You are using an argument of the wrong data type (e.g., inputting a matrix when a string is called for).

## G0072 Too many files open

The limit on simultaneously open files is 10 .

## G0073 Redefinition of

declare An attempt has been made to initialize a variable that is already initialized. This is an error when declare := is used. declare ! = or declare ? = may be a better choice for your application.

An attempt has been made to redefine a string as a matrix or procedure, or vice versa. delete the symbol and try again. If this happens in the context of a single program, you have a programming error. If this is a conflict between different programs, use a new statement before running the second program.

A string is being forced to type matrix. Use an external matrix symbol; statement before the let statement.

G0074 Can't run program compiled under GAUSS Light

## G0075 gscroll input vector the wrong size

G0076 Call Aptech Systems Technical Support

## G0077 New size cannot be zero

You cannot reshape a matrix to a size of zero.
G0078 vargetl outside of procedure
G0079 varputl outside of procedure
G0080 File handle must be an integer
G0081 Error renaming file
G0082 Error reading file
G0083 Error creating temporary file
G0084 Too many locals
A procedure has too many local variables.
G0085 Invalid file type
You cannot use this kind of file in this way.
G0086 Error deleting file
G0087 Couldn't open
The auxiliary output file could not be opened. Check the file name and make surethere is room on the disk.
G0088 Not enough memory to convert the whole string
G0089 WARNING: duplicate definition of local
G0090 Label undefinedLabel referenced has no definition.
G0091 Symbol too long
Symbols can be no longer than 32 characters.
G0092 Open comment
A comment was never closed.

## G0093 Locate off screen <br> G0094 Argument out of range <br> G0095 Seed out of range <br> G0096 Error parsing string

parse encountered a token that was too long.

## G0097 String not closed

A string must have double quotes at both ends.

## G0098 Invalid character for imaginary part of complex number

G0099 Illegal redefinition of user keyword
G0100 Internal E R R O R \#\#\#
Notify Aptech Systems.

## G0101 Argument cannot be zero

The argument to $\ln$ or $\log$ cannot be zero.

## G0102 Subroutine calls too deep

Too many levels of gosub. Restructure your program.

## G0103 return without gosub

You have encountred a subroutine without executing a gosub.
G0104 Argument must be positive
G0105 Bad expression or missing arguments
Check the expression in question, or you forgot an argument.

## G0106 Factorial overflow

## G0107 Nesting too deep

Break the expression into smaller statements.

## G0108 Missing left bracket [

## G0109 Not enough data items

You omitted data in a let statement.

## G0110 Found ) expected ] -

G0111 Found ] expected ) -
G0112 Matrix multiplication overflow
G0113 Unclosed (
G0114 Unclosed [

## G0115 Illegal redefinition of function

You are attempting to turn a function into a matrix or string. If this is a name conflict, delete the function.

## G0116 sysstate: invalid case

G0117 Invalid argument

## G0118 Argument must be integer

File handles must be integral.

## G0120 Illegal type for save

G0121 Matrix not positive definite
The matrix is either not positive definite, or singular using the current tolerance.

## G0122 Bad file handle

The file handle does not refer to an open file or is not in the valid range for file handles．

## G0123 File handle not open

The file handle does not refer to an open file．

## G0124 readr call too large

You are attempting to read too much in one call．

## G0125 Read past end of file

You have already reached the end of the file．
G0126 Error closing file
G0127 File not open for write
G0128 File already open
G0129 File not open for read
G0130 No output variables specified
G0131 Can＇t create file，too many variables
G0132 Can＇t write，disk probably full
G0133 Function too long
G0134 Can＇t seekr in this type of file
G0135 Can＇t seek to negative row
G0136 Too many arguments or misplaced assignment oper－ ator

You have an assignment operator (=) where you want a comparison operator (==), or you have too many arguments.

## G0137 Negative argument - erf or erfc

G0138 User keyword must have one argument
G0139 Negative parameter - Incomplete Beta
G0140 Invalid second parameter - Incomplete Beta
G0141 Invalid third parameter - Incomplete Beta
G0142 Nonpositive parameter - gamma
G0143 NaN or missing value - cdfchic
G0144 Negative parameter - cdfchic
G0145 Second parameter < 1.0 - cdfchic
G0146 Parameter too large - Incomplete Beta
G0147 Bad argument to trig function
G0148 Angle too large to trig function

## G0149 Matrices not conformable

For a description of the function or operator being used and conformability rules, see Matrix Operators, Section 10.2 , or the GAUSS LANGUAGE REFERENCE.

G0150 Matrix not square
G0151 Sort failure
G0152 Variable not initialized
You have referenced a variable that has not been initialized to any value.

## G0153 Unsuccessful close on auxiliary output

The disk may be full.

## G0154 Illegal redefinition of string <br> G0155 Nested procedure definition

A proc statement was encountered inside a procedure definition.

## G0156 Illegal redefinition of procedure

You are attempting to turn a procedure into a matrix or string. If this is a name conflict, delete the procedure.

## G0157 Illegal redefinition of matrix

## G0158 endp without proc

You are attempting to end a procedure that you never started.

## G0159 Wrong number of parameters

You called a procedure with the wrong number of arguments.
G0160 Expected string variable
G0161 User keywords return nothing
G0162 Can't save proc/ keyword/fn with global references
Remove the global references or leave this in source code form for the autoloader to handle. (See library in the GAUSS LANGUAGE REFERENCE.)

G0163 Wrong size format matrix
G0164 Bad mask matrix
G0165 Type mismatch or missing arguments
G0166 Character element too long

The maximum length for character elements is 8 characters.

## G0167 Argument must be column vector

## G0168 Wrong number of returns

The procedure was defined to return a different number of items.

## G0169 Invalid pointer

You are attempting to call a local procedure using an invalid procedure pointer.

## G0170 Invalid use of ampersand

## G0171 Called symbol is wrong type

You are attempting to call a local procedure using a pointer to something else.

## G0172 Can't resize temporary file

## G0173 varindx failed during open

The global symbol table is full.
G0174 '".' and '" " operators must be inside [ ] brackets
These operators are for indexing matrices.

## G0175 String too long to compare

G0176 Argument out of range
G0177 Invalid format string
G0178 Invalid mode for getf
G0179 Insufficient heap space
G0180 Trim too much
You are attempting to trim more rows than the matrix has.
G0181 Illegal assignment - type mismatch
G0182 2nd and 3rd arguments different order
G0274 Invalid parameter for conv
G0275 Parameter is NaN (Not A Number)
The argument is a NaN (see Special Data Types, Section 9.6.9).
G0276 Illegal use of reserved word
G0277 Null string illegal here
G0278 proc without endp
You must terminate a procedure definition with an endp statement.
G0286 Multiple assign out of memory
G0287 Seed not updatedThe seed argument to rndns and rndus must be a simple local or global variablereference. It cannot be an expression or constant. These functions are obsolete,please use rndlen and rndlcu
G0288 Found break not in do loop
G0289 Found continue not in do loop
G0290 Library not foundThe specified library cannot be found on the lib_path path. Make sure install-ation was correct.
G0291 Compiler pass out of memoryNotify Aptech Systems.
G0292 File listed in library not found

A file listed in a library could not be opened.

## G0293 Procedure has no definition

The procedure was not initialized. Define it.

## G0294 Error opening temporary file

One of the temporary files could not be opened. The directory may be full.
G0295 Error writing temporary file
One of the temporary files could not be written to. The disk may be full.
G0296 Can't raise negative number to nonintegral power
G0300 File handle must be a scalar
G0301 Syntax error in library
G0302 File has been truncated or corrupted

| getname | File header cannot be read. |
| :--- | :--- |
| load | Cannot read input file, or file header cannot be read. |
| open | File size does not match header specifications, or file <br> header cannot be read. |

G0317 Can't open temp file
G0336 Disk full
G0339 Can't debug compiled program
G0341 File too big
G0347 Can't allocate that many globals
G0351 Warning: Not reinitializing : declare ?=

The symbol is already initialized. It will be left as is. G0352 Warning: Reinitializing : declare !=

The symbol is already initialized. It will be reset.
G0355 Wrong size line matrix
G0360 Write error
G0364 Paging error
G0365 Unsupported executable file type
G0368 Unable to allocate translation space
G0369 Unable to allocate buffer
G0370 Syntax Error in code statement
G0371 Syntax Error in recode statement
G0372 Token verify error
Notify Aptech Systems.

## G0373 Procedure definition not allowed

A procedure name appears on the left side of an assignment operator.
G0374 Invalid make statement
G0375 make Variable is a Number
G0376 make Variable is Procedure
G0377 Cannot make Existing Variable
G0378 Cannot make External Variable
G0379 Cannot make String Constant

## G0380 Invalid vector statement

G0381 vector Variable is a Number
G0382 vector Variable is Procedure
G0383 Cannot vector Existing Variable
G0384 Cannot vector External Variable
G0385 Cannot vector String Constant
G0386 Invalid extern statement
G0387 Cannot extern number
G0388 Procedures always external
A procedure name has been declared in an extern statement. This is a warning only.

G0389 extern variable already local
A variable declared in an extern statement has already been assigned local status.

G0390 String constant cannot be external
G0391 Invalid code statement
Error Messages
G0392 code Variable is a Number
G0393 code Variable is Procedure
G0394 Cannot code Existing Variable
G0395 Cannot code External Variable
G0396 Cannot code String Constant
G0397 Invalid recode statement
G0398 recode Variable is a Number
G0399 recode Variable is Procedure
G0400 Cannot recode External Variable
G0401 Cannot recode String Constant
G0402 Invalid keep statement
G0403 Invalid drop statement
G0404 Cannot define Number'
G0405 Cannot define String
G0406 Invalid select statement
G0407 Invalid delete statement
G0408 Invalid outtyp statement
G0409 outtyp aiready defaulted to 8
Character data has been found in the output data set before an outtyp 2 or outtyp 4 statement. This is a warning only.
G0410 outtyp must equal 2 , 4, or 8
G0411 outtyp override...precision set to 8
Character data has been found in the output data set after an outtyp 2 or outtyp 4 statement. This is a warning only.
G0412 default not allowed in recode statement
default allowed only in code statement.

G0413 Missing file name in dataloop statement G0414 Invalid listwise statement

G0415 Invalid lag statement
G0416 lag variable is a number
G0417 lag variable is a procedure
G0418 Cannot lag External Variable
G0419 Cannot lag String Constant
G0421 Command not supported in Run-Time Module
G0428 Cannot use debug command inside program
G0429 Invalid number of subdiagonals
G0431 Error closing dynamic library
G0432 Error opening dynamic library
G0433 Cannot find DLL function
G0434 Error opening default dynamic library
G0435 Invalid mode
G0436 Matrix is empty
G0437 loadexe not supported; use dlibrary instead
G0438 callexe not supported; use dllcal! instead
G0439 File has wrong bit order
G0440 File has wrong byte order

G0441 Type vector malloc failed
G0442 No type vector in gfblock
G0445 Illegal left-hand side reference in procedure
G0446 Argument is the wrong size
G0447 vfor called with illegal loop level
G0454 Failure opening printer for output
G0456 Failure buffering output for printer
G0457 Cannot take log of a negative number
G0458 Attempt to index proc/fn/keyword as a matrix
G0459 Missing right brace
G0460 Unexpected end of statement
G0461 Too many data items
G0462 Negative trim value
G0463 Failure generating graph
G0465 Redefinition of structure, number of elements G0466 Redefinition of structure, type mismatch

G0467 Redefinition of structure, unrecognized member G0468 Structure definition inside procedure definition G0469 Cannot create translator temp file G0470 Symbol not found

G0472 Invalid name
G0473 String not terminated with null byte
G0477 FOR loops nested too deep
G0486 Character argument too long
G0487 License expired
G0490 License manager initialization error
G0491 License manager error
G0492 Licensing failure
G0497 Missing right parenthesis
G0500 Cannot create temporary filename
G0503 Cannot assign matrix to scalar member
G0504 Invalid structure member
G0505 Invalid structure redefinition
G0506 Structure assignment mismatch
G0507 Undefined structure
G0508 Structure argument mismatch
G0509 Too many structure members
G0510 Duplicate name for structure member
G0514 Not supported for structures
G0515 Too many values in locator

G0516 Too many dimensions in result
G0517 Too many dimensions in argument
G0518 Not implemented for complex
G0519 Illegal dereference of structure array
G0520 Arguments not conformable
G0521 Argument must be real
G0522 Illegal indexing of dereferenced structure
G0523 Numeric argument must be integer
G0524 Found comma, expecting index
G0525 Argument contains NaNs
G0526 Argument must be compact format
G0529 Array orders must be >= 1
G0531 Two trailing dimensions of argument must be the same size

G0532 Both dimensions of argument must be the same size
G0533 1-dimensional argument must contain only 1 element G0534 Cannot create file

G0538 Zero illegal in for loop increment
G0541 Illegal assignment to FOR loop counter
G0542 Object too large for 32-bit version
G0543 Array has too many dimensions for matrix assign

G0547 Array not conformable for indexing
G0548 Array not conformable for boolean operation
G0549 Global structure pointer cannot point to local structure

G0550 Invalid use of *
G0551 Feature not authorized
G0553 Path too long
G0554 Unable to create sparse matrix
G0555 Cannot index uninitialized structure
G0556 \#IF nesting limit exceeded
G0557 \#ELSE without \#IF
G0558 \#ENDIF without \#IF
G0559 Symbol not \#DEFINE'd
G0560 Too many \#DEFINE's
G0561 Duplicate \#DEFINE
G0562 Open /* */comment
G0563 Open @ @ comment
G0564 Illegal redefinition of sparse matrix
G0565 Initializer too large, increase maxdeclet in config (.cfg) file

G0566 Can't create profiler data file

G0567 Sparse matrix uninitialized
G0568 Operation not defined for triangular, symmetric, or Hermitian sparse matrix

G0569 Argument must be complex
G0570 Diagonal must be real
G0571 Diagonal must not contain zeros
G0572 Argument must be triangular
G0573 Argument must be symmetric
G0574 Sparse type mismatch
G0575 Unable to load variable
G0576 Threading error
G0577 Expected THREADSTAT, THREADBEGIN, or THREADJOIN

G0578 A THREADJOIN failed
G0579 Cannot call RUN from inside thread
G0580 Unable to converge in allowed number of iterations
G0581 Incorrect Argument: Number of eigenvalues must be positive

G0582 Incorrect Argument: Number of column vectors must be >= number of eigenvalues +2 and < rows of input matrix G0583 Could not apply shift during an Arnoldi iteration cycle. Try increasing size of ncv

G0584 Invalid Input: 'which' must be 'LM' 'SM' 'LR' 'LI' 'SR' or 'SI' and type string

G0585 Error Return from LAPACK eigenvalue calculation
G0586 dneupd error 1: contact Aptech Systems
G0587 Input matrix must be sparse
G0588 Incorrect Input: Number of eigenvalues must be scalar

G0589 Incorrect Input: Tolerance must be scalar
G0590 No eigenvalues found to specified tolerance in allowed iterations

G0591 Incorrect Input: Max iterations must be scalar
G0592 Incorrect Input: Number of column vectors must be scalar

G0593 Incorrect Input: Third input, probability, must be >0 and < 1

G0594 Incorrect Input: Number of successes (input 1) must be less than number of trials (input 2)

G0595 Incorrect Input: State vector cannot have more than

G0596 Incorrect Input: Inputs 1 and 2 (cols and rows) must be scalar or $1 \times 1$ matrix

G0597 Incorrect Input: Input must be dense matrix G0598 Incorrect Input: First input may have 1 column only

G0599 Incorrect Input: Input 2 may not have more columns that input 1 has rows

G0600 Incorrect Input: Input 1 must be square G0601 Incorrect Input: Input 2 must be square G0602 Incorrect Input: 1 <= il < iu and iu <= rows of $x$ G0603 Failure to converge

## 30 Maximizing Performance

These hints will help you maximize the performance of your new GAUSS System.

### 30.1 Library System

Some temporary files are created during the autoloading process. If you have a tmp path configuration variable or a tmp environment string that defines a path on a RAM disk, the temporary files will be placed on the RAM disk.

For example:

```
set tmp=f:\tmp
```

tmp path takes precedence over the tmp environment variable.
A disk cache will also help, as well as having your frequently used files in the first path in the src_path.

You can optimize your library . lcg files by putting the correct drive and path on each file name listed in the library. The lib command will do this for you.

Use the compile command to precompile your large frequently used programs. This will completely eliminate compile time when the programs are rerun.

### 30.2 Loops

The use of the built-in matrix operators and functions rather than do loops will ensure that you are utilizing the potential of GAUSS.

Here is an example:
Given the vector $x$ with 8000 normal random numbers,

```
x = rndn(8000,1);
```

you could get a count of the elements with an absolute value greater than 1 with a do loop, like this:

```
c = 0;
i = 1;
do while i <= rows(x);
    if abs(x[i]) > 1;
        c = c+1;
    endif;
    i = i+1;
endo;
print c;
```

Or, you could use:

```
c = sumc(abs(x) .> 1);
print c;
```

The do loop takes over 40 times longer.

### 30.3 Memory Usage

Computers today can have large amounts of RAM. This doesn't mean that large data sets should be read entirely into memory. Many GAUSS procedures and applications are written to allow for data sets to be read in sections rather than all at once. Even if you have enough RAM to store the data set completely, you should consider taking
advantage of this feature. The speed-ups using this feature can be significant. For example, ols is called using a data set stored in a matrix versus stored on the disk in a GAUSS data set. The computer is a 2.8 Megahertz computer with Windows XP.

```
y = rndn (250000,1);
x = rndn (250000,100);
xlbl = 0$+"X"+ftocv(seqa (1,1,100),1,0);
lbl = "Y" | xlbl;
call saved(y~x,"test",lbl);
__output = 0;
t0 = date;
call ols("",y,x);
t1 = date;
t2 = date;
call ols("test", "Y",xlbl);
t3 = date;
print ethsec(t2,t3)/100 " seconds";
print;
print ethsec(t0,t1)/100 " seconds";
    25.750000 seconds
    9.6720000 seconds
```

This represents more than a $50 \%$ speedup by leaving the data on the disk.

## maxvec, maxbytes

maxvec is a GAUSS procedure that returns the value of the global variable maxvec that determines the amount of data to be read in at a time from a GAUSS data set. This value can be modified for a particular run by setting $\qquad$ maxvec in your command file to some other value. The value returned by a call to maxvec can be permanently modified by editing system. dec and changing the value of $\qquad$ maxvec. The value returned when running GAUSS Light is always 8192 .
maxbytes is a GAUSS procedure that returns the value of a scalar global $\qquad$ maxbytes that sets the amount of available RAM. This value can be modified for a particular run by setting $\qquad$ maxbytes in your command file to some other value. The value returned by a call to maxbytes can be permanently modified by editing sys tem. dec and changing the value of $\qquad$ maxbytes.

If you wish to force GAUSS procedures and applications to read a GAUSS data set in its entirety, set $\qquad$ maxvec and maxbytes to very large values.

### 30.3.1 Hard Disk Maintenance

The hard disk used for the swap file should be optimized occasionally with a disk optimizer. Use a disk maintenance program to ensure that the disk media is in good shape.

### 30.3.2 CPU Cache

There is a line for cache size in the gauss.cfg file. Set it to the size of the CPU data cache for your computer.

This affects the choice of algorithms used for matrix multiply functions.
This will not change the results you get, but it can radically affect performance for large matrices.

## 31 GAUSS Graphics Colors

The following is a chart and list of colors available for use in GAUSS graphics with both the name and RGB value listed.

|  | Color Name | RGB Value |
| :--- | :--- | :--- |
|  | aliceblue | $240,248,255$ |
|  | antiquewhite | $250,235,215$ |
|  | aqua | $0,255,255$ |
|  | aquamarine | $127,255,212$ |
|  | azure | $240,255,255$ |
|  | beige | $245,245,220$ |
|  | bisque | $255,228,196$ |
|  | black | $0,0,0$ |
|  | blanchedalmond | $255,235,205$ |
|  | blue | $0,0,255$ |
|  | blueviolet | $138,43,226$ |
|  | brown | $165,42,42$ |
|  | burlywood | $222,184,135$ |
|  | cadetblue | $95,158,160$ |
|  | chartreuse | $127,255,0$ |
|  | chocolate | $210,105,30$ |
|  | coral | $255,127,80$ |
|  | comflowerblue | $100,149,237$ |
|  | comsilk | $255,248,220$ |
|  | crimson | $220,20,60$ |
|  | cyan | $0,255,255$ |
|  | darkblue | $0,0,139$ |
|  | darkcyan | $0,139,139$ |
|  | darkgoldenrod | $184,134,11$ |
|  | darkgray | $169,169,169$ |
|  | darkgreen | $0,100,0$ |
|  | darkgrey | $169,169,169$ |
|  | darkkhaki | $189,183,107$ |
|  | darkmagenta | $139,0,139$ |
|  | darkolivegreen | $85,107,47$ |
|  | darkorange | $255,140,0$ |
|  | darkorchid | $153,50,204$ |
|  | darkred | $139,0,0$ |
|  | darksalmon | $233,150,122$ |
|  | darkseagreen | $143,188,143$ |
|  | darkslateblue | $72,61,139$ |
|  | darkslategray | $47,79,79$ |
|  | darkslategrey | $47,79,79$ |
|  | darkturquoise | $0,206,209$ |
| darkviolet | $148,0,211$ |  |
| deeppink | $255,20,147$ |  |
| dimgray | 105,105 |  |
|  |  |  |


|  | Color Name | $R G B$ Value |
| :--- | :--- | :--- |
|  | dimgrey | $105,105,105$ |
|  | dodgerblue | $30,144,255$ |
|  | frebrick | $178,34,34$ |
|  | floralwhite | $255,250,240$ |
|  | forestgreen | $34,139,34$ |
|  | fuchsia | $255,0,255$ |
|  | gainsboro | $220,220,220$ |
|  | ghostwhite | $248,248,255$ |
|  | gold | $255,215,0$ |
|  | goldenrod | $218,165,32$ |
|  | gray | $128,128,128$ |
|  | grey | $128,128,128$ |
|  | green | $0,128,0$ |
|  | greenyellow | $173,255,47$ |
|  | honeydew | $240,255,240$ |
|  | hotpink | $255,105,180$ |
|  | indianred | $205,92,92$ |
|  | indigo | $75,0,130$ |
|  | ivory | $255,255,240$ |
|  | khaki | $240,230,140$ |
|  | lavender | $230,230,250$ |
|  | lavenderblush | $255,240,245$ |
|  | lawngreen | $124,252,0$ |
|  | lemonchiffon | $255,250,205$ |
|  | lightblue | $173,216,230$ |
|  | lightcoral | $240,128,128$ |
|  | lightcyan | $224,255,255$ |
|  | lightgoldenrodyellow | $250,250,210$ |
|  | lightgray | $211,211,211$ |
|  | lightgreen | $144,238,144$ |
|  | lightgrey | $211,211,211$ |
|  | lightpink | $255,182,193$ |
|  | lightsalmon | $255,160,122$ |
|  | lightseagreen | $32,178,170$ |
|  | lightskyblue | $135,206,250$ |
|  | lightslategray | $119,136,153$ |
|  | lightslategrey | $119,136,153$ |
|  | lightsteelblue | $176,196,222$ |
|  | lightyellow | $255,255,224$ |
|  | lime | $0,255,0$ |
|  | limegreen | $50,205,50$ |
|  | linen | $250,240,230$ |
|  | magenta | $255,0,255$ |
|  |  |  |


|  | Color Name | $R G B$ Value |
| :--- | :--- | :--- |
|  | maroon | $128,0,0$ |
|  | mediumaquamarine | $102,205,170$ |
|  | mediumblue | $0,0,205$ |
|  | mediumorchid | $186,85,211$ |
|  | mediumpurple | $147,112,219$ |
|  | mediumseagreen | $60,179,113$ |
|  | mediumslateblue | $123,104,238$ |
|  | mediumspringgreen | $0,250,154$ |
|  | mediumturquoise | $72,209,204$ |
|  | mediumvioletred | $199,21,133$ |
|  | midnightblue | $25,25,112$ |
|  | mintcream | $245,255,250$ |
|  | mistyrose | $255,228,225$ |
|  | moccasin | $255,228,181$ |
|  | navajowhite | $255,222,173$ |
|  | navy | $0,0,128$ |
|  | oldlace | $253,245,230$ |
|  | olive | $128,128,0$ |
|  | olivedrab | $107,142,35$ |
|  | orange | $255,165,0$ |
|  | orangered | $255,69,0$ |
|  | orchid | $218,112,214$ |
|  | palegoldenrod | $238,232,170$ |
|  | palegreen | $152,251,152$ |
|  | paleturquoise | $175,238,238$ |
|  | palevioletred | $219,112,147$ |
|  | papayawhip | $255,239,213$ |
|  | peachpuff | $255,218,185$ |
|  | peru | $205,133,63$ |
|  | pink | $255,192,203$ |
|  | plum | $221,160,221$ |
|  | powderblue | $176,224,230$ |
|  | purple | $128,0,128$ |
|  | red | 252,45 |
|  | rosybrown | $188,143,143$ |
|  | royalblue | $65,105,225$ |
|  | saddlebrown | $139,69,19$ |
|  | salmon | $250,128,114$ |
|  | sandybrown | $244,164,96$ |
|  | seagreen | $46,139,87$ |
|  | seashell | sienna |
|  | silver | 253 |
|  |  |  |


|  | Color Name | RGB Value |
| :--- | :--- | :--- |
|  | skyblue | $135,206,235$ |
|  | slateblue | $106,90,205$ |
|  | slategray | $112,128,144$ |
|  | slategrey | $112,128,144$ |
|  | snow | $255,250,250$ |
|  | springgreen | $0,255,127$ |
|  | steelblue | $70,130,180$ |
|  | tan | $210,180,140$ |
|  | teal | $0,128,128$ |
|  | thistle | $216,191,216$ |
|  | tomato | $255,99,71$ |
|  | turquoise | $64,224,208$ |
|  | violet | $238,130,238$ |
|  | wheat | $245,222,179$ |
|  | white | $255,255,255$ |
|  | whitesmoke | $245,245,245$ |
|  | yellow | $255,255,0$ |
|  | yellowgreen | $154,205,50$ |

## 32 Reserved Words

The following words are used for GAUSS functions. You cannot use these names for variables or procedures in your programs:

A

| abs | AmericanBinomPut_Greeks |
| :--- | :--- |
| acf | AmericanBinomPut_ImpVol |
| aconcat | AmericanBSCall |
| acos | AmericanBSCall_Greeks |
| aeye | AmericanBSCall_ImpVol |
| amax | AmericanBSPut |
| amean | AmericanBSPut_Greeks |
| AmericanBinomCall_ImpVol |  |
| AmericanBinomCall_Greeks | AmericanBSPut_Impl_ImpVol |
| AmericanBinomCall_amin |  |
| AmericanBinomPut | amult |


| annotationGetDefaults | asum |
| :--- | :--- |
| annotationSetBkd | atan |
| annotationSetFont | atan2 |
| annotationSetLineColor | atranspose |
| annotationSetLineStyle | axmargin |
| annotationSetLineThickne B |  |
| ss | balance |
| annualTradingDays | band |
| arccos | bandchol |
| arcsin | bandcholsol |
| arctan | bandrv |
| arctan2 | bandsolpd |
| areshape | bar |
| arrayalloc | base10 |
| arrayindex | begwind |
| arrayinit | besselj |
| arraytomat | beta |
| asciiload | box |
| asclabel | asin |
| astd | astds |


| calcbox | cdfGenPareto |
| :--- | :--- |
| call | cdfLaplace |
| callexe | cdfLaplaceInv |
| cdfBeta | cdfLogistic |
| cdfBetaInv | cdfLogisticInv |
| cdfBinomial | cdfMvn |
| cdfBinomialInv | cdfMvn2e |
| cdfBvn | cdfMvnce |
| cdfBvn2 | cdfMvne |
| cdfBvn2e | cdfMvt2e |
| cdfCauchy | cdfMvtce |
| cdfCauchyInv | cdfMvte |
| cdfChic | cdfn |
| cdfChii | cdfN2 |
| cdfChinc | cdfNc |
| cdfExp | cdfNcd |
| cdfExpInv | cdfNegBinomial |
| cdfFc | cdfNegBinomialInv |
| cdfFnc | cdfNi |
| cdfFncInv | cdfPoisson |
| cdfGam |  |


|  | cdfRayleigh | cint |
| :---: | :---: | :---: |
|  | cdfRayleighInv | clear |
|  | cdftc | clearg |
|  | cdftci | close |
|  | cdftnc | closeall |
|  | cdftvn | cls |
|  | cdfWeibull | cmsplit |
|  | cdfWeibullInv | cmsplit2 |
|  | cdir | code |
|  | ceil | color |
|  | cfft | cols |
|  | cffti | colsf |
|  | ChangeDir | combinate |
|  | chdir | combinated |
|  | checkinterrupt | comlog |
|  | chiBarSquare | commandeerm |
|  | chol | commandeersa |
|  | choldn | compile |
|  | cholsol | complex |
|  | cholup | con |
|  | chrs | cond |


| conformed | crout |
| :--- | :--- |
| conj | croutp |
| cons | csrcol |
| conscore | csrlin |
| continue | csrtype |
| contour | cumprodc |
| conv | cumsumc |
| convertsatostr | curve |
| convertstrtosa | cvtosa |
| coreleft | datacreate |
| corrm | datacreatecomplex |
| corrms | datalist |
| corrvc | dataload |
| corrx | dataloop |
| corrxs | dataopen |
| cos | datasave |
| cosh | date |
| counts | datestr |
| countwts | create |

dayinyr
dayOfWeek
dbAddDatabase
dbClose
dbCommit
dbCreateQuery
dbExecQuery
dbGetConnectOptions
dbGetDatabseName
dbGetDriverName
dbGetDrivers
dbGetHostName
dbGetLastErrorNum
dbGetLastErrorText
dbGetNumericalPrecPolicy
dbGetPassword
dbGetPort
dbGetPrimaryIndex
dbGetTableHeaders
dbGetTables
dbGetUserName
dbHasFeature
dbIsDriverAvailable
dbIsOpen
dbIsOpenError
dbNumericalPrecPolicy
>dbOpen
dbQueryBindValue
dbQueryClear
dbQueryCols
dbQueryExecPrepared
dbQueryFetchAllM
dbQueryFetchAllSA
dbQueryFetchNextM
dbQueryFetchNextSA
dbQueryFinish
dbQueryGetBoundValue
dbQueryGetBoundValues
dbQueryGetField
dbQueryGetLastErrorNum
dbQueryGetLastErrorText
dbQueryGetLastInsertID

| dbQueryGetLastQuery | dbSetPort |
| :--- | :--- |
| dbQueryGetPosition | dbSetUserName |
| dbQueryIsActive | dbTransaction |
| dbQueryIsForwardOnly | debug |
| dbQueryIsNull | declare |
| dbQueryIsSelect | delete |
| dbQueryIsValid | DeleteFile |
| dbQueryPrepare | delif |
| dbQueryRows | delrows |
| dbQuerySeek | denseSubmat |
| dbQuerySeekFirst | denseToSp |
| dbQuerySeekLast | denseToSpRE |
| dbQuerySeekNext | denseToZero |
| dbQuerySeekPrevious | design |
| dbQuerySetForwardOnly | det |
| dbRemoveDatabase | detl |
| dbRollback | dfft |
| dbSetConnectoptions | dffti |
| dbSetDatabaseName | diagee |
| dbSetHostName | diag |
| dbSetPassword |  |


| digamma | draw |
| :--- | :--- |
| disable | dsCreate |
| dlibrary | dstat |
| dllcall | dstatmt |
| do | dstatmtControlCreate |
| dos | dtdate |
| doswin | dtday |
| DosWinCloseall | dttime |
| DoSWinOpen | dttodtv |
| dotfeq | dttostr |
| dotfeqmt | dttoutc |
| dotfge | dtvnormal |
| dotfgemt | dtvtodt |
| dotfgt | dtvtoutc |
| dotfgtmt | dummy |
| dotfle | dummybr |
| dotflemt | edimmydn |
| dotflt | edig |
| dotfltmt | exfne |


| eigcg | envget |
| :--- | :--- |
| eigcg2 | eof |
| eigch | eq |
| eigch2 | eqSolve |
| eigh | eqSolvemt |
| eighv | eqSolvemtControlCreate |
| eigrg | eqSolvemtOutCreate |
| eigrg2 | eqSolveSet |
| eigrs | eqv |
| eigrs2 | erf |
| eigv | erfc |
| elapsedTradingDays | erfcplx |
| else | erfccplx |
| elseif | erfCInv |
| enable | erfInv |
| end | error |
| endfor | errorlog |
| endif | errorlogat |
| endo | etdays |
| endp | ethsec |
| endwind |  |
| etstr |  |


| EuropeanBinomCall__Greans | fcheckerr |
| :--- | :--- |
| EuropeanBinomCall_Greeks | fclearerr |
| EuropeanBinomCall_ImpVol | feq |
| EuropeanBinomPut | feqmt |
| EuropeanBinomPut_Greeks | fflush |
| EuropeanBinomPut_ImpVol | fft |
| EuropeanBSCall | ffti |
| EuropeanBSCall_Greeks | fftm |
| EuropeanBSCall_ImpVol | fftmi |
| EuropeanBSPut | fftn |
| EuropeanBSPut_Greeks | fge |
| EuropeanBSPut_ImpVol | fgemt |
| exctsmpl | fgets |
| exec | fgetsa |
| execbg | fgetsat |
| exp | fgetst |
| expr | fgt |
| extern | fgtmt |
| external | fileinfo |
| eye | files |
|  |  |


| fix | fputst |
| :--- | :--- |
| fle | fseek |
| flemt | fstrerror |
| floor | ftell |
| flt | ftocv |
| fltmt | ftos |
| fmod | ftostrc |
| fn |  |
| fne | gamma |
| fnemt | gammacplx |
| font | gammaii |
| fontload | gausset |
| fonts | gdaAppend |
| fontunload | gdaCreate |
| fontunloadall | gdaDStat |
| fopen | gdaDStatMat |
| for | gdaGetIndex |
| format | gdaGetName |
| formatcv | gdaGetNames |
| formatnv | gdaGetOrders |
| fputs | gdaGetType |
|  |  |


| gdaGetVarInfo | getmatrix4D |
| :--- | :--- |
| gdaIsCplx | getname |
| gdaLoad | getnamef |
| gdaPack | getNextTradingDay |
| gdaRead | getNextWeekDay |
| gdaReadByIndex | getnr |
| gdaReadSome | getnrmt |
| gdaReadSparse | getorders |
| gdaReadStruct | getpath |
| gdaReportVarInfo | getPreviousTradingDay |
| gdaSave | getPreviousWeekDay |
| gdaUpdate | getRow |
| gdaUpdateAndPack | getscalar3D |
| gdaWrite | getscalar4D |
| gdaWriteSome | getTrRow |
| gdtfastcat | getwind |
| ge | gosub |
| getarray | goto |
| getdims | gradMT |
| getf | gradMTm |


| gradMTT | hessMTT |
| :--- | :--- |
| gradp | hessMTG |
| gradpcplx | hessMTTgw |
| graph | hessMTTm |
| graphgpg | hessMTTmw |
| graphprt | hessMTTw |
| graphset | hesscplx |
| graphsev3 | hessp |
| gt | hist |
| hardcopy | histf |
| hasimag | histp |
| header | hsec |
| headermt | hess |
| hessMTm | iff |
| hessMTg | imag |
| hessMTw | include |



| lapgeigh | lncdfbvn2 |
| :--- | :--- |
| lapgeighv | lncdfmvn |
| lapgeigv | lncdfn |
| lapgschur | lncdfn2 |
| lapgsvdcst | lncdfnc |
| lapgsvds | lnfact |
| lapgsvdst | lngamma |
| lapsvdcusv | lngammacplx |
| lapsvds | lnpdfmvn |
| lapsvdusv | lnpdfmvt |
| ldlp | lnpdfn |
| ldlsol | lnpdft |
| le | load |
| let | loadarray |
| lib | loadd |
| library | loadexe |
| license_id | loadf |
| line | loadk |
| linsolve | loadm |
| lncdfbvn | loads |



```
meanc
median new
mergeby
mergebysa
mergevar nextnevn
minc
minindc
minv null
miss null1
missex numCombinations
missrv O
moment oldfft
momentd
movingave
movingaveExpwgt
movingaveWgt
msym
N
nametype
ndpchk
ndpclex
ndpcntrl
ne
nextn
not
oldffti
ols
olsmt
    olsmtControlCreate
olsqr
olsqr2
olsqrmt
ones
open
O
oldfft
*
openpqg
```

| optn | pinvmt |
| :---: | :---: |
| optnevn | plot |
| or | plotAddBar |
| orth | plotAddHist |
| output | plotAddHistF |
| outwidth | plotAddHistP |
|  | plotAddScatter |
| pacf | plotAddTS |
| packedToSp | plotAddXY |
| packr | plotAddArrow |
| parse | plotAddArea |
| pause | plotAddShape |
| pdfCauchy | plotAddTextbox |
| pdfexp | plotArea |
| pdfGenPareto | plotBar |
| pdfLaplace | plotClearLayout |
| pdfLogistic | plotContour |
| pdfn | plotCustomLayout |
| pdfRayleigh | plotGetDefaults |
| pdfeibull | plotHist |
| pi | plotHistF |
| pinv |  |


| plotHistP | plotSetXLabel |
| :--- | :--- |
| plotLayout | plotSetXRange |
| plotLogLog | plotSetXTicCount |
| plotLogX | plotSetXTicInterval |
| plotLogY | plotSetXTicLabel |
| plotOpenWindow | plotSetYLabel |
| plotPolar | plotSetYRange |
| plotSave | plotSetYTicCount |
| plotScatter | plotSetZLabel |
| plotSetBar | plotSurface |
| plotSetBkdColor | plotsym |
| plotSetFill | plotTS |
| plotSetGrid | plotXY |
| plotSetLegend | polar |
| plotSetLineColor | polychar |
| plotSetLineStyle | polyeval |
| plotSetLineSymbol | polygamma |
| plotSetLineThickness | polyint |
| plotSetNewWindow | polymake |
| plotSetWhichYAxis |  |


| polymult | pvGetParVector |
| :---: | :---: |
| polyroot | pvLength |
| pop | pvList |
| pqgwin | pvnumoffsets |
| presn | proffsets |
| previousindex | prPack |
| princomp | pvPacki |
| print | pvPackm |
| printdos | pvPackmi |
| printfm | pvPacks |
| printfmt | pvPacksi |
| proc | pvPacksm |
| prode | pvPacksmi |
| psi | pvPutParVector |
| push | pvTest |
| putarray | pvUnpack |
| putf | Q |
| putvals | QNewton |
| pvCreate | QNewtonmt |
| pvGetIndex | QNewtonmtControlCreate |
| pvGetParnames | QNewtonmtOutCreate |
|  | QNewtonSet |


| QProg | rank |
| :--- | :--- |
| QProgmt | rankindx |
| QProgmtInCreate | readr |
| qqre | real |
| qqrep | recode |
| qr | recserar |
| qre | recsercp |
| qrep | register_off |
| qrsol | register_on |
| qrtsol | register_reset |
| qtyr | register_show |
| qtyre | replay |
| qtyrep | rerun |
| quantile | reshape |
| quantiled | retp |
| quantilem | return |
| quantilemd |  |
| qyr |  |


| rfftip | rndKMnb |
| :--- | :--- |
| rfftn | rndKMp |
| rfftnp | rndKMu |
| rfftp | rndKMvm |
| rndBernoulli | rndLaplace |
| rndBeta | rndLCbeta |
| rndCauchy | rndLCgam |
| rndChiSquare | rndLCi |
| rndcon | rndLCn |
| rndbeta | rndLCnb |
| rndCreateState | rndLCu |
| rndExp | rndLCvm |
| rndgam | rndLogNorm |
| rndGamma | rndmod |
| rndGeo | rndmult |
| rndGumbel | rndMVn |
| rndi | rndMVt |
| rndKMbeta | rndKMgam |
| rndKMn |  |



| setvmode | sortr |
| :--- | :--- |
| setvwrmode | sortrc |
| setwind | sparseCols |
| shell | sparseEye |
| shiftr | sparseFD |
| show | sparseFP |
| showpqg | sparseHConcat |
| sin | sparseNZE |
| singleindex | sparseOnes |
| sinh | sparseRows |
| sleep | sparseScale |
| solpd | sparseSet |
| sortc | sparseSolve |
| sortcc | sparseSubmat |
| sortd | sparseTD |
| sorthc | sparseTranspose |
| sorthcc | sparseTrTD |
| sortind | sparseTscalar |
| sortindc | sparseVConcat |
| sortindmc | spChol |
| sortmc | spConadSol |
| spara |  |


| spCreate | spZeroes |
| :--- | :--- |
| spDenseSubmat | sqpmt_feasible |
| spDiagRvMat | sqpmt_meritFunct |
| spEigv | sqpSolve |
| spEye | sqpSolveMT |
| spGetNZE | sqpSolveMTcontrolCreate |
| spLDL | sqpSolveMTlagrangeCreate |
| spline | sqpSolveMToutCreate |
| spline1D | sqpSolveset |
| spline2D | sqrt |
| spLU | stdc |
| spNumNZE | stdsc |
| spOnes | stocv |
| SpreadsheetReadM | stof |
| SpreadsheetReadSA | stop |
| SpreadsheetWrite | strcombine |
| spScale | strindx |
| spSubmat | string |
| spToDense | strlen |
| spTrTDense | strput |
| spTScalar | strindx |


| strsect | svd |
| :--- | :--- |
| strsplit | svd1 |
| strsplitPad | svd2 |
| strtodt | svdcusv |
| strtodtd | svds |
| strtof | svdusv |
| strtofcplx | sysstate |
| strtriml | system |
| strtrimr | tab |
| strtrunc | tan |
| strtruncl | tanh |
| strtruncpad | tempname |
| strtruncr | ThreadBegin |
| struct | ThreadEnd |
| submat | threadfor |
| subscat | threadendfor |
| substute | ThreadJoin |
| subvec | timeadStat |
| sumc | sumr |


| timeutc | union |
| :--- | :--- |
| title | unionsa |
| tkf2eps | uniqindmc |
| tkf2ps | uniqindx |
| tkf2ps_margin | uniqindxsa |
| tocart | unique |
| todaydt | uniquemc |
| toeplitz | uniquesa |
| token | until |
| topolar | upmat |
| trace | upmat1 |
| trap | upper |
| trapchk | use |
| trigamma | utctodt |
| trim | utctodtv |
| trimr | utrisol |
| trunc | varCovMS |
| type | varCovx |
| typecv | vapef |


|  | varget |  | volume |
| :---: | :---: | :---: | :---: |
|  | vargetl |  | vput |
|  | varmall |  | vread |
|  | varmares |  | vtypecv |
|  | varput | W |  |
|  | varputl |  | wait |
|  | vartype |  | waitc |
|  | vartypef |  | walkindex |
|  | vcm |  | while |
|  | vcms |  | winclear |
|  | vcx |  | wincleararea |
|  | vcxs |  | winclearttylog |
|  | vec |  | winclose |
|  | vech |  | wincloseall |
|  | vecr |  | winconvertpqg |
|  | vfor |  | window |
|  | vget |  | wingetactive |
|  | view |  | wingetattributes |
|  | viewxyz |  | wingetcolorcells |
|  | vlist |  | wingetcursor |
|  | vnamecv |  | winmove |
|  |  |  | winopenpqg |

winopentext
winopentty
winpan
winprint
winprintpqg
winrefresh
winrefresharea
winresize
winsetactive
winsetbackground
winsetcolor
winsetcolorcells
winsetcolormap
winsetcursor
winsetforeground
winsetrefresh
winsettextwrap
winwrite
winzoompqg
writer
X
x_indev
xlsGetSheetCount
xlsGetSheetSize
xlsMakeRanget
xlsReadM
xlsReadSA
xlsWrite
xlsWriteM
xlsWriteSA
xlabel
xor
xpnd
xtics
$x y$
xyz

Y
ylabel
ytics
Z
zeros
zeta
zlabel

## ztics

## 33 Singularity Tolerance

The tolerance used to determine whether or not a matrix is singular can be changed. The default value is $1.0 \mathrm{e}-14$ for both the LU and the Cholesky decompositions. The tolerance for each decomposition can be changed separately. The following operators are affected by a change in the tolerance:

## Crout LU Decomposition

```
crout(x)
croutp(x)
inv(x)
det(x)
y/x when neither }x\mathrm{ nor }y\mathrm{ is scalar and }x\mathrm{ is square.
```


## Cholesky Decomposition

```
chol(x)
```

chol(x)
invpd(x)

```
\(\operatorname{solpd}(y, x)\)
\(y / x \quad\) when neither \(x\) nor \(y\) is scalar and \(x\) is not square.

\subsection*{33.1 Reading and Setting the Tolerance}

The tolerance value may be read or set using the sysstate function, cases 13 and 14 .

\subsection*{33.2 Determining Singularity}

There is no perfect tolerance for determining singularity. The default is \(1.0 \mathrm{e}-14\). You can adjust this as necessary.

A numerically better method of determining singularity is to use cond to determine the condition number of the matrix. If the equation
```

1 / cond(x) + 1 eq 1

```
is true, then the matrix is usually considered singular to machine precision. (See LAPACK for a detailed discussion on the relationship between the matrix condition and the number of significant figures of accuracy to be expected in the result.)

\section*{34 Publication Quality Graphics}

GAUSS Publication Quality Graphics (PQG) is a set of routines built on the graphics functions in GraphiC by Scientific Endeavors Corporation. These routines are deprecated but included for backward compatibility.

The main graphics routines include \(x y\), \(x y z\), surface, polar and \(\log\) plots, as well as histograms, bar, and box graphs. Users can enhance their graphs by adding legends, changing fonts, and adding extra lines, arrows, symbols and messages.

The user can create a single full size graph, inset a smaller graph into a larger one, tile a window with several equally sized graphs or place several overlapping graphs in the window. Graphic panel size and location are all completely under the user's control.

\subsection*{34.1 General Design}

GAUSS PQG consists of a set of main graphing procedures and several additional procedures and global variables for customizing the output.

All of the actual output to the window happens during the call to these main routines:
\begin{tabular}{ll} 
bar & Bar graphs. \\
box & Box plots. \\
contour & Contour plots. \\
draw & Draw graphs using only global variables. \\
hist & Histogram. \\
histp & Percentage histogram.
\end{tabular}
\begin{tabular}{ll} 
histf & Histogram from a vector of frequencies. \\
loglog & Log scaling on both axes. \\
logx & Log scaling on \(X\) axis. \\
logy & Log scaling on Y axis. \\
polar & Polar plots. \\
surface & 3-D surface with hidden line removal. \\
\(x y\) & Cartesian graph. \\
\(x y z\) & 3-D Cartesian graph.
\end{tabular}

\subsection*{34.2 Using Publication Quality Graphics}

\subsection*{34.2.1 Getting Started}

There are four basic parts to a graphics program. These elements should be in any program that uses graphics routines. The four parts are the header, data setup, graphics format setup, and graphics call.

\section*{Header}

In order to use the graphics procedures, the pgraph library must be activated. This is done in the library statement at the top of your program or command file. The next line in your program will typically be a command to reset the graphics global variables to their default state. For example:
```

library mylib, pgraph;
graphset;

```

\section*{Data Setup}

The data to be graphed must be in matrices. For example:
```

x = seqa(1,1,50);
y = sin(x);

```

\section*{Graphics Format Setup}

Most of the graphics elements contain defaults that allow the user to generate a plot without modification. These defaults, however, may be overridden by the user through the use of global variables and graphics procedures. Some of the elements that may be configured by the user are axes numbering, labeling, cropping, scaling, line and symbol sizes and types, legends, and colors.

\section*{Calling Graphics Routines}

The graphics routines take as input the user data and global variables that have previously been set. It is in these routines where the graphics file is created and displayed.

Following are three PQG examples. The first two programs are different versions of the same graph. The variables that begin with _p are the global control variables used by the graphics routines. (For a detailed description of these variables, see Global Control Variables, Section 34.6 .)

Example 1 The routine being called here is a simple XY plot. The entire window will be used. Four sets of data will be plotted with the line and symbol attributes automatically selected. This graph will include a legend, title, and a time/date stamp (time stamp is on by default):
```

library pgraph;
graphset;
x = seqa(.1,.1,100);
y = sin(x);
y = y ~ y*.8 ~ y*.6 ~ y*.4; /* 4 curves plotted against x
*/
_plegctl = 1; /* legend on */
title("Example xy Graph"); /* Main title */
xy(x,y); /* Call to main routine */

```

Example 2 Here is the same graph with more of the graphics format controlled by the user. The first two data sets will be plotted using symbols at data points only (observed data); the data points in the second two sets will be connected with lines (predicted results):
```

library pgraph;
*/
graphset;
*/
x = seqa(.1,.1,100);
y = sin(x);
y = y ~ y*. }8~\mp@subsup{\textrm{y}}{}{*}.6~\mp@subsup{y}{}{*}.4
against x */
_pdate = ""; /* date is not printed */
_plctrl = { 1, 1, 0, 0 }; /* 2 curves w/symbols, 2
without */
_pltype = { 1, 2, 6, 6 }; /* dashed, dotted, solid
lines */
_pstype = { 1, 2, 0, 0 }; /* symbol types circles,
squares */
_plegctl= { 2, 3, 1.7, 4.5 }; /* legend size and loc-
ations */
_plegstr= "Sin wave 1.\0"\ /* 4 lines legend text */
"Sin wave .8\0"\
"Sin wave .6\0"\
"Sin wave .4";
ylabel("Amplitude")
xlabel("X Axis");
title("Example xy Graph"); /* main title */
xy(x,y);

```
```

/* Y axis label */

```
/* Y axis label */
/* X axis label */
/* X axis label */
```

/* activate PGRAPH library

```
/* activate PGRAPH library
/* reset global variables
/* reset global variables
/* generate data */
/* generate data */
/* 4 curves plotted
/* 4 curves plotted
/* call to main routine */
```

/* call to main routine */

```

Example 3 In this example, two graphics panels are drawn. The first is a full-sized surface representation, and the second is a half-sized inset containing a contour of the same data located in the lower left corner of the window:
```

library pgraph; /* activate pgraph library
*/
/* Generate data for surface and contour plots */
x = seqa (-10,0.1,71)'; /* note x is a row vector
*/
y = seqa(-10,0.1,71); /* note y is a column vec-
tor */
z = cos(5*sin(x) - y); /* z is a 71x71 matrix */
begwind; /* initialize graphics win-
dows */
makewind(9,6.855,0,0,0); /* first window full size
*/
makewind(9/2,6.855/2,1,1,0); /* second window inset to
first */
setwind(1);
*/
graphset;
*/
pzclr = { 1, 2, 3, 4 }; /* set Z level colors */
title("cos(5*sin(x) - y)"); /* set main title */
xlabel("X Axis"); /* set X axis label */
ylabel("Y Axis"); /* set Y axis label */
scale3d(miss(0,0),miss(0,0),-5|5);
surface(x,y,z);
nextwind;
*/
graphset;
*/
_pzclr = { 1, 2, 3, 4 }; /* set Z level colors */
_pbox = 15; /* white border */
contour(x,y,z); /* call contour routine */
endwind;
/* Display windows */

```

While the structure has changed somewhat, the four basic elements of the graphics program are all here. The additional routines begwind, endwind, makewind, nextwind, and setwind are all used to control the graphic panels.

\section*{GAUSS User Guide}

As Example 3 illustrates, the code between graphic panel functions (that is, setwind or nextwind) may include assignments to global variables, a call to graphset, or may set up new data to be passed to the main graphics routines.

You are encouraged to run the example programs supplied with GAUSS. Analyzing these programs is perhaps the best way to learn how to use the PQG system. The example programs are located on the examples subdirectory.

\subsection*{34.2.2 Graphics Coordinate System}

PQG uses a \(4190 \times 3120\) pixel resolution grid on a \(9.0 \times 6.855\)-inch printable area. There are three units of measure supported with most of the graphics global elements:

\section*{Inch Coordinates}

Inch coordinates are based on the dimensions of the full-size 9.0x6.855-inch output page. The origin is \((0,0)\) at the lower left corner of the page. If the picture is rotated, the origin is at the upper left. (For more information, see Inch Units in Graphic Panels, Section 34.3.6 .)

\section*{Plot Coordinates}

Plot coordinates refer to the coordinate system of the graph in the units of the user's X, Y and Z axes.

\section*{Pixel Coordinates}

Pixel coordinates refer to the \(4096 \times 3120\) pixel coordinates of the full-size output page. The origin is \((0,0)\) at the lower left corner of the page. If the picture is rotated, the origin is at the upper left.

\subsection*{34.3 Graphic Panels}

Multiple graphic panels for graphics are supported. These graphic panels allow the user to display multiple graphs on one window or page.

A graphic panel is any rectangular subsection of the window or page. Graphc panels may be any size and position on the window and may be tiled or overlapping, transparent or nontransparent.

\subsection*{34.3.1 Tiled Graphic Panels}

Tiled graphic panels do not overlap. The window can easily be divided into any number of tiled graphic panels with the window command. window takes three parameters: number of rows, number of columns, and graphic panel attribute (1=transparent, \(0=\) noontransparent).

This example will divide the window into six equally sized graphic panels. There will be two rows of three graphic panels-three graphic panels in the upper half of the window and three in the lower half. The attribute value of 0 is arbitrary since there are no other graphic panels beneath them.
```

window(nrows,ncols,attr);
window (2, 3,0);

```

\subsection*{34.3.2 Overlapping Graphic Panels}

Overlapping graphic panels are laid on top of one another as they are created, much as if you were using the cut and paste method to place several graphs together on one page. An overlapping graphic panel is created with the makewind command.

In this example, makewind will create an overlapping graphic panel that is 4 inches wide by 2.5 inches tall, positioned 1 inch from the left edge of the page and 1.5 inches from the bottom of the page. It will be nontransparent:
```

makewind(hsize,vsize,hpos,vpos,attr);
window (2,3,0);
makewind (4, 2.5,1,1.5,0);

```

\subsection*{34.3.3 Nontransparent Graphic Panels}

A nontransparent graphic panel is one that is blanked before graphics information is written to it. Therefore, information in any previously drawn graphic panels that lie under it will not be visible.

\subsection*{34.3.4 Transparent Graphic Panels}

A transparent graphic panel is one that is not blanked, allowing the graphic panel beneath it to "show through". Lines, symbols, arrows, error bars, and other graphics objects may extend from one graphic panel to the next by using transparent graphic panels. First, create the desired graphic panel configuration. Then create a full-window, transparent graphic panel using the makewind or window command. Set the appropriate global variables to position the desired object on the transparent graphic panel. Use the draw procedure to draw it. This graphic panel will act as a transparent "overlay" on top of the other graphic panels. Transparent graphic panels can be used to add text or to superimpose one graphic panel on top of another.

\subsection*{34.3.5 Using Graphic Panel Functions}

The following is a summary of the graphic panel functions:
\begin{tabular}{ll} 
begwind & Graphic panel initialization procedure. \\
endwind & End graphic panel manipulations, display graphs. \\
window & Partition window into tiled graphic panels. \\
makewind & Create graphic panel with specified size and position. \\
setwind & Set to specified graphic panel number. \\
nextwind & Set to next available graphic panel number. \\
getwind & Get current graphic panel number.
\end{tabular}

\section*{savewind \\ loadwind \\ Save graphic panel configuration to a file. \\ Load graphic panel configuration from a file.}

This example creates four tiled graphic panels and one graphic panel that overlaps the other four:
```

library pgraph;
graphset;
begwind;
window(2,2,0); /* Create four tiled graphic
panels (2 rows, 2 columns) */
/* Create graphic panel that
overlaps the tiled graphic
panels */
ysize = 6.855/2;
makewind(xsize,ysize,xsize/2,ysize/2,0);
x = seqa (1,1,1000); /* Create X data */
y =(sin(x) + 1) * 10.; /* Create Y data */
setwind(1); /* Graph 1, upper left corner */
xy(x,y);
nextwind; /* Graph 2, upper rt. corner */
logx(x,y);
nextwind; /* Graph 3, lower left corner */
logy(x,y);
nextwind; /* Graph 4, lower rt. corner */
loglog(x,y);
nextwind; /* Graph 5, center, overlayed */
bar(x,y);
endwind; /* End graphic panel processing,
display graph */

```

\subsection*{34.3.6 Inch Units in Graphic Panels}

Some global variables allow coordinates to be input in inches. If a coordinate value is in inches and is being used in a graphic panel, that value will be scaled to "graphic panel inches" and positioned relative to the lower left corner of the graphic panel. A "graphic panel inch" is a true inch in size only if the graphic panel is scaled to the full window, otherwise X coordinates will be scaled relative to the horizontal graphic panel size and Y coordinates will be scaled relative to the vertical graphic panel size.

\subsection*{34.3.7 Saving Graphic Panel Configurations}

The functions savewind and loadwind allow the user to save graphic panel configurations. Once graphic panels are created (using makewind and window), savewind may be called. This will save to disk the global variables containing information about the current graphic panel configuration. To load this configuration again, call loadwind. (See loadwind in the GAUSS LANGUAGE REFERENCE.

\subsection*{34.4 Graphics Text Elements}

Graphics text elements, such as titles, messages, axes labels, axes numbering, and legends, can be modified and enhanced by changing fonts and by adding superscripting, subscripting, and special mathematical symbols.

To make these modifications and enhancements, the user can embed "escape codes" in the text strings that are passed to title, xlabel, ylabel and asclabel or assigned to _pmsgstr and _plegstr.

The escape codes used for graphics text are:
\begin{tabular}{ll} 
exttt 000 & String termination character (null byte). \\
{\([\)} & Enter superscript mode, leave subscript mode. \\
[ Enter subscript mode, leave superscript mode.
\end{tabular}
@
exttt \(20 n\) Select font number \(n\). (see SELECTING FONTS, following).

The escape code \(\backslash I\) (or \(\backslash I\) ) can be embedded into title strings to create a multiple line title:
```

title("This is the first line\lthis is the second line");

```

A null byte 1000 is used to separate strings in _plegstr and _pmsgstr:
```

_pmsgstr = "First string\000Second string\000Third string";

```
or
```

_plegstr = "Curve 1\000Curve 2";

```

Use [. . ] to create the expression \(M(t)=E\left(e^{t z}\right)\) :
```

_pmsgstr = "M(t) = E(e[tx])";

```

Use @ to generate [ and ] in an X axis label:
```

xlabel("Data used for x is: data@[.,1 2 3@]");

```

\subsection*{34.4.1 Selecting Fonts}

Four fonts are supplied with the Publication Quality Graphics system. They are Simplex, Complex, Simgrma, and Microb. (For a list of the characters available in each font, see PQG Fonts, CHAPTER 35 .)

Fonts are loaded by passing to the fonts procedure a string containing the names of all fonts to be loaded. For example, this statement will load all four fonts:
```

fonts("simplex complex microb simgrma");

```

The fonts command must be called before any of the fonts can be used in text strings. A font can then be selected by embedding an escape code of the form " \(\backslash 20 \mathrm{n}\) " in the string that is to be written in the new font. The \(n\) will be \(1,2,3\) or 4 , depending on the order in which the fonts were loaded in fonts. If the fonts were loaded as in the previous example, the escape characters for each would be:
\begin{tabular}{ll}
\(\backslash 201\) & Simplex \\
\(\backslash 202\) & Complex \\
\(\backslash 203\) & Microb \\
\(\backslash 204\) & Simgrma
\end{tabular}

The following example demonstrates how to select a font for use in a string:
```

title("\201This is the title using Simplex font");
xlabel("\202This is the label for X using Complex font");
ylabel("\203This is the label for Y using Microb font");

```

Once a font is selected, all succeeding text will use that font until another font is selected. If no fonts are selected by the user, a default font (Simplex) is loaded and selected automatically for all text work.

\subsection*{34.4.2 Greek and Mathematical Symbols}

The following examples illustrate the use of the Simgrma font; they assume that Simgrma was the fourth font loaded. (For the available Simgrma characters and their numbers, see PQG Fonts, CHAPTER 35 .) The Simgrma characters are specified by either:
1. The character number, preceeded by a " \(\backslash\) ".
2. The regular text character with the same number.

For example, to get an integral sign \(" \int n\) in Simgrma, embed either a " \(\backslash 044^{\prime \prime}\) or a \(", "\) in a string that has been set to use the Simgrma font.

To produce the title \(f(x)=\sin ^{2}(\pi x)\), the following title string should be used:
```

title("\201f(x) = sin[2](%5C204p%5C201x)");

```

The " \(p\) " (character 112) corresponds to " \(\pi\) " in Simgrma.
To number the major X axis tick marks with multiples of \(\pi / 4\), the following could be passed to asclabel:
```

lab = "\2010 \204p\201/4 \204p\201/2 3\204p\201/4 \204p";
asclabel(lab,0);
xtics(0,pi,pi/4,1);

```
\(\mathbf{x t i c s}\) is used to make sure that major tick marks are placed in the appropriate places. This example will number the X axis tick marks with the labels \(\square^{2}, \square^{1}, 1, \sqcup\), and \(\square^{2}\) :
```

lab = "\204m\201[-2] \204m\201[-1] 1 \204m m\201[2]";
asclabel(lab,0) ;

```

This example illustrates the use of several of the special Simgrma symbols:
```

    pmsgstr = "\2041\2011/2\204p ,\201e[-\204m[\2012]\201/2]
    d\204m";

```

This produces:
\[
\sqrt{ } 1 / 2 \pi \int e^{-\square^{2} / 2} d \square
\]

\subsection*{34.5 Colors}
\begin{tabular}{llcl}
0 & Black & 8 & Dark Grey \\
1 & Blue & 9 & Light Blue \\
2 & Green & 10 & Light Green \\
3 & Cyan & 11 & Light Cyan \\
4 & Red & 12 & Light Red \\
5 & Magenta & 13 & Light Magenta \\
6 & Brown & 14 & Yellow \\
7 & Grey & 15 & White
\end{tabular}

\subsection*{34.6 Global Control Variables}

The following global variables are used to control various graphics elements. Default values are provided. Any or all of these variables can be set before calling one of the main graphing routines. The default values can be modified by changing the declarations in pgraph. dec and the statements in the procedure graphset in pgraph.src. graphset can be called whenever the user wants to reset these variables to their default values.
\(\bar{p}\) ag \(\quad 2 \times 1\) vector, the graph will be shifted to the right and up if this is not 0 .
If this is 0 , the graph will be centered on the output page. Default is 0 . f

Note: Used internally. (For the same functionality, see makewind in the GAUSS LANGUAGE REFERENCE.) This is used by the graphic
panel routines. The user must not set this when using the graphic panel procedures.
\(2 \times 1\) vector, size of the graph in inches on the printer output. Maximum size is \(9.0 \times 6.855\) inches (unrotated) or \(6.855 \times 9.0\) inches (rotated). If this is 0 , the maximum size will be used. Default is 0 .

Note: Used internally. (For the same functionality, see makewind in the GAUSS LANGUAGE REFERENCE). This is used by the graphic panel routines. The user must not set this when using the graphic panel procedures.

Mx11 matrix, draws one arrow per row of the input matrix (for total of M arrows). If scalar zero, no arrows will be drawn.
\begin{tabular}{ll}
{\([M, 1]\)} & \(x\) starting point. \\
{\([M, 2]\)} & \(Y\) starting point. \\
{\([M, 3]\)} & \(x\) ending point. \\
{\([M, 4]\)} & \(Y\) ending point. \\
{\([M, 5]\)} & ratio of the length of the arrow head to half its width. \\
{\([M, 6]\)} & size of arrow head in inches. \\
{\([M, 7]\)} & \begin{tabular}{l} 
type and location of arrow heads. This integer number \\
\\
\\
will be interpreted as a decimal expansion \(m n\), for
\end{tabular} \\
& \(m\), type of arrow head: \\
& \(0 \quad\) solid \\
& \(1 \quad\) empty
\end{tabular}

[M, 11] controls thickness of lines used to draw arrow. This value may be zero or greater. A value of zero is normal line width.

To create two single-headed arrows, located using inches, use
```

parrow ={ { 1 1 2 2 3 0.2 11 10 2 6 0,
342 2 3 0.2 11 10 2 6 0 };

```

Mx12 matrix, draws one 3-D arrow per row of the input matrix (for a total of M arrows). If scalar zero, no arrows will be drawn.
[M, 1] \(\quad \mathrm{x}\) starting point in 3-D plot coordinates.
[M,2] y starting point in 3-D plot coordinates.
[ \(M, 3] \quad \mathrm{z}\) starting point in 3-D plot coordinates.
\([M, 4] \quad \mathrm{x}\) ending point in 3-D plot coordinates.
[ \(M, 5] \quad y\) ending point in 3-D plot coordinates.
\([M, 6] \quad z\) ending point in 3-D plot coordinates.
\([M, 7] \quad\) ratio of the length of the arrow head to half its width.
\([M, 8] \quad\) size of arrow head in inches.
[ \(M, 9] \quad\) type and location of arrow heads. This integer number will be interpreted as a decimal expansion mn . For example: if 10 , then \(m=1, \quad n=0\).
\(m\), type of arrow head:
0 solid

    \(\begin{array}{lllllllllllll}3 & 4 & 5 & 2 & 2 & 2 & 3 & 0.2 & 11 & 10 & 6 & 0 & \} ;\end{array}\)

If this is a scalar, it will be expanded to that value.
For example:
```

/* turn X axis on, Y axis off */
paxes = { 1, 0 };
/* turn all axes off */
paxes = 0;
/* turn all axes on */
_paxes = 1;

``` histograms.
p
The first column controls the bar shading:
0 no shading
1 dots
2 vertical cross-hatch
3 diagonal lines with positive slope
4 diagonal lines with negative slope
5 diagonal cross-hatch
6 solid

The second column controls the bar color, see Colors, Chapter 34.5 .
- scalar, width of bars in bar graphs and histograms. The valid range is
\(\bar{p}\) bo scalar, draws a box (border) around the entire graph. Set to desired
pbo
\(x C t\)
1 \(0-1\). If 0 , the bars will be a single pixel wide. If 1 , the bars will touch each other. Default is 0.5 , so the bars take up about half the space open to them. color of box to be drawn. Use 0 if no box is desired. Default is 0 .
\(5 \times 1\) vector, controls box plot style, width, and color. Used by procedure box only.
[1] box width between 0 and 1. If 0 , the box plot is drawn as two vertical lines representing the quartile ranges with a filled circle representing the 50th percentile.
box color, Colors, Chapter 34.5 . If 0, the colors may be individually controlled using global variable _ pcolor.
[3] \(\min / \max\) style for the box symbol. One of the following:

1 minimum and maximum taken from the actual limits of the data. Elements 4 and 5 are ignored.

2
statistical standard with the minimum and maximum calculated according to interquartile range as follows:
\[
\text { intqrange }=75 \text { th }-25 \text { th }
\]
\[
\begin{aligned}
& \min =25 \text { th }-1.5 \text { intqrange } \\
& \max =75 \text { th }+1.5 \text { intqrange }
\end{aligned}
\]

Elements 4 and 5 are ignored.
3 minimum and maximum percentiles taken from elements 4 and 5 .
\begin{tabular}{ll} 
[4] & minimum percentile value \((0-100)\) if_pboxctl [3] \\
\(=3\).
\end{tabular}
[5] \begin{tabular}{l} 
maximum percentile value \((0-100)\) if_pboxctl [3] \\
\(=3\).
\end{tabular}
- \(5 x\) M output matrix containing computed percentile results from procedure box. \(M\) corresponds to each column of input \(y\) data.
\begin{tabular}{ll}
{\([1, M]\)} & minimum whisker limit according to _pboxct \(1[3]\). \\
{\([2, M]\)} & 25 th percentile (bottom of box). \\
{\([3, M]\)} & 50th percentile (median). \\
{\([4, M]\)} & 75th percentile (top of box). \\
{\([5, M]\)} & \begin{tabular}{l} 
maximum whisker limit according to _pboxct 1
\end{tabular} \\
& {\([3]\).}
\end{tabular}
\(\bar{p}_{\text {po }} \quad\) scalar or Kx1 vector, colors for main curves in \(x y, x y z\) and \(\mathbf{l o g}\)
graphs. To use a single color set for all curves set this to a scalar color value. If 0 , use default colors. Default is 0 .

The default colors come from a global vector called_pcsel. This vector can be changed by editing pgraph. dec to change the
default colors, see Colors, Chapter 34.5 (pcsel is not documented elsewhere).
\(-\quad\) scalar or \(1 \times 5\) vector, allows plot cropping for different graphic
pcr op
crop main curves/symbols.
[2] crop lines generated using_pline.
[3] crop arrows generated using parrow.
[4] crop circles/arcs generated using_pline.
[5] crop symbols generated using _psym.
This example will crop main curves, and lines and circles drawn by pline.
```

pcrop = { 1 1 0 1 0 };

```
scalar. If 1 , the axes will intersect at the \((0,0) \mathrm{X}-\mathrm{Y}\) location if it is visible. Default is 0 , meaning the axes will be at the lowest end of the \(\mathrm{X}-\mathrm{Y}\) coordinates.
date string. If this contains characters, the date will be appended and printed.

The default is set as follows (the first character is a font selection escape code):
```

_pdate = "\201GAUSS ";

```

If this is set to a null string, no date will be printed. (For more information on using fonts within strings, see Graphics Text Elements, Section 34.4 .
\begin{tabular}{|c|c|}
\hline [ \(M, 1\) ] & x location. \\
\hline [M, 2] & left end of error bar. \\
\hline [ \(M, 3]\) & right end of error bar. \\
\hline [M, 4] & y location. \\
\hline [M, 5] & bottom of error bar. \\
\hline [M, 6] & top of error bar. \\
\hline [ \(M, 7]\) & line type: \\
\hline & 1 dashed \\
\hline & 2 dotted \\
\hline & 3 short dashes \\
\hline & 4 closely spaced dots \\
\hline & 5 dots and dashes \\
\hline & 6 solid \\
\hline [ \(M, 8\) ] & color, see Colors, CHAPTER 34.5 \\
\hline
\end{tabular}
[ \(M, 9] \quad\) line thickness. This value may be 0 or greater. A value of 0 is normal line width.

To create one error bar using solid lines, use
```

_perrbar = { 1 0 2 2 1 3 6 2 0 };

```
\(\bar{p} f r\) ame
\(2 \times 1\) vector, controls frame around axes area. On 3-D plots this is a cube surrounding the 3-D workspace.
\begin{tabular}{ll}
1 & frame on \\
0 & frame off
\end{tabular}
[2]
1 tick marks on frame
0
no tick marks
The default is a frame with tick marks.
\(2 \times 1\) vector to control grid.
[1] grid through tick marks:
0 no grid
1 dotted grid
2 fine dotted grid
3 solid grid
[2] grid subdivisions between major tick marks:

0 no subdivisions
1 dotted lines at subdivisions
2 tick marks only at subdivisions
The default is no grid and tick marks at subdivisions.
gct If scalar 0, no legend is drawn (default). If nonzero scalar, create legend displayed for the main curves. This also controls the frequency of symbols on main curves. The number of rows \((\mathrm{K})\) is equal to the number of individual curves to be plotted in the graph. Default is 0 .

0 draw line only.
>0 draw line and symbols every _plctrl points.
\(<0 \quad\) draw symbols only every _plctrl points.
-1 all of the data points will be plotted with no connecting lines.

This example draws a line for the first curve, draws a line and plots a symbol every 10 data points for the second curve, and plots symbols only every 5 data points for the third curve:
```

plctrl = { 0, 10, -5 };

```
scalar or 1 x 4 vector, legend control variable. in the default location in the lower right of the page. scalar or Kx1 vector to control whether lines and/or symbols will be

If 1 x 4 vector, set as follows:
[1] legend position coordinate units:
1 coordinates are in plot coordinates

2 coordinates are in inches
coordinates are in pixel
[2] legend text font size, where \(1<=\) size \(<=9\). Default is 5.
[3] x coordinate of lower left corner of legend box.
[4] y coordinate of lower left corner of legend box.
This example puts a legend in the lower right corner:
```

plegctl = 1;

```

This example creates a smaller legend and positions it 2.5 inches from the left and 1 inch from the bottom.
```

_plegctl = { 2 3 2.5 1 };

```
string, legend entry text. Text for multiple curves is separated by a null byte (" 1000 ").

For example:
```

_plegstr = "Curve 1\000Curve 2\000Curve 3";

```
\(\bar{p} 1 e\)

Mx9 matrix, to draw lines, circles, or radii. Each row controls one item to be drawn. If this is a scalar zero, nothing will be drawn. Default is 0 .
[M,I] item type and coordinate system:
1 line in plot coordinates
\begin{tabular}{|c|c|c|}
\hline & 2 & line in inch coordinates \\
\hline & 3 & line in pixel coordinates \\
\hline & 4 & circle in plot coordinates \\
\hline & 5 & circle in inch coordinates \\
\hline & 6 & radius in plot coordinates \\
\hline & 7 & radius in inch coordinates \\
\hline \multirow[t]{7}{*}{[M, 2]} & line type: & \\
\hline & 1 & dashed \\
\hline & 2 & dotted \\
\hline & 3 & short dashes \\
\hline & 4 & closely spaced dots \\
\hline & 5 & dots and dashes \\
\hline & 6 & solid \\
\hline [M, 3- & \multicolumn{2}{|l|}{coordinates and dimensions:} \\
\hline 7] & \multicolumn{2}{|l|}{if item type is line ( \(1<=\) pline \([M, 1]<=3\) ):} \\
\hline & [ \(M, 3\) ] & x starting point. \\
\hline & [M, 4] & y starting point. \\
\hline & [M,5] & x ending point. \\
\hline & [M, 6] & \(y\) ending point. \\
\hline & [M, 7] & 0 if this is a continuation of a curve, 1 if this begins a new curve. \\
\hline
\end{tabular}
\begin{tabular}{|c|c|}
\hline [ \(M, 3]\) & \(x\) center of circle. \\
\hline [ \(M, 4\) ] & \(y\) center of circle. \\
\hline [ \(M, 5\) ] & radius. \\
\hline [ \(M, 6]\) & starting point of arc in radians. \\
\hline [ \(M, 7]\) & ending point of are in radians. \\
\hline
\end{tabular}
if item type is radius (_pline \([M, 1]=6\) or_pline \([M, 1]=7\) ):
\([M, 3] \quad \mathrm{x}\) center of circle.
[M, 4] y center of circle.
\([M, 5] \quad\) beginning point of radius, 0 is the center of the circle.
\([M, 6] \quad\) ending point of radius.
[ \(M, 7] \quad\) angle in radians.
[M, 8] color, see COLORS, CHAPTER 34.5.
[M, 9] controls line thickness. This value may be zero or greater. A value of zero is normal line width.

Mx9 matrix. Allows extra lines to be added to an \(x y z\) or surface graph in 3-D plot coordinates.
\[
[M, I] \quad \mathrm{x} \text { starting point. }
\]


If scalar 0 , there will be no shift. Default is 0 .
Note: Used internally. (For the same functionality, see axmargin in the GAUSS Language Reference.) This is used by the graphic panel routines. The user must not set this when using the graphic panel procedures.
pl \(2 \times 1\) vector, size of the axes area in inches. If scalar 0 , the maximum

Note: Used internally. (For the same functionality, see axmargin in the GAUSS LANGUAGE REFERENCE.) This is used by the graphic panel routines. The user must not set this when using the graphic panel procedures.
\(\begin{array}{ll}\bar{p} \text { It } & \text { scalar or Kx1 vector, line type for the main curves. If this is a nonzero } \\ \text { ype } & \text { scalar, all lines will be this type. If scalar } 0 \text {, line types will be default }\end{array}\)
\(\begin{array}{ll}\bar{p} \text { It } & \text { Scalar or Kx1 vector, line type for the main curves. If this is a nonzero } \\ \text { ype } & \text { scalar, all lines will be this type. If scalar } 0 \text {, line types will be default }\end{array}\) styles. Default is 0 .
\begin{tabular}{ll}
1 & dashed \\
2 & dotted \\
3 & short dashes \\
4 & closely spaced dots \\
5 & dots and dashes \\
6 & solid
\end{tabular}

The default line types come from a global vector called _plsel.
This vector can be changed by editing pgraph. dec to change the
The default line types come from a global vector called_plsel.
This vector can be changed by editing pgraph. dec to change the default line types ( \(\_\)plsel is not documented elsewhere.)

\section*{\(\bar{p} 1 W\)} idt
size will be used.
scalar or Kx1 vector, line thickness for main curves. This value may be zero or greater. A value of zero is normal (single pixel) line width.\(h \quad\) Default is 0 .
\(\bar{p}_{\text {pmc }} \quad 9 \times 1\) vector, color values to use for plot, see COLORS, CHAPTER 34.5.
olo
r
    [1] axes.
    [2] axes numbers.
    [3] X axis label.
    [4] Y axis label.
    [5] Z axis label.
    [6] title.
    [7] box.
    [8] date.
    [9] background.
    If this is scalar, it will be expanded to a \(9 \times 1\) vector.
\(\bar{p}_{\text {pms }} \quad\) Lx 7 matrix of control information for printing the strings contained in
gct
_pmsgstr.
1
[ \(L, 1] \quad\) horizontal location of lower left corner of string.
\([L, 2] \quad\) vertical location of lower left corner of string.
[ \(L, 3] \quad\) character height in inches.
\([L, 4] \quad\) angle in degrees to print string. This may be -180 to 180 relative to the positive X axis.
\begin{tabular}{lll}
{\([L, 5]\)} & \multicolumn{1}{l}{ location coordinate system. } \\
& 1 & location of string in plot coordinates \\
{\([L, 6]\)} & 2 & location of string in inches \\
{\([L, 7]\)} & \begin{tabular}{l} 
color. \\
font thickness, may be 0 or greater. If 0 use normal line \\
width.
\end{tabular}
\end{tabular}
\({ }_{\text {pms }} \quad\) string, contains a set of messages to be printed on the plot. Each message is separated from the next by a null byte ( \((000)\). The number of messages must correspond to the number of rows in the \(\qquad\) pmsgetl control matrix. This can be created as follows:
```

_pmsgstr = "Message one.\000Message two.";

```
- scalar, controls window output during the creation of the graph.

\section*{pno}
tif y

Default is 1 .

0 no activity to the window while writing . tkf file.

1 display progress as fonts are loaded, and .tkf file is being generated.
scalar, \(2 \times 1\) or \(3 \times 1\) vector for independent control for axes numbering. The first element controls the X axis numbers, the second controls the Y axis numbers, and the third (if set) controls the Z axis numbers. Default is 1 .

If this value is scalar, it will be expanded to a vector.
0 no axes numbers displayed
axes numbers displayed, vertically oriented on axis
2 axes numbers displayed, horizontally oriented on axis For example:
```

pnum = { 0, 2 }; /* no X axis numbers, *//*
horizontal on Y axis */

```
- \(n\) nu
scalar, size of axes numbers in inches. If 0 , a size of .13 will be used. Default is 0 .
scalar. If 0 , no rotation, if 1 , plot will be rotated 90 degrees. Default is pro tat
e
scalar. If 0, a beep will sound when the graph is finished drawing to the window. Default is 1 (no beep).
0 .
- \({ }^{-}\)scalar. If 1, display graph in window, if 0 , do not display graph in window. Default is 1 .
scalar or Kx1 vector, controls symbol used at data points. To use a single symbol type for all points, set this to one of the following scalar values:
1 circle
2 square
triangle
\begin{tabular}{ll}
4 & plus \\
5 & diamond \\
6 & inverted triangle \\
7 & star \\
8 & solid circle \\
9 & solid square \\
10 & solid triangle \\
11 & solid plus \\
12 & solid diamond \\
13 & solid inverted triangle \\
14 & solid star
\end{tabular}

If this is a vector, each line will have a different symbol. Symbols will repeat if there are more lines than symbol types. Default is 0 (no symbols are shown).

\section*{psu} rf
[1] if 1 , show hidden lines. Default is 0 .
[2] color for base, see Colors, CHAPTER 34.5. The base is an outline of the \(\mathrm{X}-\mathrm{Y}\) plane with a line connecting
each corner to the surface. If 0 , no base is drawn.
Default is 7 .
\(\bar{p} s y\)
m
Mx7 matrix, M extra symbols will be plotted.
[M, I] x location.
[ \(M, 2]\) y location.
[M,3] symbol type, see _pstype earlier.
[ \(M, 4]\) symbol height. If this is 0 , a default height of 5.0 will be used.
[ \(M, 5]\) symbol color, see Colors, Chapter 34.5 .
[ \(M, 6]\) type of coordinates:
1 plot coordinates
2 inch coordinates
[ \(M, 7] \quad\) line thickness. A value of zero is normal line width.
\(\begin{array}{ll}\bar{p}_{\text {py }} & \text { Mx7 matrix for plotting extra symbols on a 3-D (surface or } x y z \text { ) } \\ \text { m3d }^{2} & \text { graph. }\end{array}\)
[M, I] x location in plot coordinates.
[ \(M, 2] \quad y\) location in plot coordinates.
\([M, 3] \quad \mathrm{z}\) location in plot coordinates.
[M, 4] symbol type, see _pstype earlier.
[ \(M, 5] \quad\) symbol height. If this is 0 , a default height of 5.0 will be used.
[ \(M, 6]\) symbol color, see Colors, Chapter 34.5 .
\([M, 7] \quad\) line thickness. A value of 0 is normal line width.
Use _psym for plotting extra symbols in inch coordinates.
\(\bar{p}\) -
string, name of Tektronix format graphics file. This must have a suppressed. The default is graphic.tkf.
\(\bar{p} t\)
scalar, the height of the title characters in inches. If this is 0 , a default height of approx. 0.13 inch will be used.
string, the graphics version number.
scalar, the maximum number of places to the right of the decimal point for the X axis numbers. Default is 12 .
scalar, the threshold in digits above which the data for the X axis will be scaled and a power of 10 scaling factor displayed. Default is 4 .
scalar, the maximum number of places to the right of the decimal point for the Y axis numbers. Default is 12 .
[1] magnification value. 1 is normal size.
[2] horizontal center of zoomed plot (0-100).
[3] vertical center of zoomed plot (0-100).
To see the upper left quarter of the screen magnified 2 times use:
scalar, the maximum number of places to the right of the decimal
scalar, the threshold in digits above which the data for the Y axis will
be scaled and a power of 10 scaling factor displayed. Default is 4 .
scalar, row vector, or Kx2 matrix, Z level color control for procedures LANGUAGE REFERENCE.)

1x3 row vector, magnifies the graphics display for zooming in on Default is 0 .
```

pzoom = { 2 25 75 };

```
```

pzoom = { 2 25 75 };

``` point for the Z axis numbers. Default is 3 .
scalar, the threshold in digits above which the data for the Z axis will be scaled and a power of 10 scaling factor displayed. Default is 4 .

\section*{35 PQG Fonts}

There are four fonts available in the Publication Quality Graphics System:
\begin{tabular}{ll} 
Simplex & standard sans serif font \\
Simgrma & Simplex greek, math \\
Microb & bold and boxy \\
complex & standard font with serif
\end{tabular}

The following tables show the characters available in each font and their ASCII values. (For details on selecting fonts for your graph, see Selecting Fonts, Section 34.4.1 .)

\subsection*{35.1 Simplex}

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\begin{tabular}{|c|c|c|c|c|c|c|}
\hline 33 & ! & 61 & \(=\) & 89 & Y & 117 \\
\hline 34 & " & 62 & > & 90 & Z & 118 \\
\hline 35 & \# & 63 & ? & 91 & [ & 119 \\
\hline 36 & \$ & 64 & @ & 92 & \(\backslash\) & 120 \\
\hline 37 & \% & 65 & A & 93 & 1 & 121 \\
\hline 38 & \& & 66 & B & 94 & - & 122 \\
\hline 39 & , & 67 & C & 95 & - & 123 \\
\hline 40 & ( & 68 & D & 96 & . & 124 \\
\hline 41 & ) & 69 & E & 97 & - & 125 \\
\hline 42 & * & 70 & F & 98 & b & 126 \\
\hline 43 & + & 71 & G & 99 & c & \\
\hline 44 & , & 72 & H & 100 & d & \\
\hline 45 & - & 73 & 1 & 101 & e & \\
\hline 46 & . & 74 & \(\checkmark\) & 102 & f & \\
\hline 47 & 1 & 75 & K & 103 & g & \\
\hline 48 & 0 & 76 & L & 104 & h & \\
\hline 49 & 1 & 77 & M & 105 & i & \\
\hline 50 & 2 & 78 & N & 106 & j & \\
\hline 51 & 3 & 79 & 0 & 107 & k & \\
\hline 52 & 4 & 80 & P & 108 & । & \\
\hline 53 & 5 & 81 & Q & 109 & m & \\
\hline 54 & 6 & 82 & R & 110 & n & \\
\hline 55 & 7 & 83 & S & 111 & \(\bigcirc\) & \\
\hline 56 & 8 & 84 & T & 112 & p & \\
\hline 57 & 9 & 85 & U & 113 & q & \\
\hline 58 & : & 86 & V & 114 & r & \\
\hline 59 & ; & 87 & W & 115 & s & \\
\hline 60 & \(<\) & 88 & X & 116 & t & \\
\hline
\end{tabular}
35.2 Simgrma
\begin{tabular}{|c|c|c|c|c|c|c|}
\hline 33 & \(\epsilon\) & 61 & \(\neq\) & 89 & \(\psi\) & 117 v \\
\hline 34 & 1 & 62 & \(\geqq\) & 90 & z & 118） \\
\hline 35 & \(\equiv\) & 63 & \(\simeq\) & 91 & ［ & \(119 \omega\) \\
\hline 36 & \(\approx\) & 64 & \(\cup\) & 92 & a & \(120 \xi\) \\
\hline 37 & \(\uparrow\) & 65 & \(\frac{1}{2}\) & 93 & ］ & \(121 \psi\) \\
\hline 38 & \(\checkmark\) & 66 & \(\frac{1}{3}\) & 94 & \(\bigcirc\) & 122 \} \\
\hline 39 & ， & 67 & H & 95 & \(\downarrow\) & 123 \\
\hline 40 & c & 68 & \(\triangle\) & 96 & \(\sim\) & 124 \\
\hline 41 & \(\bigcirc\) & 69 & \(\frac{1}{8}\) & 97 & \(\alpha\) & 125 \\
\hline 42 & \(\times\) & 70 & 中 & 98 & \(\beta\) & 126 ～ \\
\hline 43 & \(\pm\) & 71 & 「 & 99 & \(\eta\) & \\
\hline 44 & \(\int\) & 72 & \(x\) & 100 & \(\delta\) & \\
\hline 45 & 干 & 73 & 3 & 101 & \(\varepsilon\) & \\
\hline 46 & － & 74 & \(\perp\) & 102 & \(\varphi\) & \\
\hline 47 & \(\div\) & 75 & \({ }_{6}\) & 103 & \(\gamma\) & \\
\hline 48 & \(\nabla\) & 76 & \(\wedge\) & 104 & \(\chi\) & \\
\hline 49 & \(\checkmark\) & 77 & 8 & 105 & \(\iota\) & \\
\hline 50 & \(\oint\) & 78 & \％ & 106 & \(t\) & \\
\hline 51 & & 79 & \(\frac{1}{4}\) & 107 & \(\kappa\) & \\
\hline 52 & & 80 & \(\square\) & 108 & \(\lambda\) & \\
\hline 53 & 1 & 81 & \(\bigcirc\) & 109 & \(\mu\) & \\
\hline 54 & 3 & 82 & P & 110 & \(\nu\) & \\
\hline 55 & ｜｜ & 83 & \(\Sigma\) & 111 & － & \\
\hline 56 & \(\infty\) & 84 & ふ & 112 & \(\pi\) & \\
\hline 57 & \(\odot\) & 85 & \(r\) & 113 & \(v\) & \\
\hline 58 & \(\rightarrow\) & 86 & \(\leftrightarrow\) & 114 & p & \\
\hline 59 & \(\leftarrow\) & 87 & \(\Omega\) & 115 & \(\sigma\) & \\
\hline 60 & \(\leqq\) & 88 & 三 & 116 & \(\tau\) & \\
\hline
\end{tabular}

35．3 Microb

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\begin{tabular}{|c|c|c|c|c|c|c|c|}
\hline 33 & \(!\) & 61 & \(=\) & 89 & Y & 117 & \(u\) \\
\hline 34 & " & 62 & > & 90 & z & 118 & \(\checkmark\) \\
\hline 35 & \# & 63 & ? & 91 & [ & 119 & \(w\) \\
\hline 36 & \$ & 64 & @ & 92 & \(\backslash\) & 120 & \(\times\) \\
\hline 37 & \% & 65 & A & 93 & ] & 121 & y \\
\hline 38 & \& & 66 & B & 94 & - & 122 & z \\
\hline 39 & , & 67 & C & 95 & - & 123 & 1 \\
\hline 40 & [ & 68 & D & 96 & - & 124 & 1 \\
\hline 41 & ] & 69 & E & 97 & a & 125 & ) \\
\hline 42 & * & 70 & F & 98 & b & 126 & \(\sim\) \\
\hline 43 & + & 71 & 6 & 99 & c & & \\
\hline 44 & , & 72 & H & 100 & d & & \\
\hline 45 & - & 73 & I & 101 & e & & \\
\hline 46 & . & 74 & \(J\) & 102 & f & & \\
\hline 47 & 1 & 75 & K & 103 & g & & \\
\hline 48 & 0 & 76 & L & 104 & h & & \\
\hline 49 & 1 & 77 & M & 105 & i & & \\
\hline 50 & 2 & 78 & N & 106 & j & & \\
\hline 51 & 3 & 79 & 0 & 107 & k & & \\
\hline 52 & 4 & 80 & P & 108 & । & & \\
\hline 53 & 5 & 81 & Q & 109 & m & & \\
\hline 54 & 6 & 82 & R & 110 & n & & \\
\hline 55 & 7 & 83 & S & 111 & \(\bigcirc\) & & \\
\hline 56 & 8 & 84 & T & 112 & p & & \\
\hline 57 & 9 & 85 & U & 113 & q & & \\
\hline 58 & : & 86 & v & 114 & \(r\) & & \\
\hline 59 & : & 87 & W & 115 & s & & \\
\hline 60 & \(<\) & 88 & x & 116 & t & & \\
\hline
\end{tabular}

\subsection*{35.4 Complex}

\section*{PQG Fonts}
\begin{tabular}{|c|c|c|c|c|c|c|c|}
\hline 33 & ! & 61 & \(=\) & 89 & Y & 117 & u \\
\hline 34 & " & 62 & \(>\) & 90 & Z & 118 & v \\
\hline 35 & \# & 63 & ? & 91 & [ & 119 & w \\
\hline 36 & \$ & 64 & (a) & 92 & \} & 120 & x \\
\hline 37 & \% & 65 & A & 93 & ] & 121 & y \\
\hline 38 & \& & 66 & B & 94 & - & 122 & Z \\
\hline 39 & , & 67 & C & 95 & - & 123 & \{ \\
\hline 40 & ( & 68 & D & 96 & , & 124 & 1 \\
\hline 41 & ) & 69 & E & 97 & a & 125 & \} \\
\hline 42 & * & 70 & F & 98 & b & 126 & \(\sim\) \\
\hline 43 & \(+\) & 71 & G & 99 & c & & \\
\hline 44 & , & 72 & H & 100 & d & & \\
\hline 45 & - & 73 & I & 101 & e & & \\
\hline 46 & . & 74 & J & 102 & f & & \\
\hline 47 & / & 75 & K & 103 & g & & \\
\hline 48 & 0 & 76 & L & 104 & h & & \\
\hline 49 & 1 & 77 & M & 105 & i & & \\
\hline 50 & 2 & 78 & N & 106 & j & & \\
\hline 51 & 3 & 79 & 0 & 107 & k & & \\
\hline 52 & 4 & 80 & P & 108 & 1 & & \\
\hline 53 & 5 & 81 & Q & 109 & m & & \\
\hline 54 & 6 & 82 & R & 110 & n & & \\
\hline 55 & 7 & 83 & S & 111 & - & & \\
\hline 56 & 8 & 84 & T & 112 & P & & \\
\hline 57 & 9 & 85 & U & 113 & q & & \\
\hline 58 & : & 86 & V & 114 & r & & \\
\hline 59 & ; & 87 & W & 115 & s & & \\
\hline 60 & \(<\) & 88 & X & 116 & t & & \\
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